

# On the determination of a Kalman filter celestial reference frame and its application in VLBI analysis

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## Introduction

In this study, we use **Kalman filtering** for the creation of a **celestial reference frame (CRF)**. Having time series of radio source coordinates instead of temporally constant coordinates is beneficial for radio sources that exhibit temporal variations, for example, caused by source structure effects. However, the vast majority of radio sources has been observed on only very few occasions. For these sources, the constant coordinate model is sufficient and considerably more efficient to compute. Therefore, **we compute our CRF in two steps**; First, we estimate a **constant** frame of more than 4000 radio sources and then feed the residuals of about 800 selected sources into our Kalman filter to compute a **time series** frame.

We evaluate the CRF solutions by applying them in the **VLBI analysis** and comparing the estimated Earth orientation parameters (EOP) and radio source coordinates among each other as well as to external data sets.

## Methodology

### Two-level approach:

#### Constant frame

- Least-squares adjustment
- Input: normal equations

#### Time series frame

- Kalman filter
- Input: residuals based on constant frame

1. Single-session analysis to create normal equations 
2. Computation of **constant** frame (global solution)
3. Apply constant frame in single-session analysis to estimate residuals
4. Feed residuals into Kalman filter and smoother to create **time series** frame

### Advantages:

Most radio sources have been observed less than five times → **constant** model computationally very efficient

Some radio sources with excellent observational history but irregular behavior (e.g., source structure) → **time series** able to capture these non-linear effects

**Constant + time series** approach allows for a **complete** CRF, taking into account **non-linearity** of selected sources

## VLBI CRF solutions

1980 – 2016.5

5446 IVS-VLBI sessions

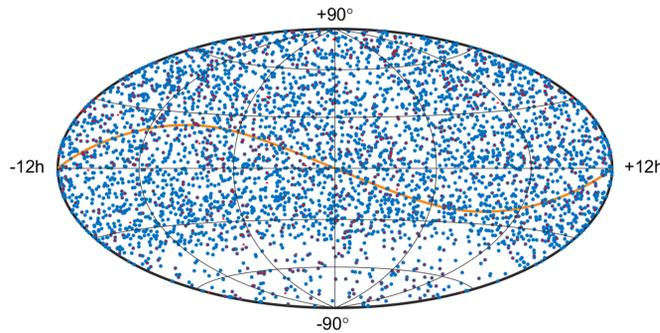


Nothnagel et al., 2015

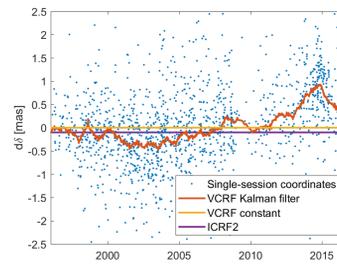
**Constant frame:** 4097 radio sources

**Time series frame:** 822 radio sources

295 used for datum definition

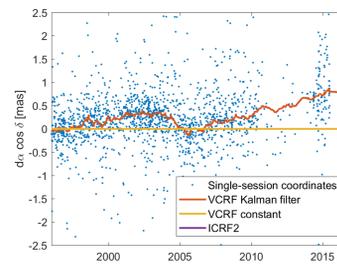


0119+115, declination



ICRF2 defining source

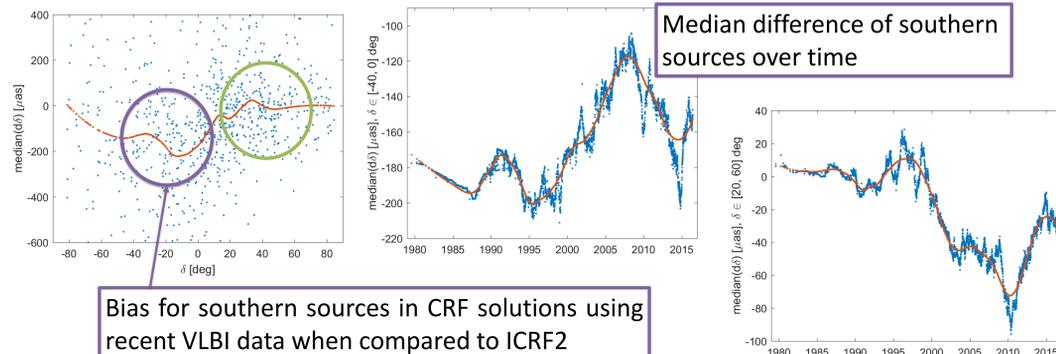
4C 39.25, right ascension



ICRF2 special handling source

## Source coordinates evaluation

### Investigating a temporal evolution of the “declination bias”



Mayer et al., 2017

Bias for southern sources in CRF solutions using recent VLBI data when compared to ICRF2

Median difference of southern sources over time

For comparison, the same for northern sources

### Source coordinates in VLBI analysis

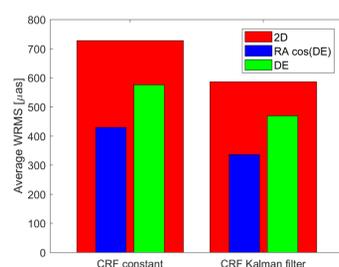
| WRMS [ $\mu$ as]         | RA cos(DE) | DE   | 2D   |
|--------------------------|------------|------|------|
| CRF constant             | 429        | 576  | 728  |
| CRF Kalman filter        | 336        | 470  | 586  |
| $\Delta$ (KF – constant) | -22%       | -18% | -20% |

estimated offsets

$$\tilde{x} = x_0 + \Delta x$$

overall coordinates

a priori coordinates (from CRF)



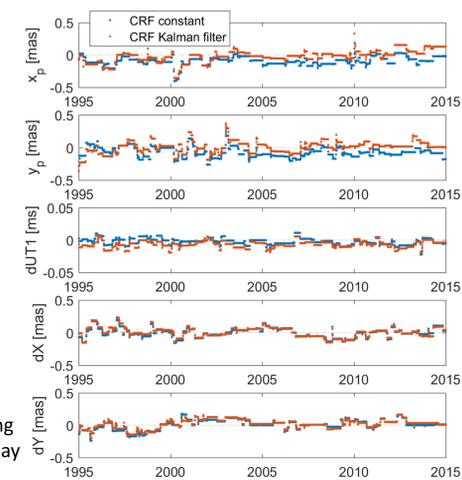
“repeatability”

| WRMS [ $\mu$ as]         | RA cos(DE) | DE  | 2D  |
|--------------------------|------------|-----|-----|
| CRF constant             | 452        | 586 | 753 |
| CRF Kalman filter        | 462        | 599 | 769 |
| $\Delta$ (KF – constant) | +2%        | +2% | +2% |

References:  
Nothnagel et al., 2015: The IVS data input to ITRF2014. International VLBI Service for Geodesy and Astrometry, GFZ Data Services. <http://doi.org/10.5880/GFZ.1.1.2015.002>  
Mayer et al., 2017: Tropospheric delay modelling and the celestial reference frame at radio wavelengths. *Astronomy & Astrophysics*, 606:A143

## EOP evaluation

- Differences of EOP estimated in VLBI analysis w.r.t. IERS 14 C04 (plot & tables) and DTRF2014 EOP (tables)
- Similar results for EOP from ITRF2014 and JTRF2014 (not shown here)



Plotted: moving medians (30-day window)

| WRMS [ $\mu$ as]         | $x_p$ | $y_p$ | dUT1 | dX  | dY  |
|--------------------------|-------|-------|------|-----|-----|
| CRF constant             | 225   | 243   | 221  | 208 | 195 |
| CRF Kalman filter        | 223   | 216   | 237  | 211 | 197 |
| $\Delta$ (KF – constant) | -1%   | -11%  | +7%  | +1% | +1% |

Reference: IERS 14 C04

| WRMS [ $\mu$ as]         | $x_p$ | $y_p$ | dUT1 | dX  | dY  |
|--------------------------|-------|-------|------|-----|-----|
| CRF constant             | 209   | 211   | 217  | 208 | 194 |
| CRF Kalman filter        | 214   | 215   | 222  | 211 | 196 |
| $\Delta$ (KF – constant) | +2%   | +2%   | +2%  | +1% | +1% |

| WRMS [ $\mu$ as]         | $x_p$ | $y_p$ | dUT1 | dX  | dY  |
|--------------------------|-------|-------|------|-----|-----|
| CRF constant             | 221   | 216   | 690  | 377 | 377 |
| CRF Kalman filter        | 225   | 221   | 691  | 377 | 380 |
| $\Delta$ (KF – constant) | +2%   | +2%   | +0%  | 0%  | +1% |

Reference: DTRF2014 EOP

| WRMS [ $\mu$ as]         | $x_p$ | $y_p$ | dUT1 | dX  | dY  |
|--------------------------|-------|-------|------|-----|-----|
| CRF constant             | 243   | 240   | 691  | 378 | 378 |
| CRF Kalman filter        | 226   | 219   | 693  | 377 | 380 |
| $\Delta$ (KF – constant) | -7%   | -9%   | +0%  | -0% | +1% |

after subtracting trend

## Summary

- **2-level CRF: complete constant** frame, consistent with **time series** frame of well-observed sources (taking into account **non-linear** coordinate variations)
- Time series allows to study **time dependence of declination bias**
- **Performance in VLBI analysis:** estimated coordinate offsets 20% smaller for Kalman filter CRF; repeatabilities of coordinates and EOP within a few percent

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