

# Chromo-Weibel plasma instabilities in Bjorken expansion \*

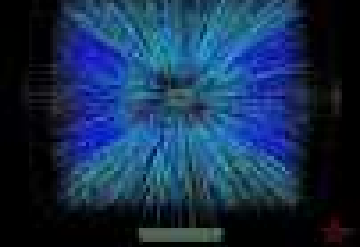
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Institute for Theoretical Physics, TU Vienna

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\*“ Dans la vie, rien n'est à craindre, tout est à comprendre.” Marie Curie



# Hard Expanding Loops (HEL)

## Hard Expanding Loops (HEL)

Weibel instabilities

Scales QGP

Hard (Thermal)

Loops -

Boltzmann -

Vlasov

Notations for

Bjorken expansion

Plasma

Instabilities

## Hard Expanding Loops (HEL)

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Hard (Thermal) Loops - Boltzmann - Vlasov

Notations for Bjorken expansion

## Plasma Instabilities

Expanding 1D+3V Abelian plasma

Expanding 3D+5V plasma

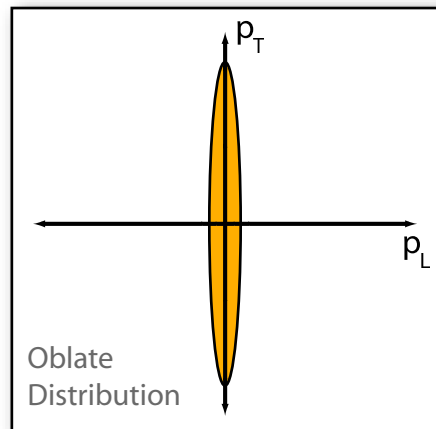
Conclusions

# Weibel instabilities

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Induced Current  
Magnetic Fluctuation

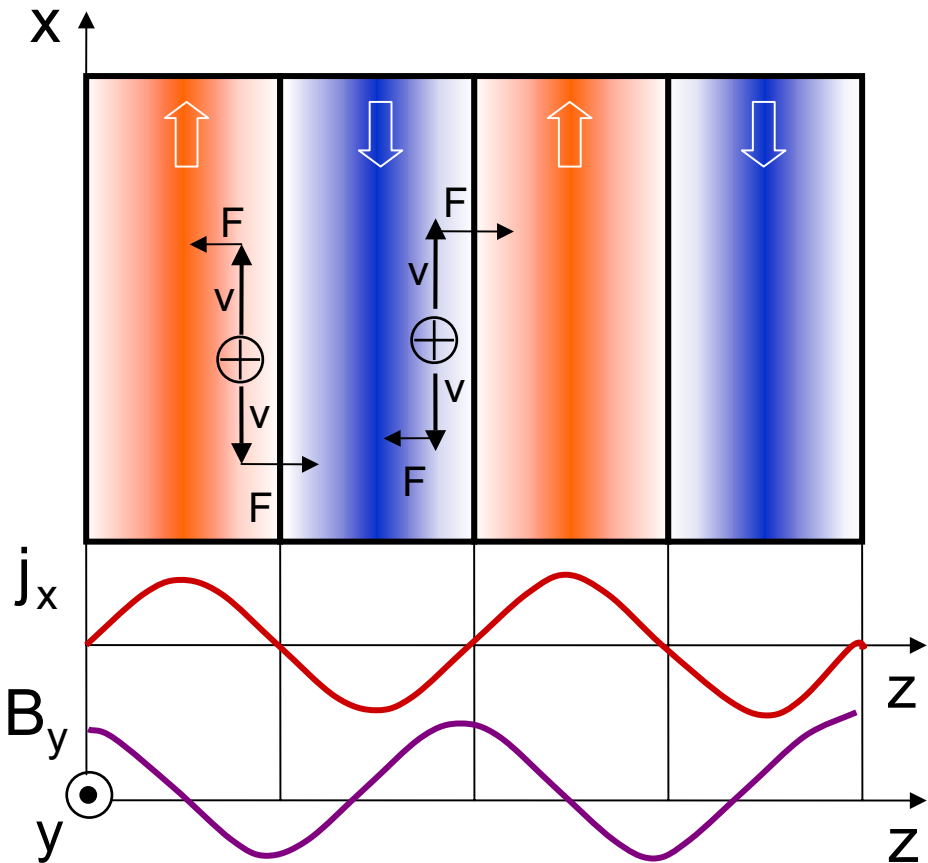


Illustration of the mechanism of filamentation instabilities.

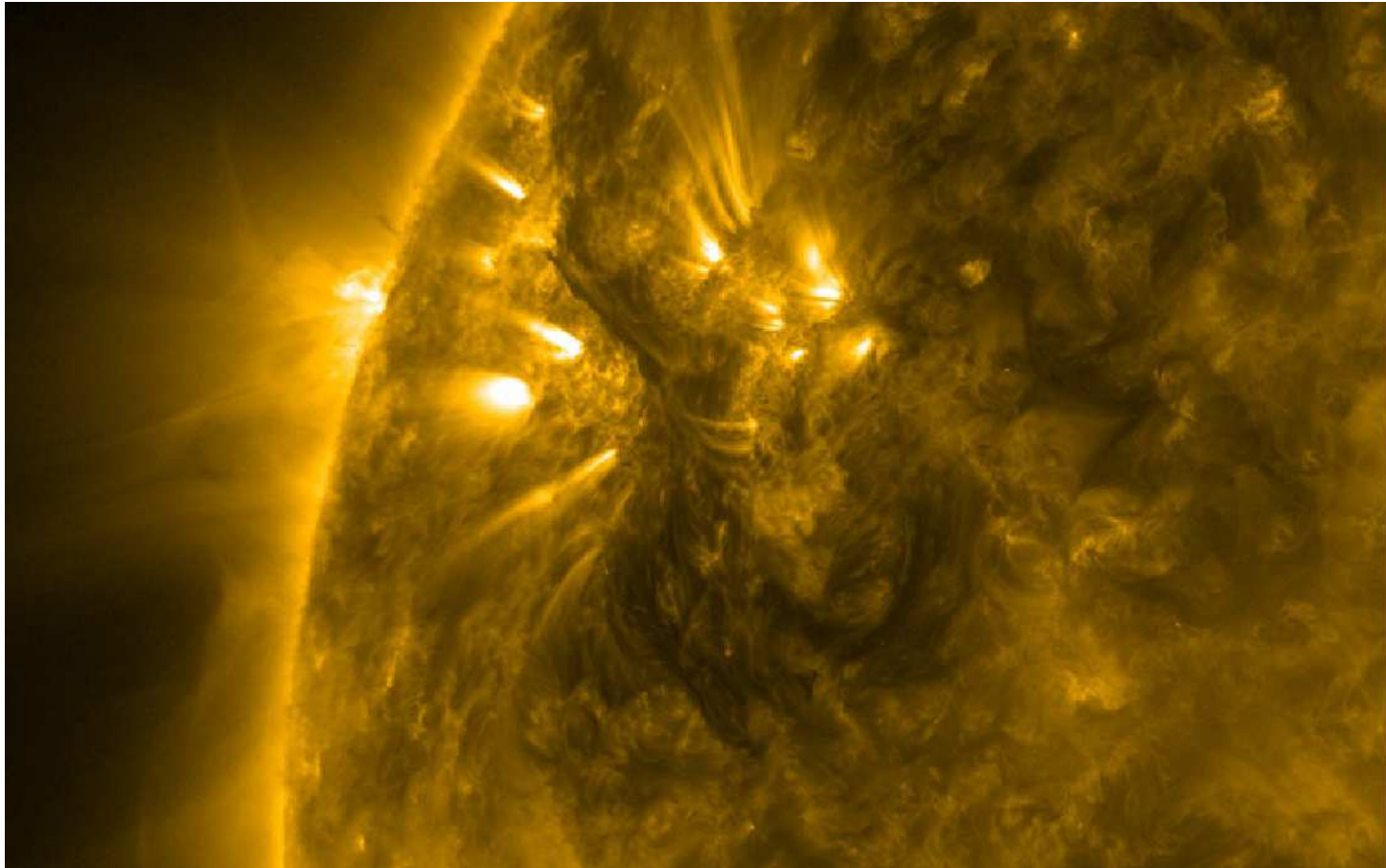
# QED Plasma

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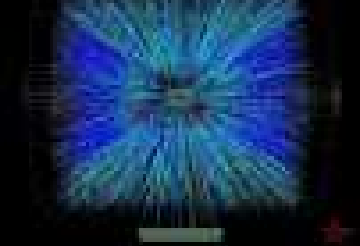
Plasma  
Instabilities

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Filaments and active solar region from NASA's Solar Dynamics Observatory

# Scales of weakly coupled QGP



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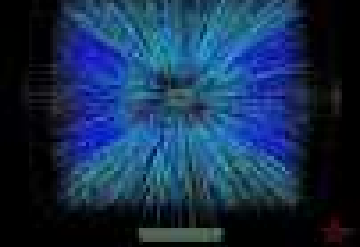
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- $T$ : energy of hard particles
- $gT$ : thermal masses, Debey screening mass, Landau damping, **plasma instabilities** [Mrowczynski 1988, 1993, ..]
- $g^2T$ : magnetic confinement, color relaxation, rate for small angle scattering
- $g^4T$ : rate for large angle scattering,  $\eta^{-1}T^4$



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# Hard (Thermal) Loops - Boltzmann - Vlasov

With color-neutral background distribution  $v \cdot \partial f_0(\mathbf{p}, \mathbf{x}, t) = 0$ ,  
 $v^\mu = p^\mu / p^0$  gauge covariant Boltzmann-Vlasov:

$$v \cdot D \partial f_a(\mathbf{p}, \mathbf{x}, t) = g v_\mu F_a^{\mu\nu} \partial_\nu^{(p)} f_0(\mathbf{p}, \mathbf{x}, t) \quad (1)$$

$$D_\mu F_a^{\mu\nu} = j_a^\nu = g \int \frac{d^3 p}{(2\pi)^3} \frac{p^\mu}{2p^0} \delta f_a(\mathbf{p}, \mathbf{x}, t). \quad (2)$$

- isotropic:  $f_0(\mathbf{p}) = f_0(|\mathbf{p}|)$ ,  $\nabla_{\mathbf{p}} f_0 \propto \mathbf{v}$

$$v \cdot D \delta f_a(\mathbf{p}, \mathbf{x}, t) = -g \mathbf{E}_a \cdot \nabla_{\mathbf{p}} f_0 \quad (stable) \quad (3)$$

- anisotropic:  $f_0(\mathbf{p})$ ,  $\nabla_{\mathbf{p}} f_0 \not\propto \mathbf{v}$

$$v \cdot D \delta f_a(\mathbf{p}, \mathbf{x}, t) = -g (\mathbf{E}_a + \mathbf{v} \times \mathbf{B}_a) \cdot \nabla_{\mathbf{p}} f_0 \quad (unstable!) \quad (4)$$

# Notations for Bjorken expansion

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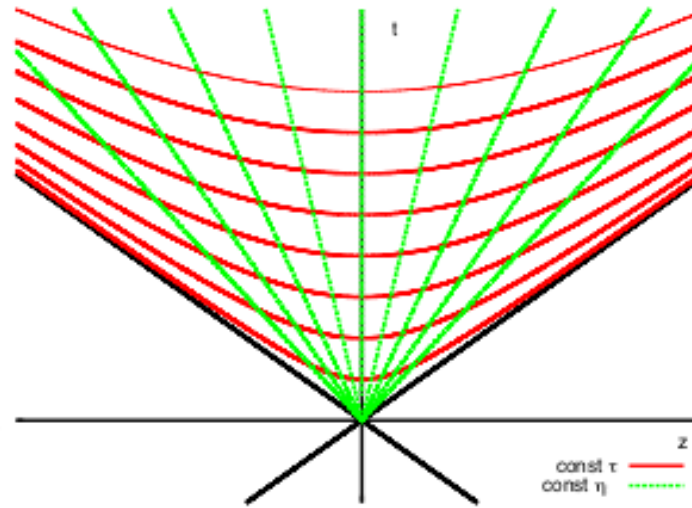
Loops -

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Notations for  
Bjorken expansion

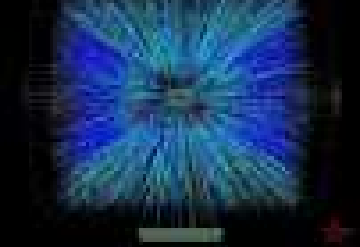
Plasma  
Instabilities



It is convenient to switch to comoving coordinates

$$\begin{aligned} t &= \tau \cosh \eta, & \beta &= \tanh \eta, \\ z &= \tau \sinh \eta, & \gamma &= \cosh \eta, \end{aligned} \quad (5)$$

with corresponding metric  $ds^2 = d\tau^2 - d\mathbf{x}_\perp^2 - \tau^2 d\eta^2$ .



# Plasma Instabilities

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Expanding 1D+3V  
Abelian plasma  
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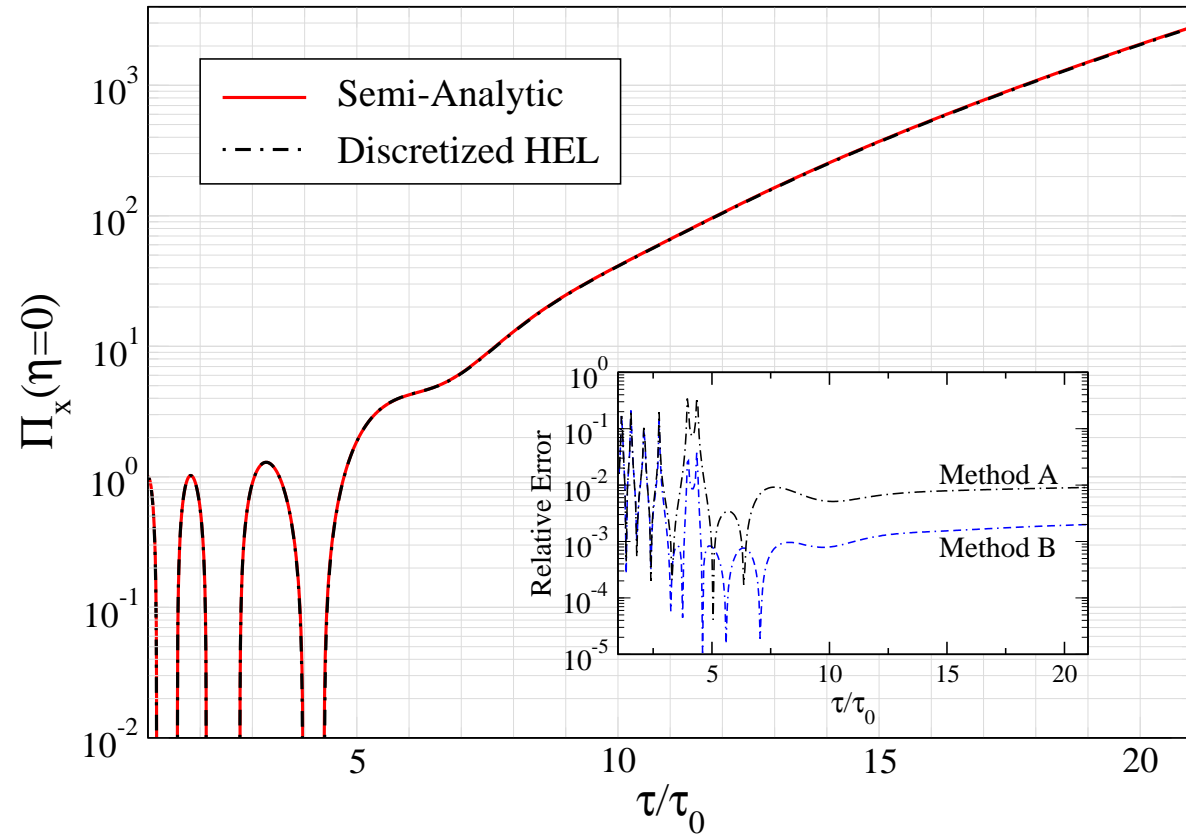
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# Expanding 1D+3V Abelian plasma

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The proper-time evolution of the canonical field momentum of a single Abelian mode.

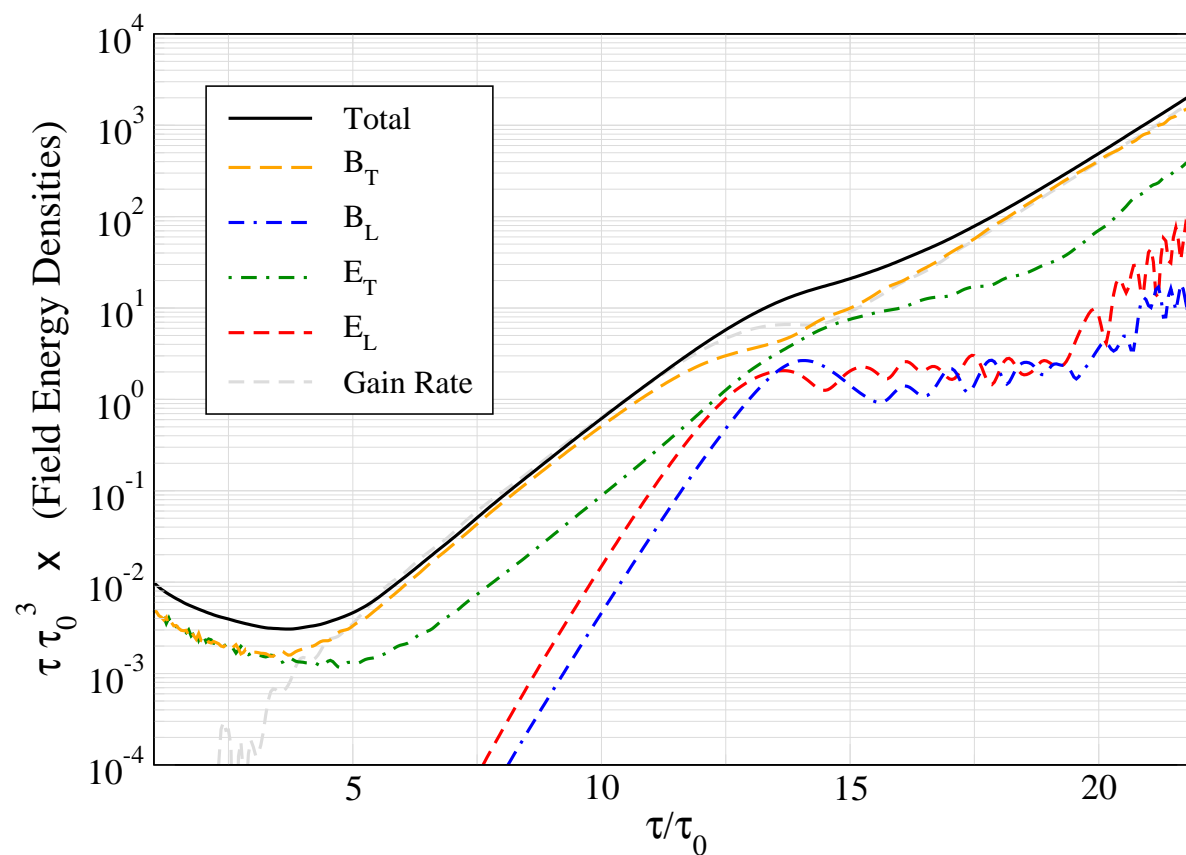
# Expanding 1D+3V non-Abelian plasma

Hard Expanding  
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Expanding 3D+5V  
plasma

Conclusions



The proper-time dependence of the chromo-field energy densities and the energy gain rate times an extra factor of  $\tau_0$  resulting from non-Abelian run initialized with Fukushima, Gelis, and McLerran (FGM) initial conditions.

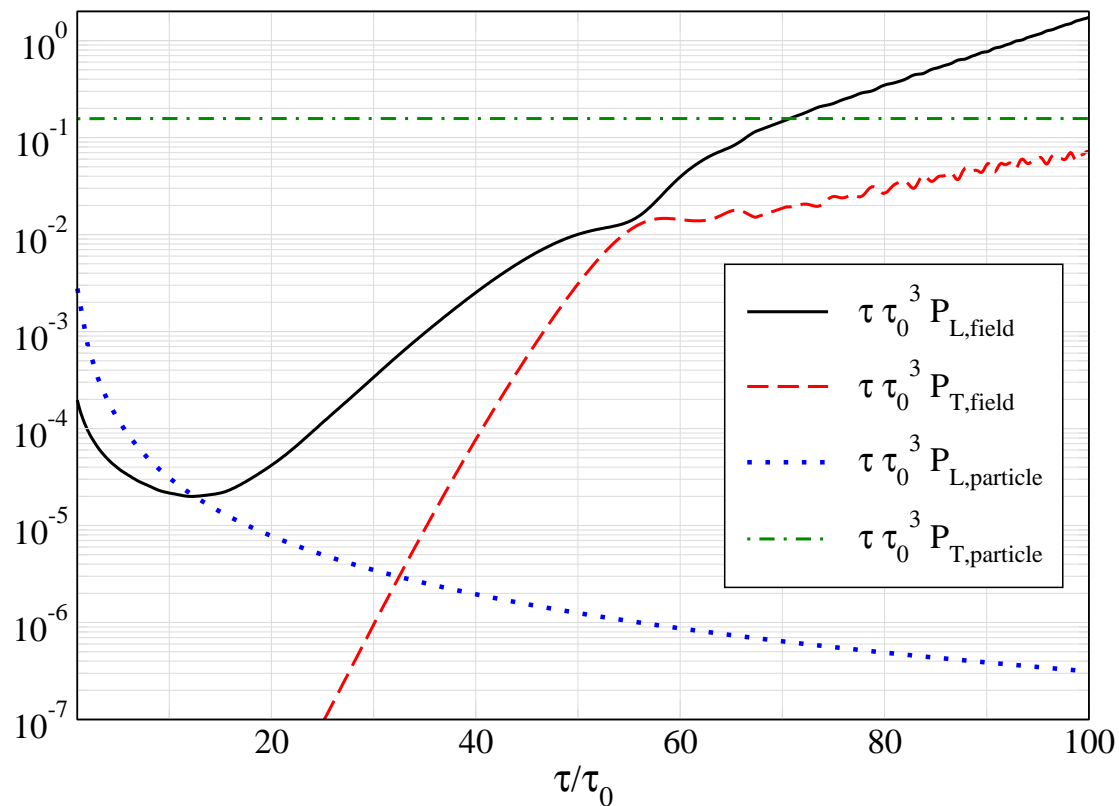
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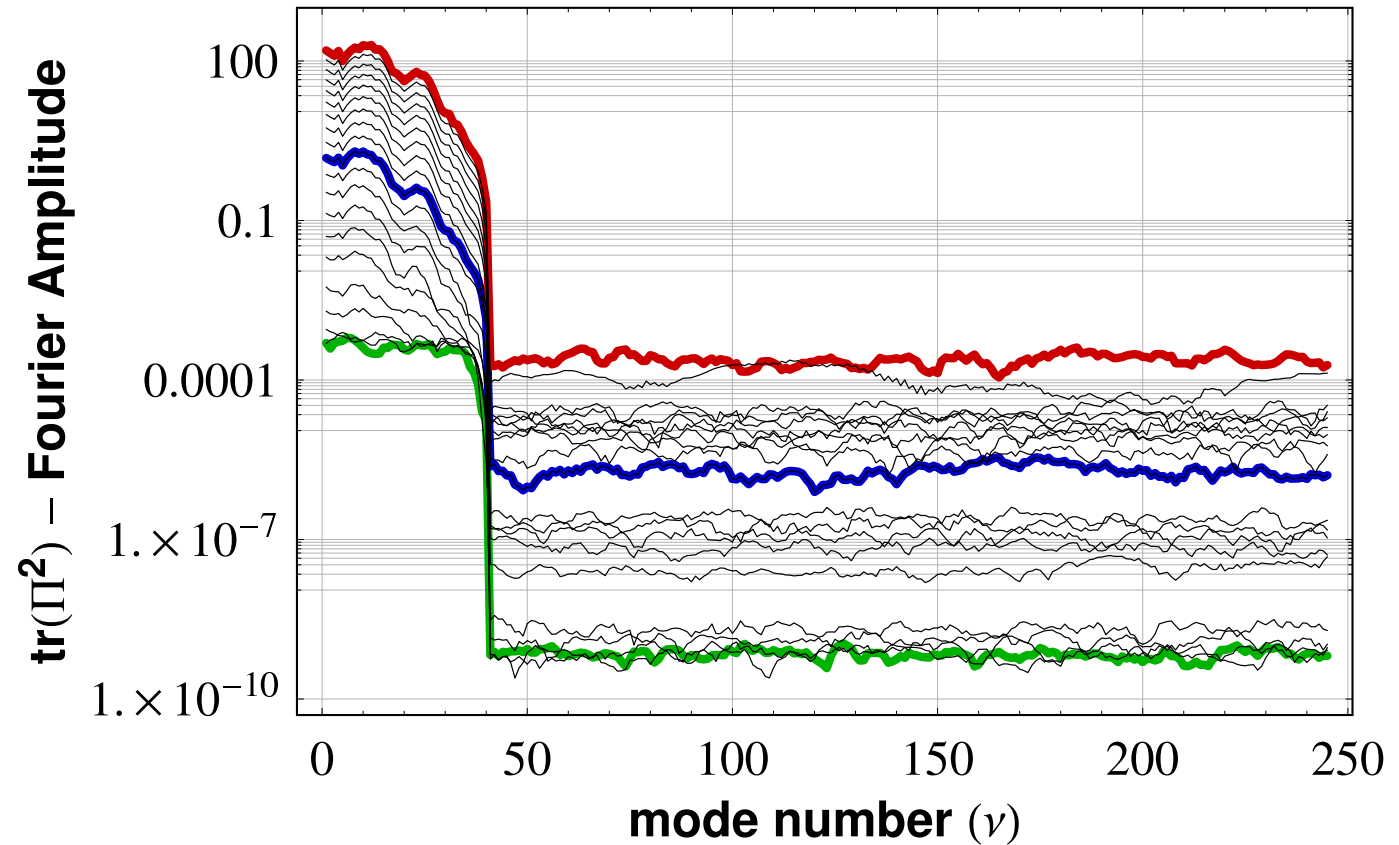


The comparison of the longitudinal and transverse pressures for the fields and particles resulting from a typical non-Abelian run initialized with FGM (CGC inspired) initial conditions.

# Expanding 1D+3V Abelian plasma

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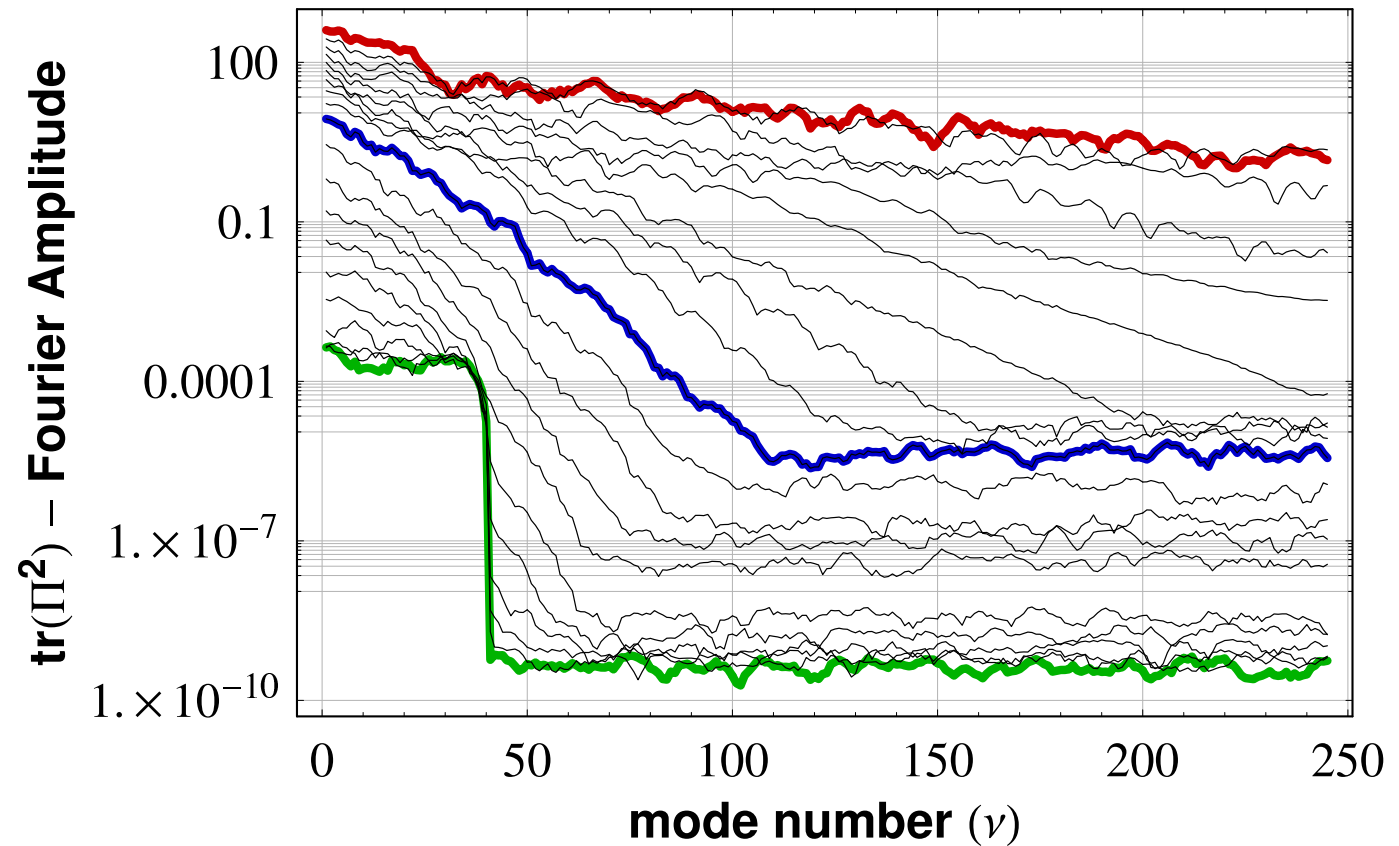


Fourier spectrum of the color-traced conjugate field momentum obtained from Abelian run with FGM initial conditions.

# Expanding 1D+3V non-Abelian plasma

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Fourier spectrum of the color-traced conjugate field momentum obtained from non-Abelian run with FGM initial conditions.

# Expanding 3D+5V plasma

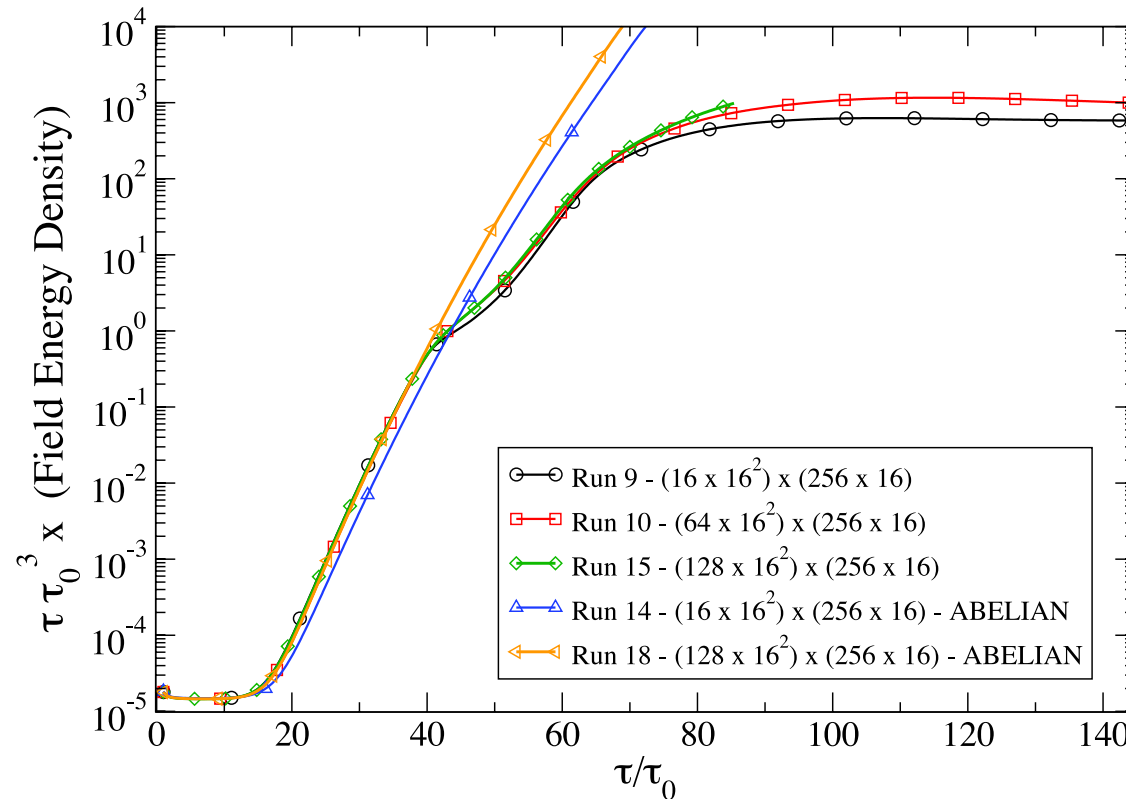
Hard Expanding  
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Expanding 3D+5V  
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Conclusions



Preliminary runs from the HEL 3d codes in Abelian and non Abelian setup with different lattice sizing's in the longitudinal  $\eta$  direction, but identical transverse size and  $\mathcal{W}$  auxiliary field numbers.

# Unstable transverse modes

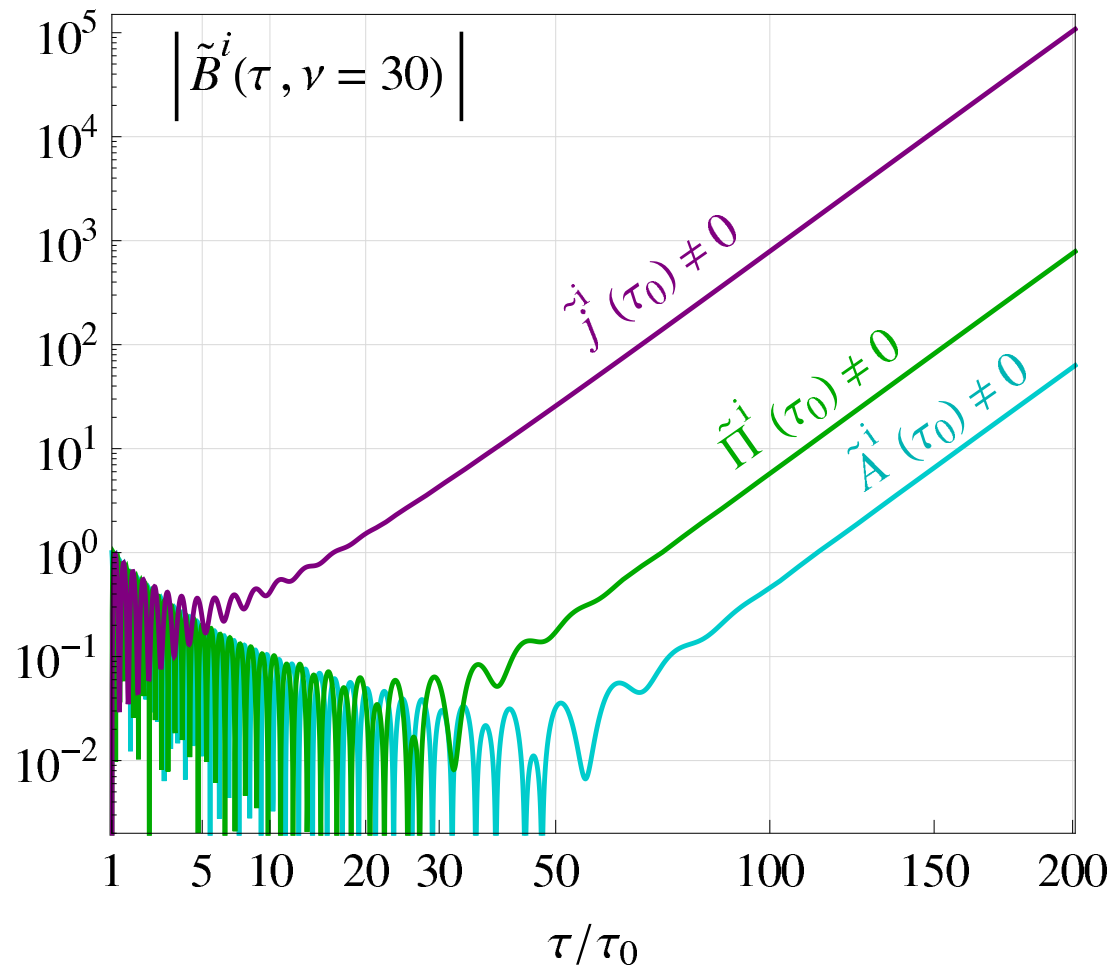
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Influence of different initial conditions for a specific mode with  $\nu = 30$

# Expanding 1D+3V non-Abelian plasma



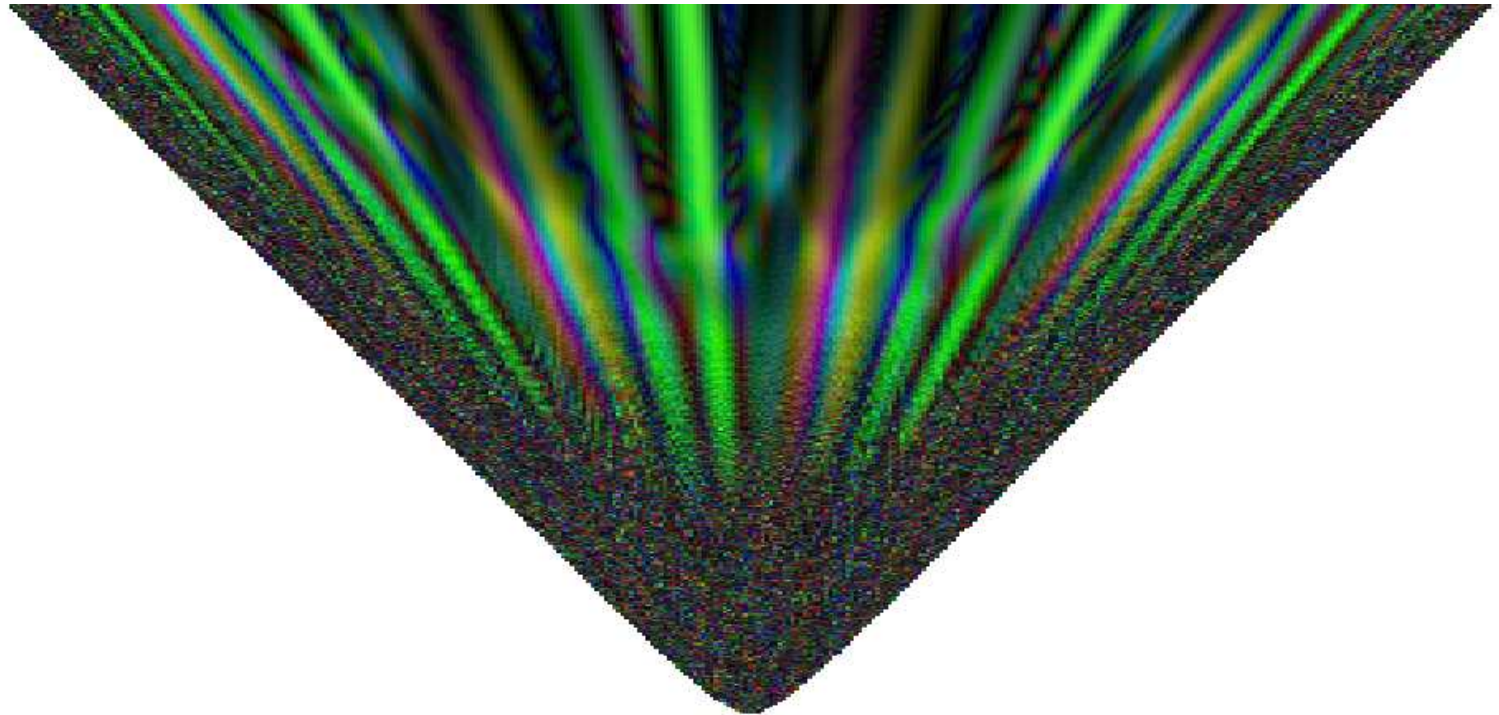
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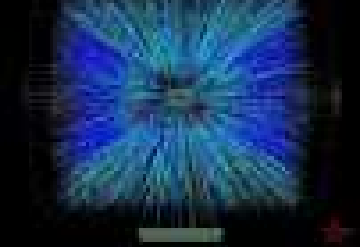
Expanding 3D+5V  
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Visualization of the space-time development of color correlations in a non-Abelian plasma instabilities in Bjorken expansion.





## Conclusions

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Conclusions

Non-abelian plasma instabilities accelerate isotropization and thermalization of the Quark Gluon Plasma.

Large amplitude turbulent field configurations can have an important effect on Quark Gluon Plasma transport such as momentum broadening, energy loss, plasma viscosity, ...

In the 1D+3V Hard Expanding Loop (HEL) 1D we found that the exponential (in  $\sqrt{\tau}$ ) growth in the Abelian (weak-field) phase is only mildly weakened when nonlinearities through non-Abelian self-interactions of the collective fields set in.

The previous 1D HEL code has been extended to full 3D+5V. Final results including different initial conditions are being computed.

# Backup - Equation of motions

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## Conjugate Momenta

$$\partial_\tau E_i = +\tau j^i + \frac{1}{\tau} D_\eta^2 A^i + \tau g^2 i [A^{j \neq i}, i [A^{j \neq i}, A^i]] \quad (6)$$

$$\partial_\tau E^\eta = -\tau j^\eta + \frac{ig}{\tau} [A^i, D_\eta A^i] \quad (7)$$

## Gauss law

$$j^\tau = +\frac{1}{\tau} D_\eta E^\eta - \frac{ig}{\tau} [A_i, E^i] \quad (8)$$

with

$$E^i \equiv \tau \partial_\tau A_i, \quad E^\eta \equiv \frac{1}{\tau} \partial_\tau A_\eta \quad (9)$$

# Backup - Expanding 1D+3V non-Abelian plasma

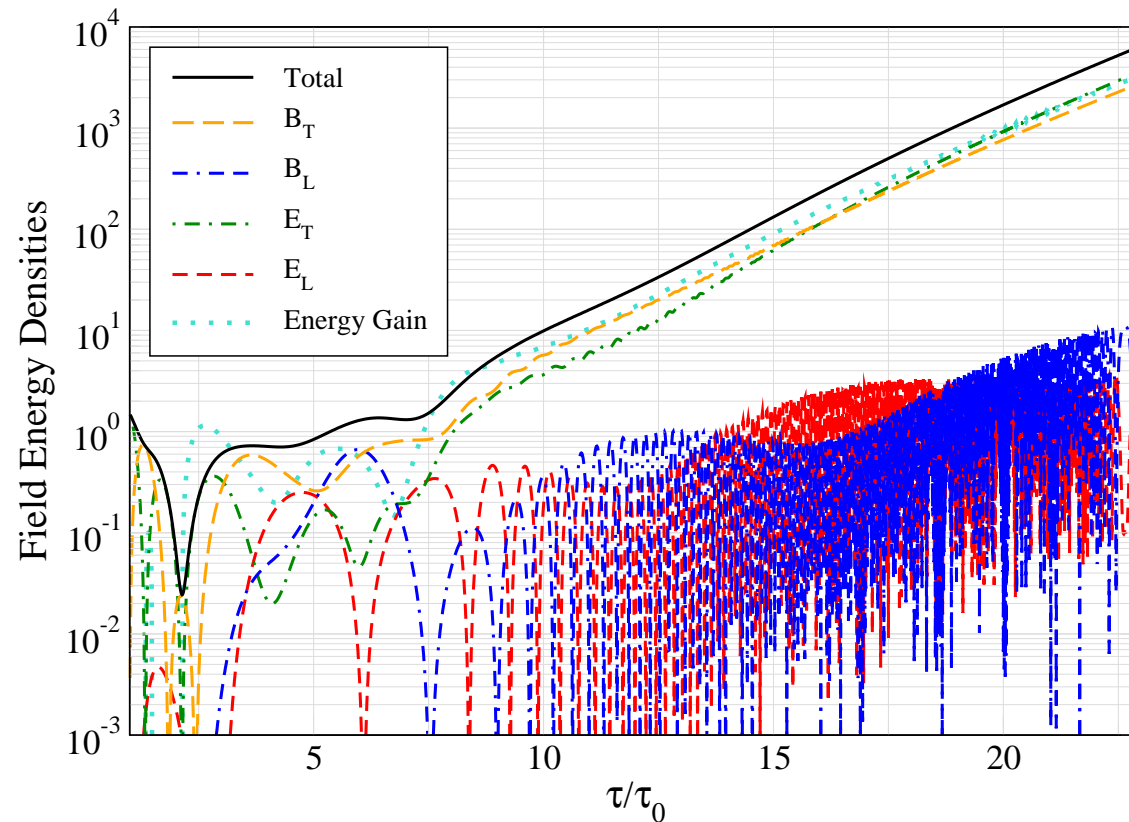
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The proper-time dependence of the chromo-field energy densities from a run with a single non-Abelian mode seeded with random noise.