

# Operations on network-based space layouts for modeling multiple space views of buildings

Georg Suter<sup>a,\*</sup>, Filip Petrushevski<sup>a</sup>, Miloš Šipetić<sup>a</sup>

<sup>a</sup>*Design Computing Group, Faculty of Architecture and Planning, Vienna University of Technology, Treitlstrasse 3, A-1040 Vienna, Austria, Phone: +43 1 58801 27220, Fax: +43 1 58801 27299*

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## Abstract

Space layouts are created by designers to model a building's spaces and related physical objects. Building services designers commonly reuse space layouts created by architectural designers to develop their designs. However, reuse tends to be limited due to differences in designers' space views. In order to address this issue of modeling multiple space views, we define a set of novel operations that can be used by designers to generate new space layouts from existing layouts. Fundamental operations include *select*, *aggregate*, and *decompose* operations. The *select* operation facilitates reuse of space layouts created in building information modeling (BIM) authoring systems. Signatures and processing of these operations are defined. We use an existing schema for network-based space layouts to represent space layouts. In a network-based space layout, specific spatial relations between layout elements are explicitly modeled as a directed, weighted graph or network. Processing of certain operations involves traversal of a spatial relation network with graph algorithms to determine layout modifications. Symmetric difference and *overlay* operations are defined as additional operations. They are composed of *union*, *intersect*, and *subtract* operations, which are fundamental operations. Fundamental and additional layout operations may be composed into expressions to model domain-specific space views. We have extended an existing layout modeling system with implementations of these layout operations. The system relies on geometric and solid modeling as well as graph libraries to represent layouts and process operations. The feasibility of modeling of multiple space views with layout operation expressions is shown with an example in which a security lighting layout of a floor of an existing office building is automatically generated from an architectural layout.

*Keywords:* Space modeling, Building information modeling, Spatial query languages

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\*Corresponding author

*Email addresses:* [georg.suter@tuwien.ac.at](mailto:georg.suter@tuwien.ac.at) (Georg Suter), [filip.petrushevski@tuwien.ac.at](mailto:filip.petrushevski@tuwien.ac.at) (Filip Petrushevski), [milos.sipetic@tuwien.ac.at](mailto:milos.sipetic@tuwien.ac.at) (Miloš Šipetić)

## 8 Nomenclature

<i>A</i>	"is adjacent to" relation
<i>le</i>	Layout element
<i>N</i>	"is near" relation
<i>O</i>	"overlaps" relation
<i>PB</i>	"partially bounds" relation
<i>PE</i>	"partially encloses" relation
<i>sbe</i>	Space boundary element
<i>se</i>	Space element
<i>se<sub>c_ws</sub></i>	Space element contained in a whole space
<i>se<sub>pe_ws</sub></i>	Space element partially enclosing a whole space
<i>sr</i>	Spatial relation element
<i>SRN</i>	Spatial relation network
<i>ss</i>	Subspace
<i>T</i>	"touches" relation
<i>ws</i>	Whole space

## 10 1. Introduction

11 Space layouts are created by designers to model a building's spaces and related physical objects, such as  
12 walls, windows, furnishing and technical equipment elements. Designers increasingly use building informa-  
13 tion modeling (BIM) authoring systems to develop space layouts [1]. Sharing of space layouts is facilitated by  
14 data exchange methods. The space schema in the Industry Foundation Classes (IFC), for example, defines  
15 rich data structures for spaces, space boundaries, and space enclosures [2].

16 It is common practice for building services designers to reuse space layouts created by architectural  
17 designers to develop their designs. However, reuse tends to be limited due to substantial differences in  
18 designers' space views. This issue of multiple, domain-specific views of objects is well-known in BIM [3, 4].  
19 For an architectural designer, a space typically includes space boundaries, windows, doors, as well as visually  
20 relevant furnishing and equipment elements. By contrast, in the space view adopted by an indoor climate  
21 control system designer, spaces are often zones that span multiple rooms with similar orientation, function,  
22 or thermal requirements. Space enclosure elements with high thermal flux, air inlets/outlets, or indoor air  
23 temperature sensors are of concern. A lighting designer in turn is usually interested in zones within rooms  
24 that are related to luminaires, shades, walls, windows, illuminance sensors, or occupancy sensors.

25 While BIM authoring systems and IFC provide general space data modeling and exchange capabilities,  
26 support for automated generation of space layouts that model multiple, domain-specific space views, as

27 outlined above, is limited. Building services designers may thus only partially reuse space layouts created  
28 by architectural designers. As a workaround, they need to manually recreate space layouts according to  
29 their space views. This existing workflow is inefficient, error-prone, and a significant barrier for seamless  
30 collaboration in multi-disciplinary design teams. According to [5], reduced errors, shorter cycle times of  
31 workflows, and reduced rework are viewed as highly important for improved quality and productivity of  
32 design firms in architecture, engineering, and construction.

33 In order to address the issue of modeling multiple space views, we describe a set of novel operations  
34 that can be used by designers to generate new space layouts from existing layouts. We build on and extend  
35 previous work, in which we have developed initial specifications for these operations [6, 7]. Layout operations  
36 may be composed into expressions to model domain-specific space views. For example, a layout operation  
37 expression may be defined to generate an indoor climate control layout from an architectural layout. We use  
38 an existing schema for network-based space to represent space layouts [8]. In a network-based space layout,  
39 spatial relations between layout elements are explicitly modeled as a directed, weighted graph or network.  
40 Processing of certain operations involves tracing of this spatial relation network with graph algorithms to  
41 determine layout modifications.

42 The remainder of this paper is organized as follows. A survey of related work is included in Section 2.  
43 Network-based space layout concepts are reviewed in Section 3. Fundamental layout operations are defined  
44 in Section 4. Additional layout operations that are compositions of fundamental operations are introduced  
45 in Section 5. The implementation of fundamental and additional layout operations in an existing layout  
46 modeling system is described in Section 6. Section 7 presents an example of a layout operation expression.  
47 Open issues and future work are discussed in Section 8.

## 48 2. Related work

49 Related work is reviewed, including IFC model view definitions, modeling and query languages, and  
50 ontology-based reasoning. We highlight aspects that deal with spatial modeling.

### 51 2.1. IFC model view definitions

52 An IFC model view definition is a subset of the original IFC schema that is relevant for specific appli-  
53 cations and life-cycle phases [9]. The IFC Coordination View defines a view for architectural, mechanical,  
54 and structural design coordination [10]. It includes *IfcSpace*, *IfcSpatialStructureElement*, and *IfcZone*  
55 classes. A building may be hierarchically divided into *IfcSpatialStructureElement* levels, such as sec-  
56 tions, floors and rooms. *IfcSpaces* and building elements may be attached to these levels. Alternatively,  
57 *IfcSpaces* may be aggregated into *IfcZones*. In contrast to *IfcSpatialStructureElements*, the latter do  
58 not have a shape. Their structure does not need to be hierarchical, that is, an *IfcSpace* may belong to one  
59 or more *IfcZones*.

Weise et al. [11] describe a schema for the definition of arbitrary IFC model views. A data subset is retrieved in two steps from an IFC model instance. In the first step, objects are selected dynamically from the original model by filtering based on criteria supplied by users at runtime. An example is the selection of objects on a particular floor. In the second step, attribute data or references to objects that are not needed are removed based on a pre-defined, static model view.

## 2.2. Modeling languages

GLIDE and EDM are early examples of modeling languages [12, 13]. Eastman and Siabiris [14] use composition and specialization in EDM to model views of constructed spaces and use spaces. Constraints verify if required relations between model entities are satisfied. An example is a constraint that checks for correct alignment of faces of constructed space and use space polyhedrons.

Zamanian et al. [15] describe a framework for modeling spatial abstractions of buildings. Decomposition, selection, and composition operations are applied to spatial configurations that are based on a spatial representation scheme. In this scheme, disjoint geometric elements (vertices, faces, solids) are generated by user-defined carrier elements (points, lines, planes). Domain-specific spatial views are defined by selection and composition operations and generated in three steps. First, Euclidean space is partitioned recursively until the desired level of granularity in a spatial configuration is reached. Second, atomic elements in the configuration are selected based on user-defined criteria. Third, selected atomic elements are composed to create new elements. The composition operation ensures that new elements are disjoint.

Stouffs et al. [16, 17] define the SORTS language for manipulating nested property structures. Although the language is not domain-specific, its development is motivated by the need for representational flexibility in building design. Property structures are composed with addition and sum operations. Furthermore, they may be combined using addition, subtract, and product operations. Primitive data constructs have specific, built-in behaviors under these operations. For example, the addition of two properties that model boundaries of solids corresponds to a merge (union) of these solids.

Grabska et al. [18, 19, 20] describe a visual design language that uses attributed, hierarchical hypergraphs to represent designs. Designers create hypergraphs representations of space layouts, for example, with operations that include hypergraph development and suppression. These operations add or remove levels of detail in a spatial hierarchy. Szuba [21] combines the hypergraph representation with a graph rewriting system to reason about spatial requirements. Activity requirements that are modeled as paths are matched against access graphs that are extracted from a space layout created in a BIM authoring system. This matching is non-trivial as it considers indirect access relations between rooms via circulation spaces.

The BERA language developed by Lee [22] provides high-level constructs to check building models against pedestrian circulation or space requirements. Users define simplified but extensible views of a building model that is populated with IFC objects. Space groups or paths may be included in a view. Paths are groups

94 of connected spaces. Pedestrian circulation networks are generated from door, vertical access, and concave  
95 points that lie on buffered space boundary polygons [23]. Edges in a circulation network relate nodes with  
96 line-of-sight.

### 97 2.3. Query languages

98 Several query languages have been developed to retrieve data from building models. Some are defined as  
99 extensions of SQL or XML, such as PMQL, GTCIS2SQL, and PMQ [24, 25, 26]. PMQL supports recursive  
100 object selection using a *cascades* operator. BimQL simplifies access to objects, attributes, and relations in  
101 the IFC schema by hiding its nested structure from users [27]. An IFC object graph is recursively traced,  
102 e.g. to derive the name of a space.

103 A spatial query language developed by Borrmann et al. [28, 29, 30] supports queries on implicit topo-  
104 logical, directional, and metric spatial relations between objects. The language is designed as an extension  
105 of SQL. Topological spatial query operators derive *equal*, *contain*, *within*, *touch*, and *overlap* relations.  
106 Their processing involves evaluation of the 9-intersection model, which uses point-set topology as geometry  
107 representation [31].

108 Nepal et al. [32] describe query operations to derive location, alignment, spacing, and variation of objects  
109 such as columns, openings, or penetrations. These relations are required for construction planning but are  
110 typically not included in building models, nor are they easily derived from other relations. Object features  
111 such as faces, center points, and center lines are relevant for queries. Query operations are based on object  
112 geometry data as well as construction planning knowledge.

### 113 2.4. Ontology-based reasoning

114 Ontology-based reasoning has the potential to simplify access to building models for users and applica-  
115 tions [33] and provide feedback to designers. Bhatt et al. [34] combine description logic with spatial logics  
116 to develop an ontology for the architectural design domain. Topological spatial relations between objects  
117 are determined by region connection calculus, which is a qualitative spatial reasoning method ([35]). Design  
118 requirements are modeled as spatial constraints that are based on this reasoning method. An example for  
119 a constraint is a range space of an occupancy sensor that must contain the functional space of a door.

120 Implicit relations in an ontology may be derived based on user-defined inference rules. In rule languages  
121 such as SWRL or SPARQL, rules are defined as subgraph patterns which a reasoner matches against an  
122 object graph. Pauwels et al. [36] define rules to derive a view of space boundaries and their sound reduction  
123 properties from a building model and construction element type data. The resulting partial model is pro-  
124 cessed with a second rule set that encodes a sound control standard. A building model can thus be checked  
125 for compliance with this standard.

## 126 2.5. Discussion

127 The following observations are made based on the above review. First, while IFC model view definitions  
128 provide a common reference for modeling multiple space views, operations to generate models are limited to  
129 selections [11]. Second, decomposition, selection, and composition operations described by Zamanian and  
130 Fenves [15] as well as space group and path operations in the BERA language [22] are high-level spatial  
131 operations that are conceptually similar to the operations described in this paper. By contrast, operations  
132 in other modeling and query languages tend to be low-level but are more generally applicable. Third, in  
133 case of the BERA language, operations use a space layout representation that is specific to circulation and  
134 space planning domains. Our operations are based on a layout representation that can be used in multiple  
135 domains (Section 3.2). Fourth, recursive object graph traversal, which is required to process operations  
136 such as the space path operation, is difficult to implement in the reviewed query languages and ontology-  
137 based reasoning methods. In summary, our operations provide novel, high-level space layout modeling  
138 functionality. They may be composed to automatically generate richly structured space layouts that model  
139 space views of multiple domains.

## 140 3. Review of network-based space layout concepts

### 141 3.1. Background

142 Space layout representations developed by Steadman [37] and Grason [38] for the space planning domain  
143 are among the first representations that model spatial relations between spaces, walls, and openings as  
144 graphs or networks. Space adjacency and access graphs are relevant for the development of space planning  
145 algorithms [39]. Flow networks are used to simulate air circulation behavior in buildings [40]. Several  
146 recent efforts explore layout representations whose spatial relation graphs are derived from IFC space data.  
147 Application domains include code compliance checking of pedestrian circulation systems, indoor navigation,  
148 construction planning, and case-based design [23, 41, 42, 43, 44].

149 Network-based space layouts extend the network approach to space layout representation to facilitate  
150 multi-domain space modeling. Concepts are reviewed in the following. For a detailed description, the reader  
151 is referred to [8]. The schema for network-based space layouts incorporates aspects of existing space schemas  
152 [45, 14, 46, 2]. In contrast to the IFC space schema, whole spaces and subspaces are modeled as separate  
153 classes in the layout schema. Flexible subspace modeling is supported to meet the needs of multiple domains.  
154 Furthermore, certain spatial relations in the layout schema are not modeled explicitly in IFC.

### 155 3.2. Layout schema

156 The principal classes in the schema for network-based space layouts are shown in Fig. 1. Layout elements  
157 (*le*'s) include whole spaces (*ws*'s), subspaces (*ss*'s), space boundary elements (*sbe*'s), and space elements



177 six base relations in an SRN that are derived from layout element geometries. They include  $PB_{SBE,WS}$ ,  
 178  $PB_{SBE,SS}$ ,  $T_{SBE}$ ,  $A_{SS}$ ,  $N_{SE,SBE}$ , and  $N_{SS,SE}$  relations. Relations  $A_{WS}$ ,  $N_{SE}$ ,  $PE_{SE,WS}$ , and  $PE_{SE,SS}$  are  
 179 derived from these base relations. For example, the  $A_{WS}$  relation is derived from base relations  $PB_{SBE,WS}$   
 180 and  $T_{SBE}$ , which are, respectively, the "partially bounds" relation between *sbe*'s and whole spaces, and the  
 181 "touches" relation between *sbe*'s.

### 182 3.3. Example layout

183 The structure of network-based space layouts and analysis of their SRNs is illustrated with an example  
 184 layout (Figs. 2 – 5). Each figure features selected spatial relations between *le*'s that form a subnetwork of  
 185 the example layout's SRN. Such a subnetwork is referred to as a filtered SRN. Throughout this paper, figures  
 186 show filtered rather than entire SRNs in order to simplify visualizations. Similarly, whole space volumes are  
 187 offset.

188 In Fig. 2, the filtered SRN includes base relations  $PB_{SBE,WS}$ ,  $T_{SBE}$  and relation  $A_{WS}$  that is derived  
 189 from these relations. The weight of each whole space node corresponds to the distance from that node to  
 190 the nearest *sbe* node with a degree (that is, number of incident edges) of 1. Such an *sbe* is part of the (not  
 191 explicitly modeled) building perimeter. Distances correspond to the length (that is, the number of edges) of  
 192 the shortest path between node pairs in the filtered SRN. Two whole spaces are perimeter spaces because  
 193 they have a weight of 1. Conversely, the whole space with weight 2 is a non-perimeter space. The distinction  
 194 of perimeter and non-perimeter spaces is relevant for thermal design.

195 In Fig. 3, the filtered SRN includes base relations  $A_{SS}$  ("is adjacent to") and  $N_{SS,SE}$  ("is near") between  
 196 subspaces and *se*'s. Subspace node weights correspond to the distance to the nearest door  $se_{pe\_ws}$  node with  
 197 degree 1. Such a door is an exit door. The two most distant subspaces have weights of 4. This information  
 198 is useful for pedestrian circulation design. Subspace volumes correspond to geodesic Voronoi cells [51] that  
 199 are derived from whole space boundaries (used as obstacles) and subspace positions (used as sites). Other  
 200 types of subspace volume supported by the schema include sphere and cone volumes.

201 In Fig. 4, the filtered SRN includes base relations  $N_{SE,SBE}$  ("is near"),  $PB_{SBE,SS}$  ("partially bounds"),  
 202 and derived relation  $PE_{SE,SS}$  ("partially encloses") between *se*'s, *sbe*'s, and subspaces. Subspace node  
 203 weights correspond to the distance to the nearest window  $se_{pe\_ws}$  node. Only paths that do not include  
 204 doors are considered to compute distances. Subspaces with weight 1 are near windows, whereas those with  
 205 greater weights are more remote. This information is useful for lighting design. One subspace has an  
 206 undefined weight as it is partially enclosed only by a door and there is no path to windows that does not  
 207 include doors in the filtered SRN.

208 In Fig. 5, the filtered SRN includes derived relations  $PE_{SE,WS}$  ("partially encloses") and  $N_{SE}$  ("is  
 209 near") between *se*'s and whole spaces. Whole space node weights correspond to the distance to the nearest  
 210 door node with degree 2. Such a door is an exit door. Whole spaces with weight 1 have an exit door. This

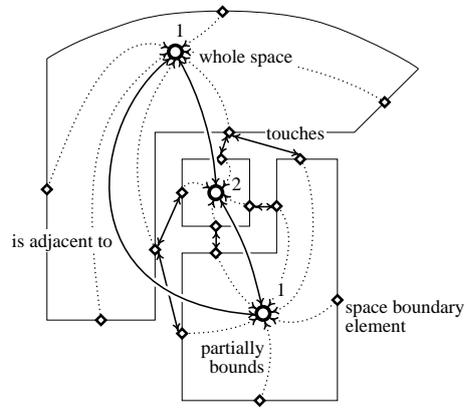


Figure 2: Example layout. The filtered SRN includes base relations  $PB_{SBE,WS}$  ("partially bounds"),  $T_{SBE}$  ("touches"), and derived relation  $A_{WS}$  ("is adjacent to") between whole spaces and *sbe*'s. Weights correspond to distances from whole space nodes to nearest *sbe* nodes with degree 1.

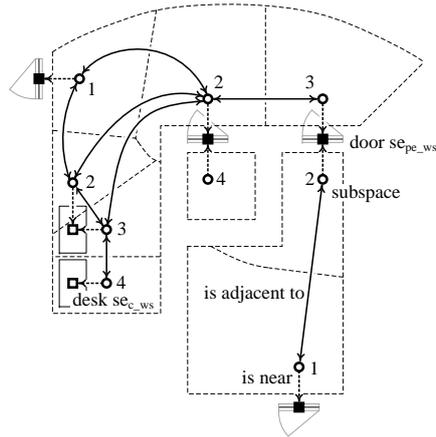


Figure 3: Example layout. The filtered SRN includes base relations  $A_{SS}$  ("is adjacent to") and  $N_{SS,SE}$  ("is near") between subspaces and *se*'s. Weights correspond to distances from subspace nodes to nearest door nodes with degree 1.

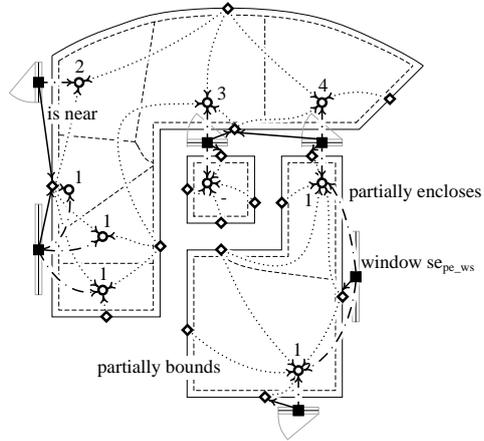


Figure 4: Example layout. The filtered SRN includes base relations  $N_{SE,SBE}$  ("is near"),  $PB_{SBE,SS}$  ("partially bounds"), and derived relation  $PE_{SE,SS}$  ("partially encloses") between  $se$ 's,  $sbe$ 's, and subspaces. Weights correspond to distances from subspace nodes to nearest window nodes. Distances are derived from paths that do not include doors.

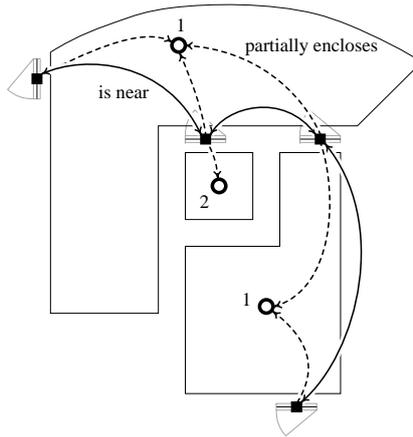


Figure 5: Example layout. The filtered SRN includes derived relations  $PE_{SE,WS}$  ("partially encloses") and  $N_{SE}$  ("is near") between  $se$ 's and whole spaces. Weights correspond to distances from whole space nodes to nearest door nodes with degree 2.

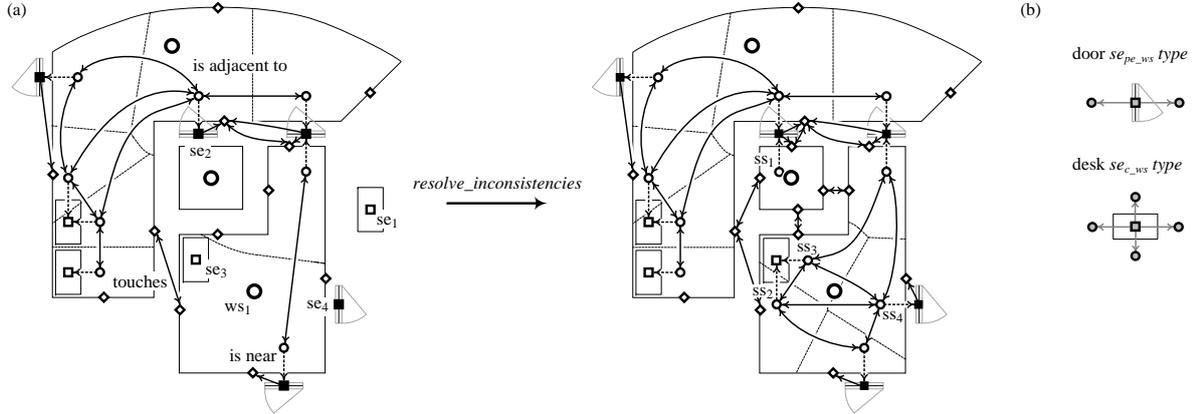


Figure 6: Inconsistency resolution example. (a) Spatial inconsistencies in the argument layout (left hand side) are identified and resolved by the *resolve\_inconsistencies* operation in the result layout (right hand side). (b) Door and desk *se* types used by the operation in this example.

211 information is useful for evacuation design.

212 Similarly, metrics for the analysis of space connectivity networks [52, 53] may be applied to SRNs. For  
 213 example, the filtered SRN in Fig.3 has two cycles, the average degree of subspace nodes is 2.8, and the  
 214 average distance (or depth) of subspaces with respect to exit doors is 2.4.

### 215 3.4. Resolution of spatial inconsistencies

216 The concept of spatial consistency of layouts is relevant for converting space layouts created in BIM  
 217 authoring systems to network-based space layouts and for layout operations presented in Sections 4 and  
 218 5. In general, spatial consistency refers to the correctness and accuracy of spatial data [54]. A spatially  
 219 consistent layout meets certain constraints on spatial relations between *le*'s [8]. For example, no pair of whole  
 220 spaces in a layout may overlap, or each subspace must be contained in a whole space. An inconsistency  
 221 resolution operation that evaluates spatial constraints to identify and resolve spatial inconsistencies in layouts  
 222 is described in [8]. Inconsistencies are resolved interactively by users or automatically based on pre-defined  
 223 rules.

224 The inconsistency resolution operation is illustrated with an example in Fig.6. The argument layout  
 225 on the left hand side of Fig.6 (a) features several spatial inconsistencies that are identified and resolved  
 226 automatically. For example, space element  $se_1$ , which is a desk  $se_{c\_ws}$  (whole space contained *se*), is not  
 227 contained in a whole space. It is removed and not included in the consistent result layout on the right hand  
 228 side of Fig.6 (a). Most inconsistencies are resolved by removal of *le*'s. On the other hand, four subspaces  
 229  $ss_1 \dots ss_4$  are inserted to ensure that space elements  $se_2, se_3,$  and  $se_4$  have all subspaces that are feasible in  
 230 their contexts. Missing subspaces are instantiated based on user-defined *se* types (Fig.6 (b)). In case of desk  
 231  $se_3$ , only  $ss_2$  and  $ss_3$  are feasible because the desk is located in the corner of its whole space. Since these  
 232 are new subspaces, all subspace volumes in whole space  $ws_1$  are inconsistent and must be regenerated. The

233 inconsistency resolution operation also ensures the consistency of *sr*'s in an SRN. For example, an existing  
234  $A_{SS}$  element in  $ws_1$  is removed and seven new ones are inserted in order to correctly reflect adjacencies  
235 between subspaces. The consistency of *sr*'s that are not shown in the figure is maintained in a similar  
236 manner.

237 Space layouts created in BIM authoring systems typically do not include *sbe*'s, *sr*'s, and subspaces.  
238 These spatial inconsistencies may be identified and resolved with the *resolve\_inconsistencies* operation. As  
239 will be shown in Section 7, it is thus feasible to model multiple space views by reusing existing, spatially  
240 inconsistent space layouts.

## 241 4. Fundamental layout operations

### 242 4.1. Overview

243 Fundamental layout operations are defined that support modeling of multiple space views. They are part  
244 of an emerging space modeling language. A formal definition of the language's syntax, however, is not an  
245 issue in this paper. Unary operations (Section 4.2) accept an argument layout and generate a result layout.  
246 They include *select*, *aggregate*, *decompose*, and *update\_WEIGHT* operations. Binary operations (Section  
247 4.3) accept two argument layouts and generate a result layout. They include *union*, *intersect*, and *subtract*  
248 operations. Variants of operations such as the *update* operation are desirable but not described here for  
249 space reasons.

250 With the exception of the *update\_WEIGHT* operation, which does not modify a layout's structure, the  
251 inconsistency resolution operation (Section 3.4) is invoked in the processing of each operation in order  
252 to identify and resolve spatial inconsistencies that are due to prior modifications of a layout. That is,  
253 result layouts returned by fundamental operations are spatially consistent. This execution behavior has two  
254 benefits. First, users are relieved from manually maintaining the spatial consistency of layouts, which is  
255 a time-consuming and error-prone task. Second, it is feasible to safely compose (or chain) operations into  
256 expressions as there are no spatial inconsistencies in layouts that could cause operations to fail or generate  
257 misleading results.

### 258 4.2. Unary operations

#### 259 4.2.1. Select

The *select* operation selects *le*'s from an argument layout  $E$  based on a filter on *le*'s in  $E$ . For example, a  
layout consisting of whole spaces that are offices may be selected with the *select* operation from an argument  
layout that also includes service rooms and circulation spaces. The operation has the signature

$$select_{F_{LE}}(E)$$

260 where

- 261 —  $F_{LE} = (p_1(LE), p_2(LE), \dots, p_n(LE))$  is a filter that consists of a list of predicates on the set  $LE$  of all
- 262  $le$ 's in  $E$  —  $le$ 's that pass  $F_{LE}$  are selected to be included in the result layout together with certain spatially
- 263 related, non-passing  $le$ 's (as defined below), and
- 264 —  $E$  is a layout (a layout operation expression).

265 If there is a predicate on whole spaces in  $F_{LE}$ , then whole spaces are selected explicitly based on the

266 values of predicates in  $F_{LE}$ . If there is no such predicate, then whole spaces are selected implicitly if they

267 are spatially related to subspaces,  $se$ 's, or  $sbe$ 's that are selected explicitly. Similarly, if an  $se$  is selected

268 explicitly but not its nearby subspaces, then these subspaces are selected implicitly (and vice versa).

269 More specifically, operation processing involves these steps:

- 270 1. Filter  $F_{LE}$  is evaluated to explicitly select  $le$ 's from the argument layout  $E$  to be included in the result
- 271 layout.
- 272 2. If there is no predicate on whole spaces in  $F_{LE}$ , then whole spaces that are spatially related to explicitly
- 273 selected  $le$ 's are selected implicitly. A whole space  $ws$  is related to a layout element  $le$  if  $le$  is a
- 274 (a) subspace that is contained in  $ws$ ,
- 275 (b) whole space contained  $se$  ( $se_{c-ws}$ ) that is contained in  $ws$ ,
- 276 (c) partially whole space enclosing  $se$  ( $se_{pe-ws}$ ) that partially encloses  $ws$ , or a
- 277 (d) space boundary element that partially bounds  $ws$ .
- 278 3. If there are explicitly selected  $se$ 's that are near non-selected subspaces, then these subspaces are
- 279 selected implicitly (and vice versa).
- 280 4. The intermediate layout generated by steps 1.–3. is passed to the *resolve\_inconsistencies* operation
- 281 to generate the spatially consistent result layout (Section 3.4).

282 A layout that is passed to the *select* operation does not need to be spatially consistent. The

283 *resolve\_inconsistencies* operation, which is invoked in step 4, ensures that the result layout is spatially

284 consistent. It is thus feasible to retrieve  $le$ 's from space layouts created in BIM authoring systems, which

285 are typically spatially inconsistent, as mentioned in Section 3.4. This facilitates reuse and subsequent

286 modification of existing space layouts with other layout operations.

287 If whole spaces are selected neither explicitly nor implicitly, then an empty layout is returned by *select*.

288 An empty layout is considered as a valid, spatially consistent layout, however, it does not include any  $le$ 's

289 and  $sr$ 's [8].

290 Examples of the *select* operation are shown in Fig. 7. In the first example (Fig. 7, top right), all whole

291 spaces are selected explicitly from the argument layout  $A$  (Fig. 7, top left). A relational algebra style notation

292 is used to make filter definitions concise and easy to read [55]. The wildcard ( $*$ ) predicate is read as 'all'. The

293 *resolve\_inconsistencies* operation inserts missing  $sbe$ 's and  $sr$ 's because the intermediate layout includes

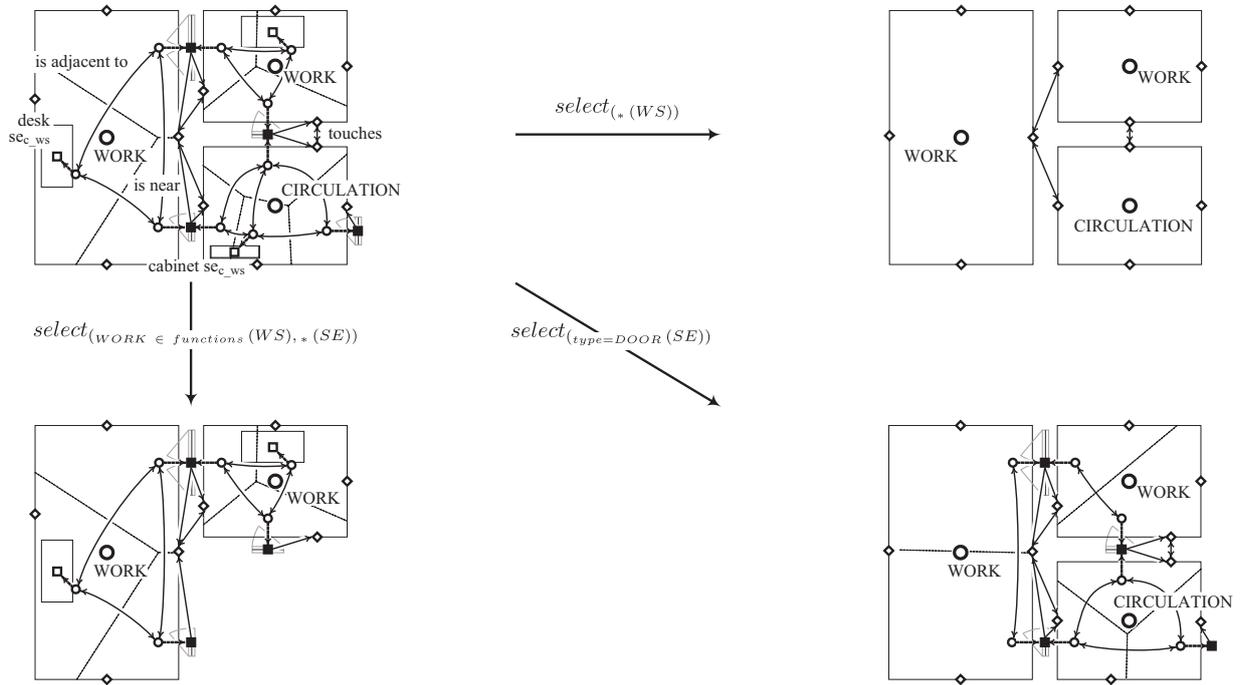


Figure 7: Examples of the *select* operation.

294 whole spaces only (step 4). In the second example (Fig. 7, down left), whole spaces are selected explicitly  
 295 from  $A$  by a predicate on their *functions* attribute. That is, whole spaces that are *WORK* spaces are  
 296 selected. All *se*'s are selected by the second predicate. The cabinet  $se_{c_ws}$  in the *CIRCULATION* whole  
 297 space is selected explicitly (step 1) but not contained in a selected whole space. It is therefore removed when  
 298 inconsistencies in the intermediate layout are resolved. Subspaces that are near explicitly selected door and  
 299 desk *se*'s are selected implicitly (step 3). In the third example (Fig. 7, down right), only doors are selected  
 300 explicitly from  $A$ . All whole spaces are selected implicitly because they are partially enclosed by doors  
 301 (step 2(c)). On the other hand, only those subspaces that are near doors are selected implicitly (step 3).  
 302 Consequently, subspace volumes are inconsistent and need to be regenerated by the *resolve\_inconsistencies*  
 303 operation (step 4).

#### 304 4.2.2. Aggregate

The *aggregate* operation merges sets of whole spaces in an argument layout  $E$  into larger whole spaces. Whole spaces in a merge set belong to the same group, as specified by whole space attributes, and are connected in a filtered SRN of  $E$ , as specified by filters on *le*'s and *sr*'s. Spatially consistent *se*'s, subspaces, and *sbe*'s are also included in the result layout. For example, the *aggregate* operation may be used to derive a layout with whole spaces that result from merging whole spaces with the same function in an argument

layout. The operation has the signature

$$\text{aggregate}_{G_{WS}, F_{LE}, F_{SR}}(E)$$

305 where

306 —  $G_{WS} = (g_{ws,1}, g_{ws,2}, \dots, g_{ws,k})$  is a list of whole space attributes that are used to group whole spaces in  
 307  $E$ ,

308 —  $F_{LE} = (p_1(LE), p_2(LE), \dots, p_m(LE))$  is a filter on  $le$ 's in  $E$  —  $le$ 's that pass  $F_{LE}$  are selected as nodes  
 309 in the filtered SRN of  $E$ ,

310 —  $F_{SR} = (p_1(SR), p_2(SR), \dots, p_n(SR))$  is a filter on  $sr$ 's in  $E$  —  $sr$ 's that pass  $F_{SR}$  are selected as edges in  
 311 the filtered SRN of  $E$ , and

312 —  $E$  is a layout.

313 Whole space grouping is inspired by grouping in aggregation operations in relational algebra [55].  $Le$ 's  
 314 and  $sr$ 's that pass filters  $F_{LE}$  and  $F_{SR}$  define the filtered SRN that is used to determine whole space  
 315 connectivity.

316 Operation processing involves these steps:

- 317 1. The set of whole spaces  $WS$  in the argument layout  $E$  is partitioned into merge sets  $\{WS_1 \subset$   
 318  $WS, WS_2 \subset WS, \dots, WS_n \subset WS\}$  such that all whole spaces in a merge set  $WS_i$  belong to the  
 319 same whole space group and are connected. Moreover, no pair of whole spaces in different merge sets  
 320 belong to the same group and are connected. Whole space groups are determined based on whole  
 321 space attributes, as specified by  $G_{WS}$ . Whole spaces in a group have the same values for all  $G_{WS}$   
 322 attributes. Whole space connectivity is determined based on the filtered SRN of  $E$ , as specified by  
 323  $F_{LE}$  and  $F_{SR}$ . Directions of  $sr$ 's are ignored to determine whole space connectivity.
- 324 2. Whole spaces in a merge set  $WS_i$  with more than one whole space are replaced by a new whole space  
 325  $ws$ . The volume of  $ws$  corresponds to the solid union [48] of whole space volumes in  $WS_i$ .
- 326 3. The intermediate layout consisting of new and unmodified whole spaces, subspaces,  $sbe$ 's, and  $se$ 's is  
 327 passed to the *resolve\_inconsistencies* operation to generate the spatially consistent result layout.

328 Additional processing is required to derive values for non-spatial attributes of new whole spaces. An  
 329 example is the *functions* attribute. This aspect, which is also relevant for other operations, is not addressed  
 330 in this paper.

331 Examples of the *aggregate* operation are shown in Fig. 8. In the first example (Fig. 8, top right), grouping  
 332 of whole spaces in the argument layout  $A$  (Fig. 8, top left) is done based on the whole space functions  
 333 attribute. The filtered SRN of  $A$  includes whole spaces and the  $A_{WS}$  relation. Two whole spaces that are  
 334 *WORK* spaces are adjacent and thus merged. In the second example (Fig. 8, down left), aggregation is done

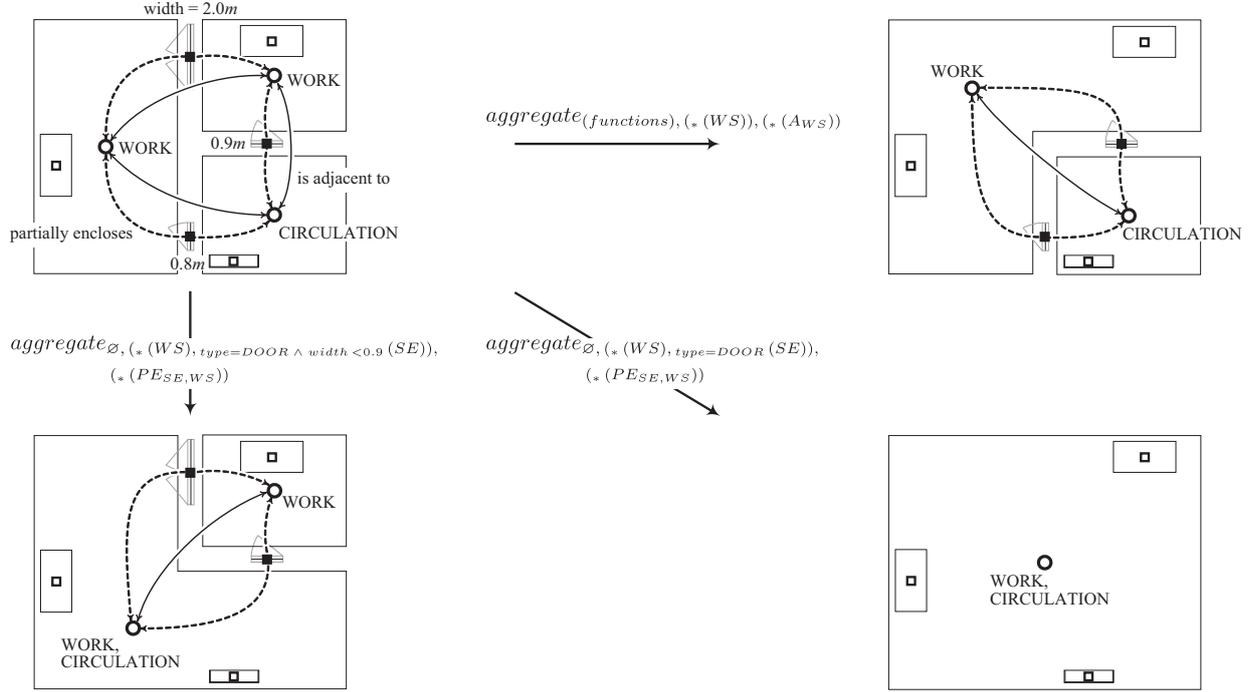


Figure 8: Examples of the *aggregate* operation.

335 based on whole space connectivity only as no whole space grouping attributes are specified ( $G_{WS} = \emptyset$ ).  
 336 The filtered SRN includes whole spaces, door *se*'s that are less than 0.9 m wide, and the  $PE_{SE, WS}$  relation.  
 337 A *WORK* and a *CIRCULATION* whole space are connected via a door that is 0.8 m wide and therefore  
 338 merged into a new whole space in the result layout. In the third example (Fig. 8, down right), filters are  
 339 similar to those in the previous example, except that all doors are included in the filtered SRN. Since all  
 340 whole spaces are connected by doors, they are merged into a single whole space.

#### 341 4.2.3. Decompose

The *decompose* operation breaks down whole spaces in an argument layout  $E$  into smaller whole spaces based on a filter on subspaces in  $E$ . The volumes of the smaller whole spaces are derived from the volumes of decomposed whole spaces and the positions of subspaces selected by the filter. Decomposed whole spaces are replaced by smaller whole spaces. Whole spaces that are not decomposed as well as spatially consistent *se*'s, subspaces, and *sbe*'s are also included in the result layout. For example, the *decompose* operation may be used to derive a layout from an argument layout where subspaces that are near luminaires are used to decompose whole spaces in which they are contained. The operation has the signature

$$decompose_{F_{LE}}(E)$$

342 where

343 —  $F_{LE} = (p_1(LE), p_2(LE), \dots, p_n(LE))$  is a filter on attributes of  $le$ 's in  $E$  – subspaces that pass  $F_{LE}$  are  
344 selected to decompose whole spaces together with certain non-passing subspaces that are spatially related  
345 to passing  $le$ 's (as defined below), and

346 —  $E$  is a layout.

347 A subspace is selected explicitly if it passes  $F_{LE}$ , and implicitly if it is spatially related to an  $le$  that passes  
348  $F_{LE}$ . Whole spaces that contain more than one explicitly or implicitly selected subspace are decomposed.  
349 The volume of each decomposed whole space and the positions of selected subspaces that are contained  
350 in it are used to derive geodesic Voronoi cells ([51], Section 3.3). These cells become the volumes of new  
351 whole spaces that replace the decomposed whole space. Any subspace in an argument layout, regardless of  
352 its volume type, may be selected to decompose whole spaces. For example, subspaces with sphere or cone  
353 volumes may be used as well as subspaces with geodesic Voronoi volumes.

354 Operation processing involves these steps:

- 355 1. Filter  $F_{LE}$  is evaluated to explicitly select  $le$ 's from the argument layout  $E$ . A subspace is selected  
356 explicitly to decompose whole spaces if it passes  $F_{LE}$ .
- 357 2. A subspace is selected implicitly if it does not pass  $F_{LE}$  but is spatially related to an explicitly selected  
358 layout element that is not a subspace. A subspace  $ss$  is related to a layout element  $le$  if  $le$  is a
  - 359 (a) whole space that contains  $ss$ ,
  - 360 (b) space boundary element that partially bounds  $ss$ , or a
  - 361 (c) space element that is near or partially encloses  $ss$ .
- 362 3. Each whole space which contains at least two selected subspaces is decomposed. Positions of these  
363 subspaces and the volume of the decomposed whole space are used as, respectively, sites and obstruc-  
364 tions to generate geodesic Voronoi cells. Whole spaces that contain no or only one subspace are not  
365 decomposed.
- 366 4. A new whole space is created for each selected subspace that generated a geodesic Voronoi cell in step  
367 4. The cell becomes the volume of the new whole space.
- 368 5. Decomposed whole spaces are removed.
- 369 6. The intermediate layout consisting of new and unmodified whole spaces, subspaces,  $sbe$ 's, and  $se$ 's is  
370 passed to the *resolve\_inconsistencies* operation to generate the spatially consistent result layout.

371 Examples of the *decompose* operation are shown in Fig. 9. In the first example (Fig. 9, top right), whole  
372 spaces in the argument layout  $A$  (Fig. 9, top left) are decomposed based on subspaces  $ss_1 \dots ss_8$ . These  
373 subspaces are selected explicitly based on their weight, which is 2. Each whole space in the result layout  
374 contains a luminaire because  $ss_1 \dots ss_8$  are near luminaires. In the second example (Fig. 9, down left), only  
375 door  $se$ 's are selected explicitly. Subspaces  $ss_9 \dots ss_{15}$  are selected implicitly to decompose whole spaces

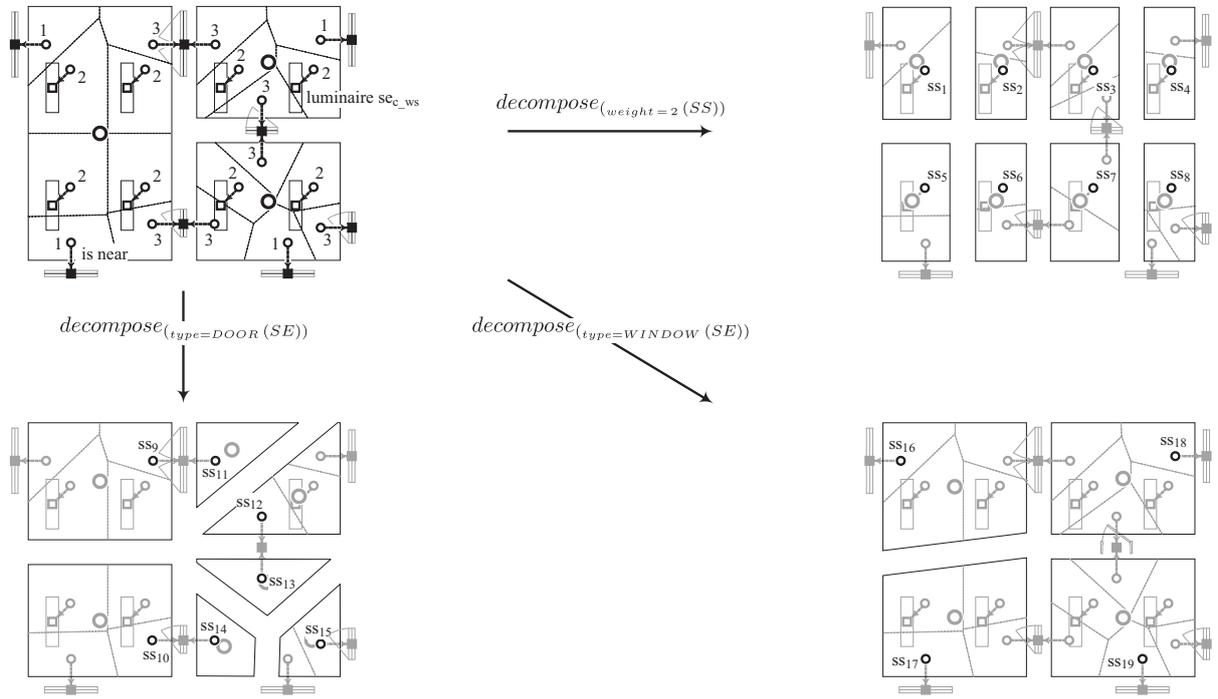


Figure 9: Examples of the *decompose* operation. Subspaces  $ss_1 \dots ss_{19}$  are selected to decompose whole spaces.

376 because they are near doors. Three luminaires are not properly contained in new whole spaces and therefore  
 377 removed when the intermediate layout is converted to the spatially consistent result layout (step 6). In  
 378 the third example (Fig. 9, down right), whole spaces are decomposed based on implicitly selected subspaces  
 379  $ss_{16} \dots ss_{19}$  that are near explicitly selected window *se*'s. Subspaces  $ss_{18}$  and  $ss_{19}$  are the only selected  
 380 subspaces in their whole spaces. Therefore these whole spaces are not decomposed (step 3).

#### 381 4.2.4. *Update*<sub>WEIGHT</sub>

The *update*<sub>WEIGHT</sub> operation derives weights of shortest paths from source *le*'s to nearest destination  
*le*'s in an argument layout *E* and assigns these to weight attributes of source *le*'s. Shortest paths are  
 restricted to a filtered SRN of *E*, as specified by filters on *le*'s and *sr*'s. For example, the *update*<sub>WEIGHT</sub>  
 operation may be used to derive a layout from an argument layout where luminaire weights correspond to  
 the weights of shortest paths from luminaires to nearest windows. The operation has the signature

$$update_{WEIGHT, F_{LE_s}, F_{LE_d}, F_{LE}, F_{SR}}(E)$$

382 where

383 —  $F_{LE_s} = (p_{s,1}(LE), p_{s,2}(LE), \dots, p_{s,k}(LE))$  is a filter on *le*'s in *E* — *le*'s that pass  $F_{LE_s}$  are selected as  
 384 source *le*'s ( $le_s$ 's),

385 —  $F_{LE_d} = (p_{d,1}(LE), p_{d,2}(LE), \dots, p_{d,t}(LE))$  is a filter on  $le$ 's in  $E$  —  $le$ 's that pass  $F_{LE_d}$  are selected as  
386 destination  $le$ 's ( $le_d$ 's),

387 —  $F_{LE} = (p_1(LE), p_2(LE), \dots, p_m(LE))$  is a filter on  $le$ 's in  $E$  —  $le$ 's that pass  $F_{LE}$  are selected as nodes  
388 in the filtered SRN of  $E$ ,

389 —  $F_{SR} = (p_1(SR), p_2(SR), \dots, p_n(SR))$  is a filter on  $sr$ 's in  $E$  —  $sr$ 's that pass  $F_{SR}$  are selected as edges in  
390 the filtered SRN of  $E$ , and

391 —  $E$  is a layout.

392 Weights of  $le_s$ 's selected by  $F_{LE_s}$  are updated by the operation. The result layout has the same structure  
393 as the argument layout.

394 Operation processing involves these steps:

- 395 1. Filter  $F_{LE_s}$  is evaluated to select  $le_s$ 's in the argument layout  $E$ .
- 396 2. Filter  $F_{LE_d}$  is evaluated to select  $le_d$ 's in  $E$ .
- 397 3. For each  $le_s$  the nearest  $le_d$  is determined. Search for the nearest  $le_d$  is restricted to the filtered SRN  
398 of  $E$ , as specified by  $F_{LE}$  and  $F_{SR}$ . Path weights are computed from  $sr$  weights. Weights of  $le$ 's and  
399 directions of  $sr$ 's are ignored.
- 400 4. For each  $le_s$  the weight of the shortest path to its nearest  $le_d$  is assigned to its weight attribute.

401 Examples of the `updateWEIGHT` operation are shown in Fig. 10. In each example, weights of luminaire  
402  $se$ 's in argument layout  $A$  (Fig. 10, top left) are updated with respect to certain window  $se$ 's. Subspace  
403 volumes are not shown in result layouts for improved visualization. For simplicity, the weight of each  $sr$  in  
404 the SRN of  $A$  is assumed to be 1. That is, luminaire weights derived by the operation correspond to lengths  
405 of shortest paths to nearest windows. Alternatively, Euclidean distances between related  $le$ 's could be used  
406 as  $sr$  weights. This would result in luminaire weights that more accurately reflect distances to nearest  
407 windows. In the first example (Fig. 10, top right), all windows are selected as destination  $le$ 's. Shortest  
408 paths are determined based on a filtered SRN that consists of  $N_{SS,SE}$  and  $A_{SS}$  relations. In the second  
409 example (Fig. 10, down left), South oriented windows  $se_1$  and  $se_2$  are selected as destinations. Filter  $F_{LE}$   
410 targets  $se$ 's that are not doors and subspaces. As a consequence, the filtered SRN consists of three connected  
411 components. Weights of two luminaires in whole space  $ws_1$  are undefined because they are disconnected  
412 from  $se_1$  and  $se_2$  in the filtered SRN. In the third example (Fig. 10, down right), West oriented windows are  
413 selected as destinations. The filtered SRN is similar to the third example. However, it has two rather than  
414 three connected components as it additionally includes the door that is 2 m wide. Two luminaires in whole  
415 space  $ws_2$ , which is partially enclosed by that door, have weights of 6 and 7 because they are connected to  
416 the West oriented window  $se_3$ .

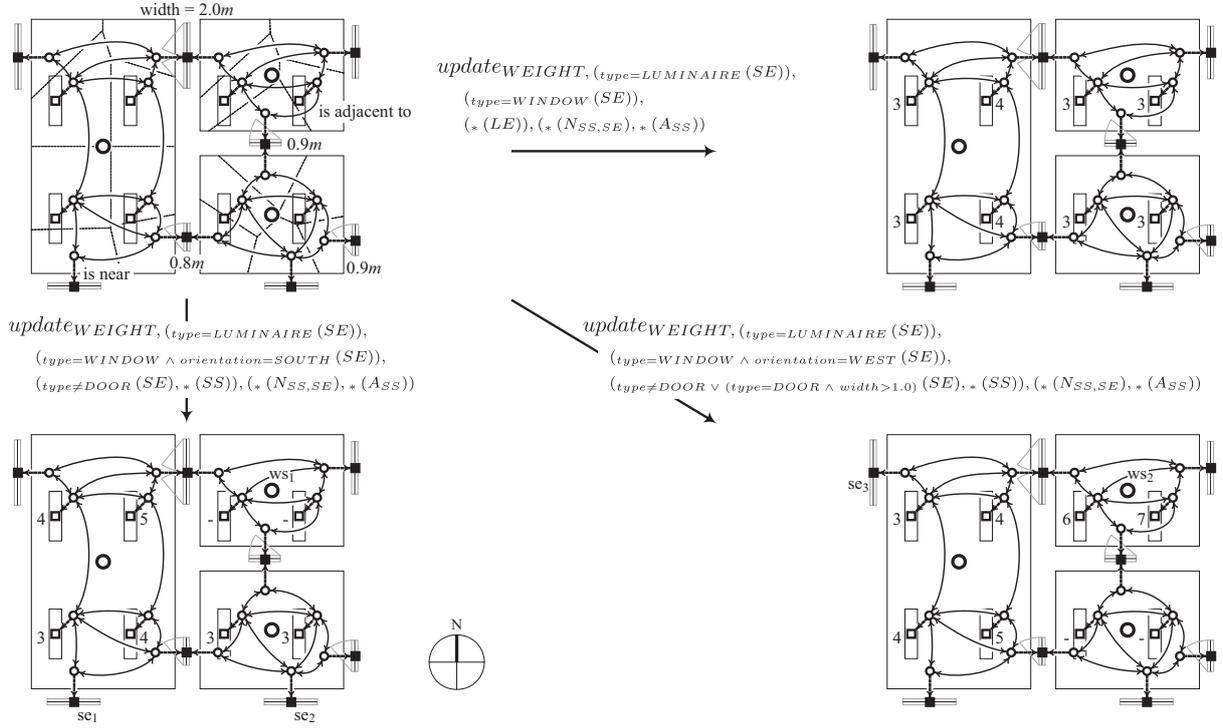


Figure 10: Examples of the  $update\ WEIGHT$  operation. Subspace volumes are not shown in result layouts.

#### 417 4.3. Binary operations

418 Binary operations include *union* ( $\cup$ ), *intersect* ( $\cap$ ), and *subtract* ( $-$ ) operations. As their signatures,  
 419 processing, and examples are similar, each of these aspects is described for all operations.

##### 420 4.3.1. Signatures

The *union* ( $\cup$ ) operation derives a layout by merging overlapping whole spaces in argument layouts  $E_1$  and  $E_2$ . Disjoint or touching whole spaces from  $E_1$  and  $E_2$  are also included in the result layout together with spatially consistent *se*'s, subspaces, and *sbe*'s. The operation has the signature

$$union(E_1, E_2)$$

421 where  $E_1$  and  $E_2$  are layouts.

The *intersect* ( $\cap$ ) operation derives a layout by intersecting overlapping whole spaces in argument layouts  $E_1$  and  $E_2$ . Spatially consistent *se*'s, subspaces, and *sbe*'s from  $E_1$  and  $E_2$  are also included in the result layout. The operation has the signature

$$intersect(E_1, E_2)$$

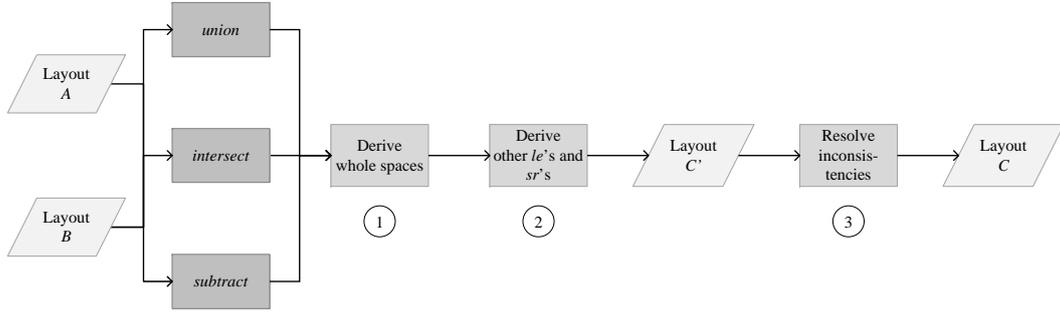


Figure 11: Processing of *union*, *intersect*, and *subtract* operations.

422 where  $E_1$  and  $E_2$  are layouts.

The *subtract* ( $-$ ) operation derives a layout by subtracting whole spaces in argument layout  $E_2$  from overlapping whole spaces in argument layout  $E_1$ . Spatially consistent *se*'s, subspaces, and *sbe*'s from  $E_1$  and  $E_2$  are also included in the result layout. The operation has the signature

$$\textit{subtract}(E_1, E_2)$$

423 where  $E_1$  and  $E_2$  are layouts.

#### 424 4.3.2. Processing

425 The processing of *union*, *intersect*, and *subtract* operations involves these steps (Fig. 11):

- 426 1. Whole spaces are derived from whole spaces in argument layouts  $A$  and  $B$ .
- 427 2. Other *le*'s (that is, subspaces, *se*'s, and *sbe*'s) and *sr*'s are derived from  $A$  and  $B$ .
- 428 3. The intermediate layout  $C'$ , which results from steps 1 and 2, is passed to the *resolve\_inconsistencies*
- 429 operation to generate the spatially consistent result layout  $C$ .

430 While step 1 is operation specific, steps 2 and 3 are the same for all operations.

431 The derivation of whole spaces (step 1) is based on the overlap relation  $O_{WS_A, WS_B}$  between whole spaces  
 432 in argument layouts  $A$  and  $B$ :

$$O_{WS_A, WS_B} = \{(ws_A, ws_B) \in WS_A \times WS_B \mid \textit{clash\_bodies}(ws_A.\textit{volume}, ws_B.\textit{volume}) \in \{\textit{CONTAINS}, \textit{CONTAINS\_ABUTS}, \textit{COINCIDENT}, \textit{INTERLOCK}\}\}$$

433 where

434 —  $WS_A$  is the set of whole spaces in argument layout  $A$ ,

435 —  $WS_B$  is the set of whole spaces in argument layout  $B$ , and

436 — *clash\_bodies* is a function that derives the spatial relation between a given pair of Brep solids [56].

437 A pair of whole space volumes are considered as overlapping if one contains the other (their boundaries  
 438 may or may not abut), if they are coincident, or if their boundaries interlock (in other words, if their interiors  
 439 partially overlap). Fig. 12 includes examples for  $O_{WS_A, WS_B}$  graphs.

440 For the *union* operation, the set  $WS_{C'}$  of whole spaces in the intermediate layout  $C'$  is derived as follows  
 441 (Fig. 12 (a)):

- 442 1. Each whole space in argument layouts  $A$  and  $B$  which does not participate in the  $O_{WS_A, WS_B}$  relation  
 443 (that is, which does not overlap with any whole space in the other layout) is inserted in  $WS_{C'}$ .
- 444 2. A new whole space  $ws_{C', i}$  is created and inserted in  $WS_{C'}$  for each connected component  $O_{WS_A, WS_B, i}$   
 445 of the  $O_{WS_A, WS_B}$  relation graph with more than one whole space node. Whole spaces that are nodes  
 446 in  $O_{WS_A, WS_B, i}$  are merged into  $ws_{C', i}$ . The volume of  $ws_{C', i}$  is derived by solid union of the volumes  
 447 of these merged whole spaces.

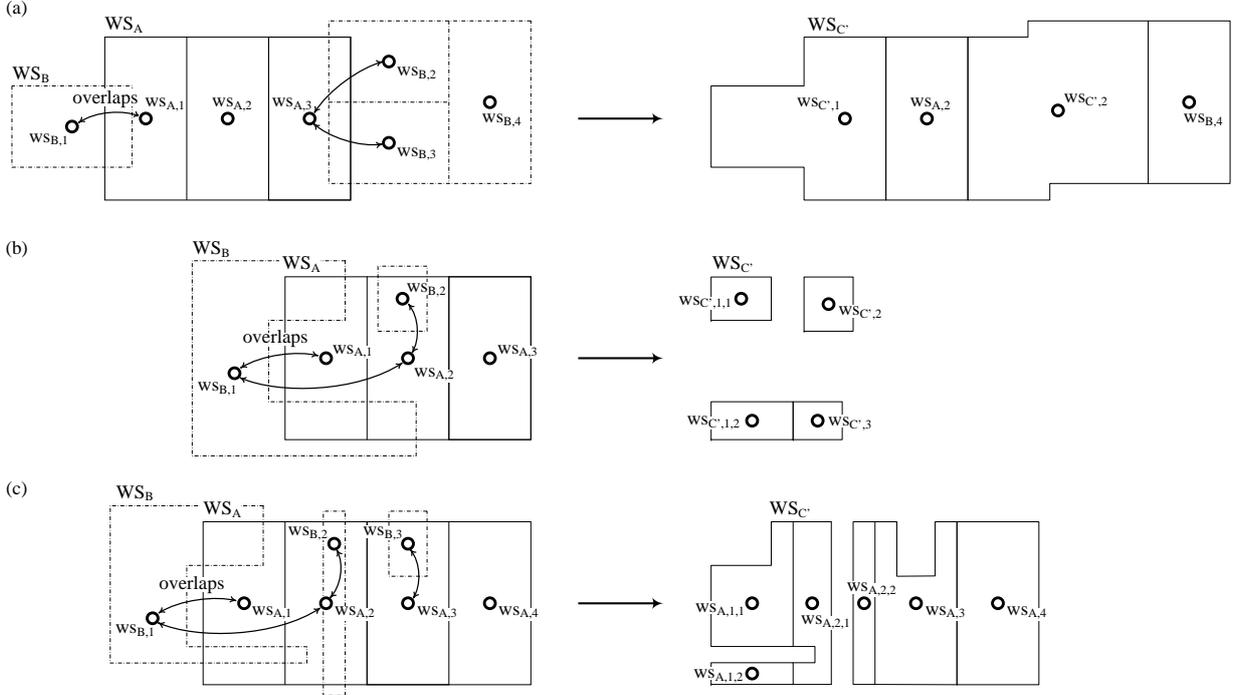


Figure 12: Examples for the derivation of whole space set  $WS_{C'}$ . (a) *union*. (b) *intersect*. (c) *subtract*.

448 For the *intersect* operation, the set  $WS_{C'}$  of whole spaces in the intermediate layout  $C'$  is derived as  
 449 follows (Fig. 12 (b)):

- 450 1. A new whole space  $ws_{C'}$  is created for each pair of overlapping whole spaces  $ws_A$  and  $ws_B$  in  $A$  and  
 451  $B$ . The volume of  $ws_{C'}$  corresponds to the solid intersection of  $ws_A$  and  $ws_B$  volumes.
- 452 2. If the  $ws_{C'}$  volume has a single part (or shell), then  $ws_{C'}$  is inserted in  $WS_{C'}$ .

453 3. If the  $ws_{C'}$  volume has multiple, disconnected parts, then  $ws_{C'}$  is split. Each part becomes the volume  
454 of a new whole space which is inserted in  $WS_{C'}$ .

455 For the *subtract* operation, the set  $WS_{C'}$  of whole spaces in the intermediate layout  $C'$  is derived as  
456 follows (Fig. 12 (c)):

- 457 1. Each whole space in  $A$  (first argument layout) which does not overlap with any whole space in layout  
458  $B$  (second argument layout) is inserted in  $WS_{C'}$ .
- 459 2. The volume of each whole space  $ws_B$  in  $B$  which overlaps a whole space  $ws_A$  in  $A$  is subtracted from  
460 the volume of  $ws_A$  by solid subtraction.
- 461 3. If the modified  $ws_A$  volume is non-empty and has a single part, then  $ws_A$  is inserted in  $WS_{C'}$ .
- 462 4. If the modified  $ws_A$  volume has multiple, disconnected parts, then  $ws_A$  is split. Each part becomes  
463 the volume of a new whole space which is inserted in  $WS_{C'}$ .

464 After the derivation of whole spaces, the next step in the processing of *union*, *intersect*, and *subtract*  
465 operations involves deriving other *le*'s and *sr*'s in the the intermediate layout  $C'$  (Fig. 11, step 2). This is  
466 done by union of subspace, *sbe*, *se*, and *sr* sets from  $A$  and  $B$ . Duplicate *le*'s, that is, *le*'s with the same  
467 unique identifier, are discarded. An *sr* element is included in  $C'$  only if related *le*'s are also included and if  
468 it is not a duplicate.

#### 469 4.3.3. Examples

470 *Union*, *intersect*, and *subtract* operations are illustrated with examples in Fig. 13. Argument layouts  $A$   
471 and  $B$  are at the top of the figure. Result layouts returned by each operation are at the bottom.

472 The union of argument layouts  $A$  and  $B$  returns the result layout at bottom left of Fig. 13. Whole space  
473  $ws_{A,1}$  in  $A$  overlaps with whole space  $ws_{B,1}$  in  $B$ . An L-shaped, merged whole space  $ws_{C,1}$  is created in  
474 the result layout which replaces  $ws_{A,1}$  and  $ws_{B,1}$ . Its volume is derived by solid union of the volumes of  
475  $ws_{A,1}$  and  $ws_{B,1}$ . Whole space  $ws_{A,2}$  in  $A$  touches  $ws_{B,1}$  and is thus included in the result layout without  
476 modification. Door *se*'s in  $A$  and  $B$  are included because they are spatially consistent. Subspaces are  
477 included as well, however, their volumes are inconsistent and regenerated by the *resolve.inconsistencies*  
478 operation.

479 The intersection of  $A$  and  $B$  returns the result layout at bottom center in Fig. 13. Whole spaces  $ws_{A,1}$   
480 and  $ws_{B,1}$  overlap and are replaced by whole space  $ws_{C,2}$  in the result layout. Solid intersection is applied  
481 to the volumes of  $ws_{A,1}$  and  $ws_{B,1}$  to create the volume of  $ws_{C,2}$ . Whole space  $ws_{A,2}$  is removed as it does  
482 not overlap with  $ws_{B,1}$ . Only one door and one subspace from  $A$  and  $B$  are spatially consistent and included  
483 in the result layout.

484 The subtraction of  $B$  from  $A$  returns the result layout at bottom right in Fig. 13. The volume of  $ws_{A,1}$   
485 is modified by solid subtraction of the volume of  $ws_{B,1}$ . Whole space  $ws_{A,2}$  is included in the result layout

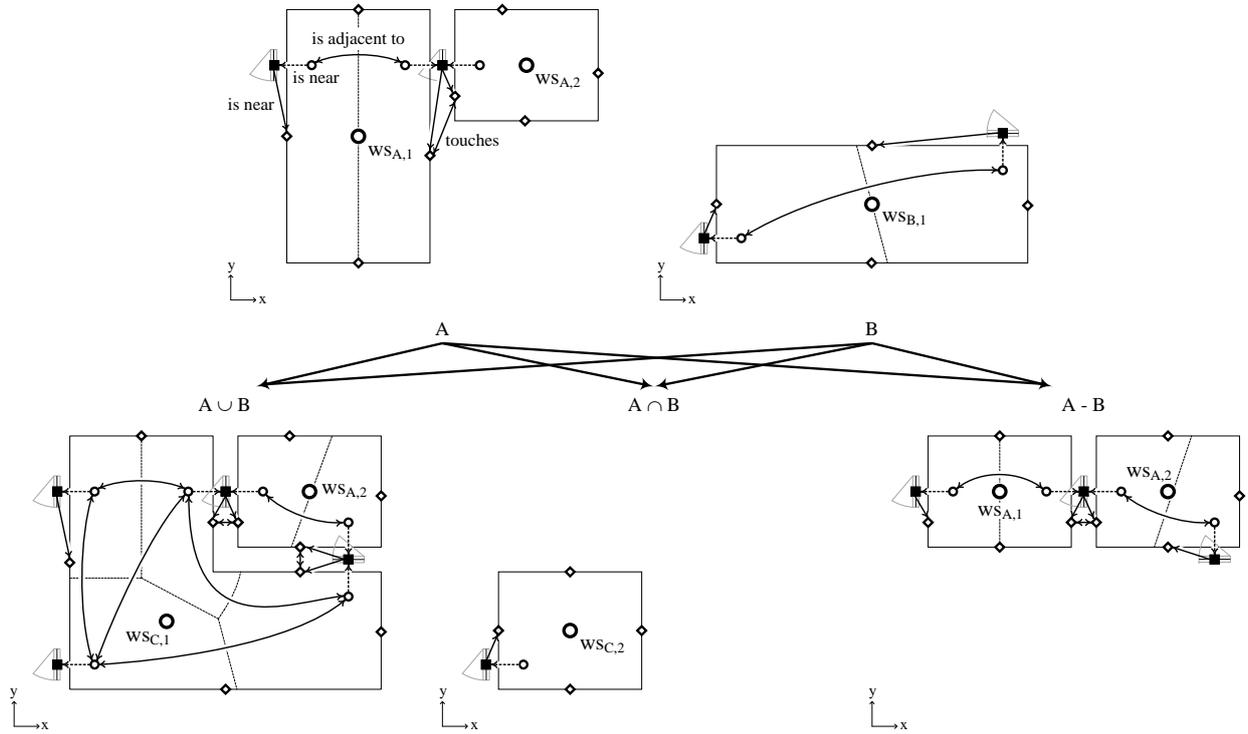


Figure 13: Examples of *union*, *intersect*, and *subtract* operations.

486 without modification as it does not overlap with  $ws_{B,1}$ . Three doors and three subspaces from  $A$  and  $B$  are  
 487 spatially consistent and included in the result layout, and one missing subspace is inserted. All subspace  
 488 volumes are regenerated.

## 489 5. Additional layout operations

490 Fundamental layout operations defined in the previous section may be composed into layout operation  
 491 expressions. Common expressions may be defined as additional layout operations. With these operations,  
 492 it is feasible to develop expressions that are more concise and easier to read.

An example of an additional layout operation is the symmetric difference ( $\Delta$ ) operation, which is a  
 composition of *subtract* and *union* operations:

$$A \Delta B = (A - B) \cup (B - A)$$

The symmetric difference operation in turn may be used to define an *overlay* operation [57]:

$$A \text{ overlay } B = (A \cap B) \cup (A \Delta B)$$

493 Fig. 14 shows an example of the *overlay* operation. Argument layouts  $A$  and  $B$  are at the top of Fig. 14  
494 and the result layout at the bottom.

## 495 6. Implementation

496 We have extended an existing layout modeling system (LMS) prototype with fundamental and additional  
497 layout operations as described in previous sections. LMS is written in C++ [58]. It relies on geometric  
498 modeling, solid modeling, and graph libraries to represent network-based space layouts and process layout  
499 operations.

500 Layout element geometries are modeled in LMS with boundary representation (Brep) solid data struc-  
501 tures of the Acis geometric and solid modeling engine [8, 50]. Whole space volumes in layouts returned by  
502 *aggregate*, *union*, *intersect*, and *subtract* operations are generated by Boolean operations on Brep solids  
503 in Acis [59]. Clash detection functions in Acis are used to derive the overlap relation  $O_{WS_A, WS_B}$  between  
504 whole spaces in the processing of *union*, *intersect*, and *subtract* operations [56]. Connected components  
505 and shortest paths in an SRN are determined with graph algorithm functions in the Boost graph library  
506 [60]. These functions are accessed to process *aggregate* and *update\_{WEIGHT}* operations. Functions in the  
507 computational geometry algorithms library (CGAL) are used to generate Euclidean Voronoi diagrams from  
508 which volumes of new whole spaces are derived in the *decompose* operation [51, 61]. We use Euclidean  
509 rather than geodesic Voronoi diagrams because implementations of the former are currently not available  
510 [62].

## 511 7. Layout operation expression example

### 512 7.1. Zoning for security lighting

513 The feasibility of modeling of multiple space views with layout operation expressions is shown with an  
514 example in which a security lighting layout of a floor of an existing office building is automatically generated  
515 from an architectural layout. The example was implemented in the LMS prototype. It further demonstrates  
516 reuse of space layouts created in BIM authoring systems.

517 An objective in security lighting control is to achieve low, uniformly distributed illuminance levels in  
518 offices during unoccupied hours. A security lighting layout should include security lighting zones that  
519 contain luminaires. This facilitates the assignment of luminaires to lighting controllers. Zones should reflect  
520 proximity of luminaires to windows. This allows a controller to perform daylight harvesting e.g. on weekends  
521 by dimming luminaires that are near naturally lit windows more than distant ones. Zones should further  
522 reflect organizational factors. That is, security lighting may be controlled separately for spaces used by  
523 different organizational units.

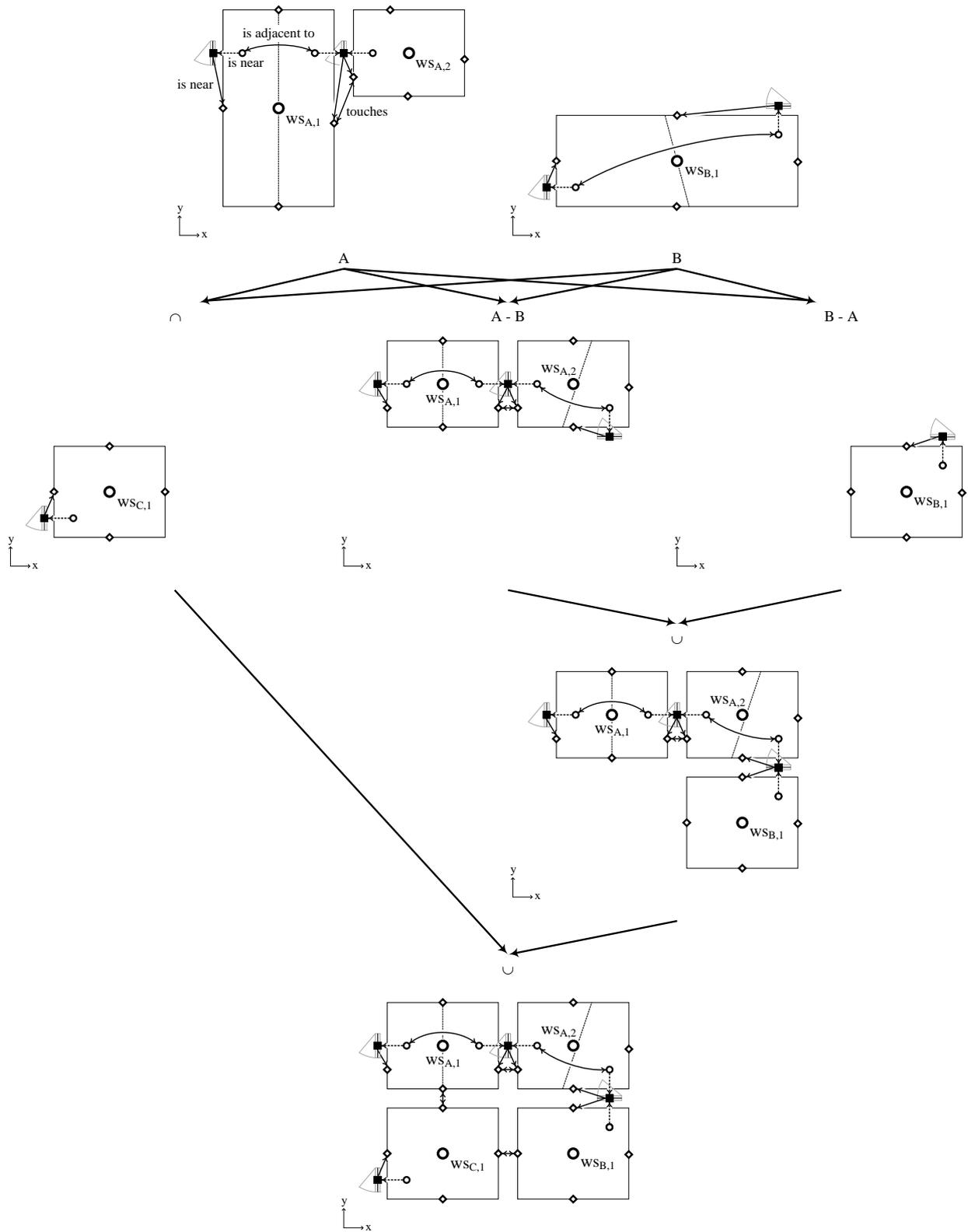


Figure 14: Example of the *overlay* operation.

524 *7.2. Expression*

525 We defined and implemented a layout operation expression in the LMS prototype according to these  
 526 zoning requirements for security lighting in offices. The expression accepts an architectural layout  $A$  (Section  
 527 7.3) as input and returns a security lighting layout:

```

// security lighting layout
overlay (
  // intermediate security lighting layout
  aggregate(weight), (* (WS)), (* (AWS)) (
    updateWEIGHT, (* (WS)), (type=WINDOW (SE)), (* (LE)), (* (AWS)), * (PESE,WS)) (
      decompose(type=LUMINAIRE (SE)) (
        select(WORK ∈ functions (WS), type=LUMINAIRE (SE), type=WINDOW (SE)) (A)
      )))
  // fire safety layout
  aggregate∅, (* (WS), type=DOOR ∧ fire_rating < 180 (SE)), (* (PESE,WS)) (
    select(type=DOOR (SE)) (A)
  )
)

```

528 The expression consists of two sub-expressions. The first derives an intermediate security lighting zone  
 529 layout (Section 7.4) from  $A$ . Zones in this layout do not reflect the requirement of separate control by  
 530 organizational units. For the sake of simplicity, we assume that zones occupied by organizational units  
 531 correspond to fire safety zones. The latter are derived based on fire-resistance properties of doors. Thus  
 532 the second sub-expression derives a fire safety layout (Section 7.5) from  $A$ . The result security lighting zone  
 533 layout (Section 7.6) is obtained by *overlay* of the intermediate security lighting layout and the fire safety  
 534 layout.

535 *7.3. Architectural layout*

536 We evaluated the layout operation expression for an architectural layout  $A$  of the second floor of an  
 537 existing office building on the campus of Vienna University of Technology. Spaces on this floor are used  
 538 by two departments and accessed by two stairs and elevators. Layout  $A$  includes 37 whole spaces and 49  
 539 window, 43 door, 42 desk, and 67 luminaire *se*'s (Fig. 15 (a)). Window, luminaire, and door *se* types were  
 540 defined and used to evaluate the expression (Fig. 15 (b)). Layout  $A$  is spatially inconsistent as it does not  
 541 include *sr* elements and subspaces that are feasible based on these *se* types.

542 We used Autodesk Architecture (AA) to create layout  $A$  [63]. AA is a BIM authoring system for  
 543 architectural design with rich space modeling capabilities. The layout was subsequently loaded into LMS.  
 544 At present, data is exchanged between AA and LMS based on the native data exchange format of the Acis

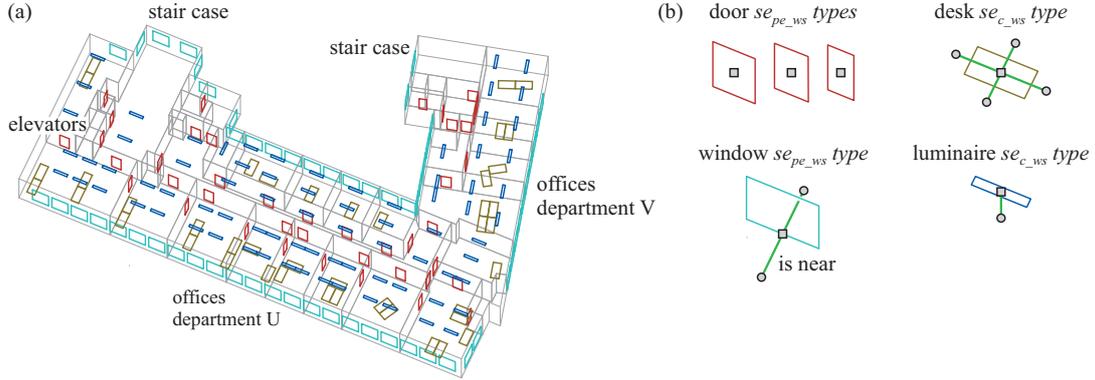


Figure 15: Architectural layout *A*. (a) Layout created in Autodesk Architecture BIM authoring system. (b) Door, desk, window, and luminaire *se* types used to evaluate the layout operation expression.

545 modeler. We plan to implement functions that import data into LMS via IFC in order to improve reuse of  
 546 non-geometric layout data.

#### 547 7.4. Intermediate security lighting layout

548 In the first operation of the sub-expression that derives the intermediate security lighting layout, whole  
 549 spaces with *WORK* function, including offices, meeting, and seminar rooms, are selected from the archi-  
 550 tectural layout *A* (Fig. 16(a)). Luminaire and window *se*'s that are contained in these whole spaces are  
 551 selected as well. As mentioned in Section 4.2.1, a layout that is used as an argument for the *select* operation  
 552 does not need to be spatially consistent. Hence it is feasible to pass the spatially inconsistent *A*, which was  
 553 originally created in the AA BIM authoring system and loaded into LMS, to the *select* operation.

554 In the second operation, whole spaces are decomposed based on subspaces that are near luminaires. As  
 555 a result, each new whole space in the layout returned by the *decompose* operation contains a luminaire.

556 In the third operation, weights of whole spaces are updated with respect to nearest windows (Fig. 16 (c)).  
 557 Weights are derived based on a filtered SRN that consists of  $A_{WS}$  and  $PE_{SE,WS}$  relations. Edges have  
 558 weights of 1. As a result of this operation, whole spaces that are partially enclosed by a window have a  
 559 weight of 1. Whole spaces that are more distant from windows have weights of 2 or 3.

560 In the fourth operation, whole spaces are aggregated into intermediate security lighting zones (Fig. 16 (e)).  
 561 Grouping is done based on whole space weights. The filtered SRN that is used to determine whole space  
 562 connectivity consists of whole spaces and the  $A_{WS}$  relation. All luminaires in a zone have the same weight  
 563 or distance to the nearest window.

#### 564 7.5. Fire safety layout

565 In the first operation of the sub-expression that derives the fire zone layout, all door *se*'s are selected from  
 566 *A* together with whole spaces which they partially enclose. Again, the spatially inconsistent *A* is passed to

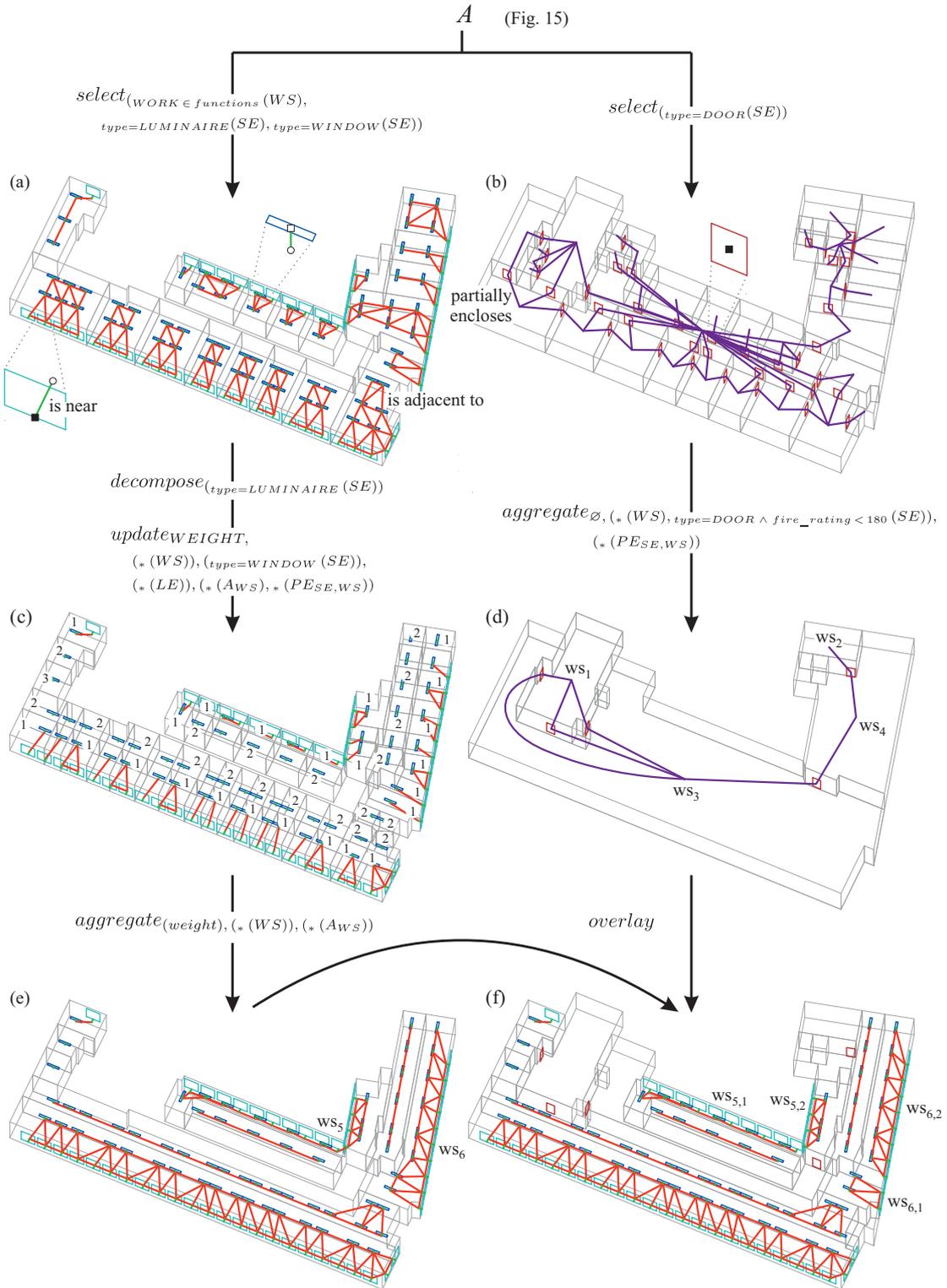


Figure 16: Layout operation expression example. (a) - (c) intermediate layouts, (d) fire safety layout, (e) intermediate security lighting layout, (f) security lighting layout.

567 the *select* operation. Except for inaccessible vertical duct spaces, all whole spaces in  $A$  are selected implicitly  
568 (Fig. 16 (b)). There are no subspaces in the layout resulting from this operation because it is generated with  
569 a door *se* type that does not have subspaces (Fig. 15 (b)).

570 In the second operation, whole spaces are aggregated into fire safety zones (Fig. 16 (d)). As no grouping  
571 attribute is specified ( $G_{WS} = \emptyset$ ), aggregation is done based on whole space connectivity only. The filtered  
572 SRN consists of whole spaces, doors with a fire-rating of less than 180 minutes, and the  $PE_{SE,WS}$  relation.  
573 That is, fire safety zones are separated by doors with a fire-rating of at least 180 minutes. Resulting fire  
574 safety zones correspond to two vertical circulation zones ( $ws_1$  and  $ws_2$ ) and two zones ( $ws_3$  and  $ws_4$ ) that  
575 are used by the two departments.

### 576 7.6. Security lighting layout

577 The security lighting layout returned by the layout operation expression is generated by *overlay* of  
578 intermediate security lighting and fire safety layouts (Fig. 16 (f)). Two whole spaces ( $ws_5$  and  $ws_6$ ) in the  
579 intermediate security lighting layout are split into two new whole spaces each (respectively,  $ws_{5,1}$ ,  $ws_{5,2}$   
580 and  $ws_{6,1}$ ,  $ws_{6,2}$ ) because they span across fire safety zones  $ws_3$  and  $ws_4$ . Altogether, the security lighting  
581 layout generated by the expression meets office security lighting zone requirements for daylight harvesting  
582 and separate control of spaces used by different organizational units (Section 7.1).

## 583 8. Conclusions

584 We have defined a set of operations on network-based space layouts that support modeling of multiple,  
585 domain-specific views of buildings. Operations may be safely composed into expressions as each operation  
586 returns a spatially consistent layout. We have implemented these operations as extensions of an existing  
587 layout modeling system prototype. With a layout operation expression example we have shown the feasibility  
588 of automatically generating a security lighting layout from an architectural layout created in a BIM authoring  
589 system.

590 Further layout operations are desirable to improve the expressiveness of an emerging space modeling  
591 language. The selection of layouts that include layout elements on a shortest path could be useful for indoor  
592 route planning applications. Current work aims to enhance modeling of multiple spatial abstractions of  
593 buildings with operations that derive spatial relations between layouts [64]. For example, whole spaces in  
594 different layouts may be related by containment or overlap relations. This would facilitate queries that  
595 involve the traversal of SRN's of related layouts with graph algorithms. An example is the retrieval of  
596 detailed symbolic location data, such as "the Library is located on the Ground Floor of the North Wing of  
597 the Main Building", from a collection of layouts that model a pedestrian circulation space view.

598 Maintaining the consistency of multiple space views is a relevant issue for future work. For example,  
599 when an architectural designer merges whole spaces in an architectural layout, dependent layouts that

600 model other space views become inconsistent. This could be resolved by re-evaluating expressions that  
601 generate dependent layouts. However, this approach is inadequate for addressing roundtrip or iterative  
602 design scenarios [1]. For example, modification of luminaire locations by a lighting designer would need  
603 to be reflected in the architectural layout. Additional, 'inverse' layout operation expressions are desirable  
604 to reflect such changes in the architectural layout. Similarly, the definition of reusable layout operation  
605 expressions that model space views of specific domains appears promising. Expressions could be defined to  
606 generate layouts for artificial lighting, natural ventilation, access control, and so on. On the other hand, the  
607 generality of these expressions needs to be explored, for example, their potential to model space views for  
608 classes of buildings, such as office buildings or health facilities.

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