Comparison of Synchronous Reluctance Machines with High-Anisotropy Rotors

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Abstract — In terms of torque capability, power factor and efficiency, synchronous reluctance machines with high-anisotropy rotors represent an alternative to conventional induction machines. In particular, they have very robust rotors and can therefore operate at constant power in a wider field-weakening range. The paper discusses a comparison of the various machine concepts using an identical machine geometry by using finite element analyses. Experimental results obtained from two machine designs confirm the numerical analyses.

Index Terms — Two-axes inductances, Reluctance machine, Permanent magnet machine, Synchronous machine, Finite element analysis

I. INTRODUCTION

In most inverter fed electrical drives, an asynchronous induction machine, a synchronous reluctance machine or a permanent magnet excited synchronous machine is utilized. For an application in a high-performance drive with a wide field-weakening range, both types of synchronous machines are more favourable against induction machines due to their inherent suitability for a position-sensorless control scheme and additionally their more robust rotor [1]–[5].

To achieve a comparable performance, the synchronous reluctance machine should have a high-anisotropy rotor design with internal flux barriers [1], [3], [6], [7]. In comparison to the conventional synchronous reluctance machine, the effective saliency of such rotor designs can be increased by permanent magnets inserted into the flux barriers [7]–[10]. On the other hand, the permanent magnet excited synchronous machine can be realized with such a high-anisotropy rotor design and two possible arrangements of the permanent magnets.

Consequently, there are four different machine concepts which utilize identical stator and rotor geometries. The paper compares these machine designs in terms of the operating behaviour in particular in the field-weakening region. In order to confirm the results from various finite element analyses, measurement data from two rotor designs are presented additionally.

II. MACHINE DESIGNS

Fig. 1 depicts the various arrangements of high-anisotropy rotors with internal rotor flux barriers concerned:

a. conventional reluctance machine without any permanent magnets, \( l_d > l_q \),
b. permanent magnet assisted reluctance machine with \( \psi_{Mq} < 0, l_d > l_q \),
c. normal-saliency permanent magnet reluctance machine with \( \psi_{Md} > 0, l_d > l_q \),
d. inverse-saliency permanent magnet reluctance machine with \( \psi_{Md} > 0, l_d < l_q \).

Fig. 2 depicts stator and high-saliency rotor of the different machine designs concerned. With all four designs, the stator is identical and consists of 24 slots carrying a conventional three-phase full-pitch winding. Slot wedges with a magnetic anisotropy are utilized to minimize the cogging torque of the unskewed machine.

With regard to the circumferential symmetry, only one pole pitch is included in the finite element model. The various angular rotor positions are modelled with a concentric sliding surface inside the air-gap. This facilitates fully independent stator and rotor model parts without any remeshing of the air-gap regions when considering different angular rotor displacements [11]–[13].
III. Space Vector Calculus

In the dq rotor fixed reference frame, the normalized stator current and stator flux space vectors are given by

\[ i_{S,dq} = i_S e^{j\beta} = i_{Sd} + j i_{Sq}, \]
\[ \psi_{S,dq} = \psi_S e^{j\theta} = \psi_{Sd} + j \psi_{Sq}, \]

where \( \beta, \theta \) denote stator current angle and stator flux angle, respectively. By using direct and quadrature axis stator inductances \( l_d, l_q \), the stator linkage flux is defined as

\[ \psi_{Sd} = l_d i_{Sd} + \psi_{Md}, \]
\[ \psi_{Sq} = l_q i_{Sq} + \psi_{Mq}. \]

Consequently, the electromagnetic torque can be written as

\[ t_i = -\frac{3}{2} \text{Im} \left( \frac{\psi_{Sd}}{i_{Sd}} \overline{\psi_{S,dq}} \right) = \frac{3}{2} \left( \psi_{Sd} i_{Sd} - \psi_{Sq} i_{Sq} \right) \]
\[ = \frac{3}{2} i_S \left( \frac{\psi_{Md}}{i_S} \sin \beta - \frac{\psi_{Mq}}{i_S} \cos \beta + \frac{l_d - l_q}{2} \sin 2\beta \right). \]

The conventional reluctance machine can be described with a vanishing linkage flux \( \psi_M = 0 \). With the permanent magnet assisted reluctance machine, \( \psi_{Mq} < 0 \) represents the permanent magnet linkage flux which counteracts to any quadrature axis stator current \( i_{Sq} > 0 \). On the other hand, the permanent magnet excited reluctance machine with \( \psi_{Md} > 0 \) can be designed as either a normal-saliency machine \( l_d > l_q \) or an inverse-saliency machine with \( l_d < l_q \).

IV. Analysis Results

A. Comparison with Measurements

Fig. 3 and Fig. 4 depict a comparison of measurement data and numerical results from the permanent magnet assisted reluctance machine with \( \psi_{Mq} = -0.30 \) and the inverse-saliency permanent magnet excited reluctance machine with \( \psi_{Md} = 0.66 \).

The results discussed further on are evaluated from various finite element analyses. Thereby, the electromagnetic torque is obtained from the Maxwell stresses inside the airgap. On the other hand, the inductances presented in the following are always apparent inductances obtained by utilizing the frozen permeabilities method.

B. Reluctance Machines

As from (4), for any given stator current \( i_S \) the maximum torque of the conventional reluctance machine is achieved with a current angle of \( \cos 2\beta = 0 \). On the other hand, for any given stator current \( i_S \) the maximum torque of the permanent magnet assisted reluctance machine is achieved with a current angle of

\[ \sin \beta = \frac{\psi_{Mq}}{4 (l_d - l_q)} i_S + \sqrt{\left( \frac{\psi_{Mq}}{4 (l_d - l_q)} i_S \right)^2 + \frac{1}{2}}. \]

Fig. 5 shows the ratio \( l_d/l_q \) in dependence on the stator current magnitude \( i_S \) with various current angles. Consequently, the permanent magnets with \( \psi_{Mq} = -0.30 \) significantly increase the saliency-ratio resulting in a wider speed range with constant power. Further, Fig. 6 and Fig. 7 depict the torque \( t_i \) with various stator current magnitudes. Finally, Fig. 8 and Fig. 9 show current trajectories result-
ing in a contour map of the torque $t_i$. Obviously, the compensation of the quadrature axis current accomplished by the permanent magnets significantly increases the evolved torque in the range of $0 \leq \beta \leq \pi$.

C. Permanent Magnet Machines

As from (4), for any given stator current $i_S$ in case of the normal-saliency machine the maximum torque of the is achieved with a current angle of

$$
\cos \beta = - \frac{\psi_{Md}}{4 (l_d - l_q) i_S} + \sqrt{\left( \frac{\psi_{Md}}{4 (l_d - l_q) i_S} \right)^2 + \frac{1}{2} \left( \frac{\psi_{Md}}{4 (l_d - l_q) i_S} \right)^2}
$$

(6)

and in case of the inverse-saliency machine

$$
\cos \beta = - \frac{\psi_{Md}}{4 (l_d - l_q) i_S} - \sqrt{\left( \frac{\psi_{Md}}{4 (l_d - l_q) i_S} \right)^2 + \frac{1}{2} \left( \frac{\psi_{Md}}{4 (l_d - l_q) i_S} \right)^2}.
$$

(7)

Fig. 10 shows the ratio $l_d/l_q$ of the normal-saliency machine and the ratio $l_q/l_d$ of the inverse-saliency machine with $\psi_{Md} = 0.66$ in dependence on the stator current magnitude $i_S$ with various current angles. Further, Fig. 11 and Fig. 12 depict the torque $t_i$ with various stator current magnitudes. Finally, Fig. 13 and Fig. 14 show current trajectories resulting in a contour map of the torque $t_i$. Obviously, the inverse-saliency permanent magnet machine yields the highest saliency-ratio resulting in the widest speed range with constant power. On the other hand, the normal-saliency machine acts rather like a reluctance machine because of the high saturation occurring from the flux concentration in the direct axis. Therefore, this arrangement does not present a significant improvement against the arrangement without permanent magnets. Further, the inverse-saliency permanent magnet machine can operate on the current limit in a wide speed range. Consequently, it can produce much higher torque values without demagnetizing the permanent magnets in case of an increased current limit of the inverter. Thus, the inverse-saliency machine shows an inherent suitability for electrical drives where short overload operational conditions require high torque values.

V. Conclusion

Synchronous reluctance machines with internal rotor flux barriers are well suited for an application in position-sensorless drives with a wide field-weakening range due to their high effective saliency. By using an identical machine geometry, the conventional reluctance machine and the permanent magnet assisted reluctance machine as well
and voltage limits of the inverter. These diagrams obvi-
ously show the advantages of a high saliency ratio $L_d/L_q$ in
case of normal-saliency machines or $L_q/L_d$ in case of inverse-
saliency machines in particular in the field-weakening re-
gion. Thereby, the results from the finite element analyses
are successfully compared with measurement data obtained
from two machine designs.

Fig. 11: Torque $t_i$ versus stator current angle $\beta$, current magni-
tudes of $i_S = 0.25 \ldots 1.50$, normal-saliency PM reluctance
machine

Fig. 12: Torque $t_i$ versus stator current angle $\beta$, current magni-
tudes of $i_S = 0.25 \ldots 1.50$, inverse-saliency PM reluctance
machine

as the normal-saliency permanent magnet machine and the
inverse-saliency permanent magnet machine are compared
against their operational behaviour in particular in the
field-weakening range.

The comparison is done in terms of current trajectories
with respect to the $dq$ reference frame according to current
and voltage limits of the inverter. These diagrams obviously
show the advantages of a high saliency ratio $L_d/L_q$ in case of normal-saliency machines or $L_q/L_d$ in case of inverse-
saliency machines in particular in the field-weakening re-
gion. Thereby, the results from the finite element analyses
are successfully compared with measurement data obtained
from two machine designs.

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