

PAPER • OPEN ACCESS

Evidence for a universal Fermi-liquid scattering rate throughout the phase diagram of the copper-oxide superconductors

To cite this article: N Bariši *et al* 2019 *New J. Phys.* **21** 113007

View the [article online](#) for updates and enhancements.

Recent citations

- [Phonon spectrum of underdoped HgBa₂CuO₄+ investigated by neutron scattering](#)
I. Ahmadova *et al*



PAPER

Evidence for a universal Fermi-liquid scattering rate throughout the phase diagram of the copper-oxide superconductors

OPEN ACCESS

RECEIVED

18 May 2019

REVISED

27 August 2019

ACCEPTED FOR PUBLICATION

11 October 2019

PUBLISHED

1 November 2019

Original content from this work may be used under the terms of the [Creative Commons Attribution 3.0 licence](#).

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



N Barišić^{1,2,3}, M K Chan^{2,6}, M J Veit^{2,7}, C J Dorow^{2,8}, Y Ge^{2,9}, Y Li², W Tabis^{1,2,4}, Y Tang², G Yu², X Zhao^{2,5} and M Greven²

¹ Institute of Solid State Physics, TU Wien, A-1040, Vienna, Austria

² School of Physics and Astronomy, University of Minnesota, Minneapolis, MN 55455, United States of America

³ Department of Physics, Faculty of Science, University of Zagreb, HR-10000 Zagreb, Croatia

⁴ AGH University of Science and Technology, Faculty of Physics and Applied Computer Science, 30-059 Krakow, Poland

⁵ State Key Lab of Inorganic Synthesis and Preparative Chemistry, College of Chemistry, Jilin University, Changchun 130012, People's Republic of China

⁶ Present address: National High Magnetic Field Laboratory, Los Alamos National Laboratory, Los Alamos, NM 87545, United States of America.

⁷ Present address: Department of Applied Physics, Stanford University, Stanford, CA 94305, United States of America.

⁸ Present address: Department of Physics, University of California, San Diego, CA 92093, United States of America.

⁹ Present address: Department of Physics, Penn State University, University Park, PA 16802, United States of America.

E-mail: nbarisic@phy.hr and greven@umn.edu

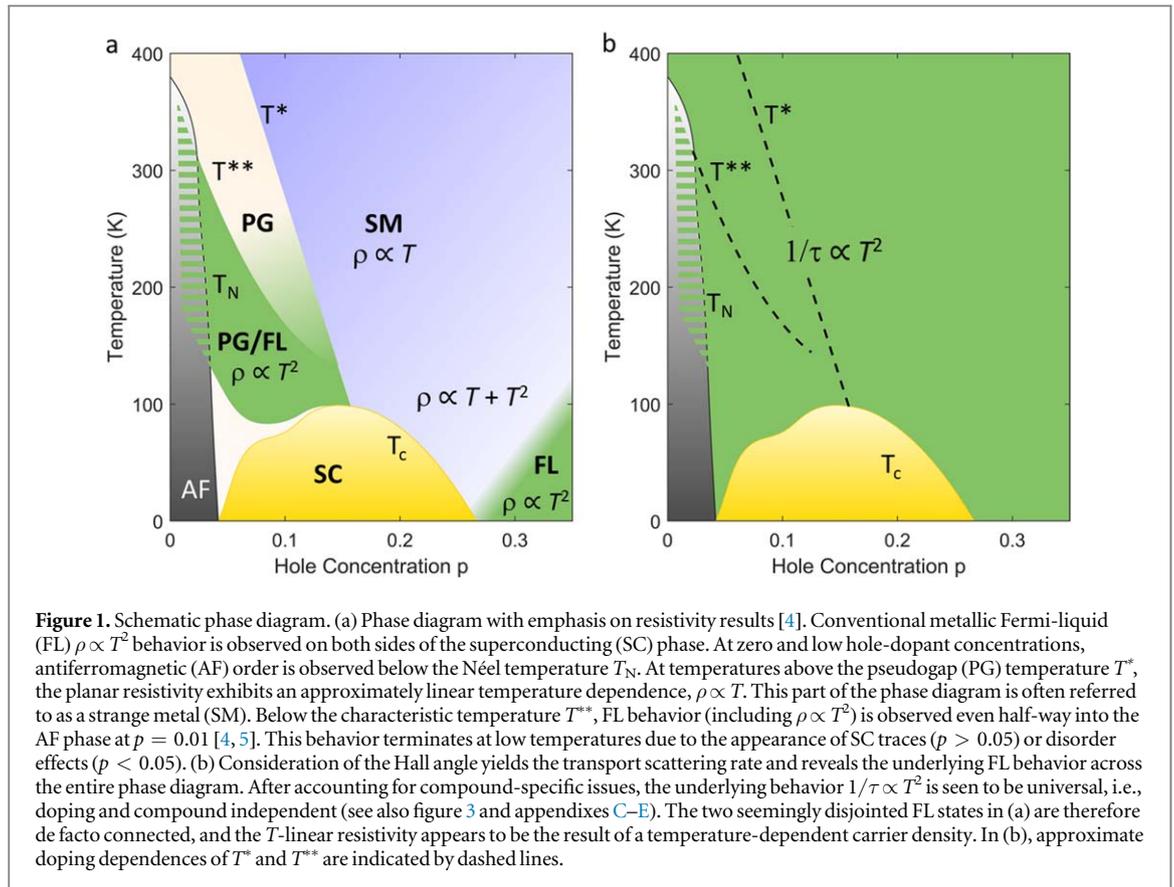
Keywords: cuprate superconductors, transport properties, phase diagram, pseudogap (PG), strange-metal (SM), fermi liquid (FL)

Abstract

The phase diagram of the cuprate superconductors continues to pose formidable scientific challenges. While these materials are typically viewed as doped Mott insulators, it is well known that they are Fermi liquids at high hole-dopant concentrations. It was recently demonstrated that at moderate doping, in the pseudogap (PG) region of the phase diagram, the charge carriers are also best described as a Fermi liquid. Nevertheless, the relationship between the two Fermi-liquid (FL) regions and the nature of the strange-metal (SM) state at intermediate doping have remained unsolved. Here we show for the case of the model cuprate superconductor $\text{HgBa}_2\text{CuO}_{4+\delta}$ that the normal-state transport scattering rate determined from the cotangent of the Hall angle remains quadratic in temperature across the PG temperature, upon entering the SM state, and that it is doping-independent below optimal doping. Analysis of prior transport results for other cuprates reveals that this behavior is universal throughout the entire phase diagram and points to a pervasive FL transport scattering rate. These observations can be reconciled with a variety of other experimental results for the cuprates upon considering the possibility that the PG phenomenon is associated with the gradual, non-uniform localization of one hole per planar CuO_2 unit.

1. Introduction

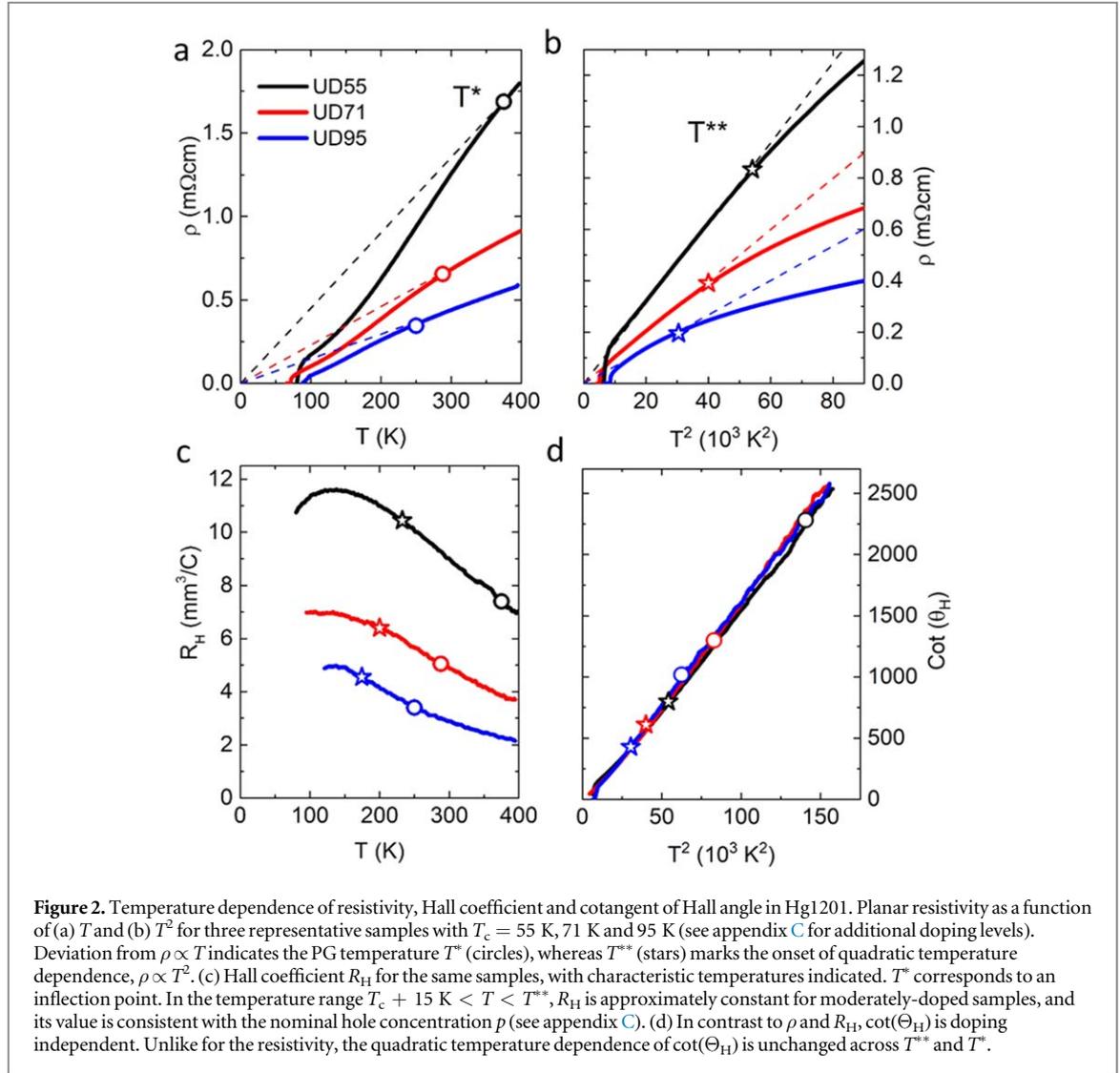
The cuprates exhibit a complex phenomenology that is often argued to be incompatible with Landau's highly successful Fermi-liquid (FL) description of conventional metals [1], except at very high hole-dopant concentrations p ($p > 0.30$) [2, 3]. In the undoped state, these materials are Mott insulators with strong antiferromagnetic correlations. The approximately linear temperature dependence of the planar dc-resistivity ($\rho \propto T$) in the so-called strange-metal (SM) region of the phase diagram (figure 1(a)) is observed from about 10 to 1000 K [6] and can reach rather large values in excess of 1 m Ω cm. This is a seemingly unphysical situation wherein the electronic mean-free path appears to be shorter than the lattice constant, and hence the Ioffe-Regel limit is crossed. Consequently, the conventional theoretical description of metals based on quasiparticles with well-defined crystal momenta that experience occasional scattering events is often argued to be inadequate [1]. At the hole concentration $p^* \approx 0.19$, just above the optimal doping level at which the superconducting (SC) transition temperature (T_c) is maximized, the SC state directly evolves from the peculiar SM state. The



intervening region of the phase diagram at lower doping is marked by the pseudogap (PG) phenomenon below $T^*(p)$ and by evidence for a phase transition [7–14]. These and other experimental observations have been argued to be the result of an underlying quantum critical point at p^* with associated fluctuations that give rise to the extended T -linear resistive behavior and to the superconductivity [1]. On the other hand, there also have been suggestions that, fundamentally, FL theory should prevail [4, 15–19], and that the consideration of electron interactions results in resistivity saturation values much larger than implied by the Ioffe-Regel condition, consistent with experiment [4, 20]. In fact, there has been a recent revival of FL concepts in correlated systems in general, including considerations of a FL scattering rate that extends to high temperatures (appendix A).

HgBa₂CuO_{4+δ} (Hg1201) may be viewed as a model compound due to its relative structural simplicity (tetragonal symmetry, one CuO₂ layer per formula unit, no CuO chains), negligible residual resistivity and large optimal T_c of nearly 100 K [21]. Below T^{**} ($T_c < T^{**} < T^*$; figure 1(a)), the planar resistivity of Hg1201 exhibits quadratic temperature dependence, $\rho \propto T^2$, the behavior characteristic of a FL [4]. This finding motivated optical conductivity measurements that yielded the quadratic frequency dependence and the temperature-frequency scaling of the optical scattering rate close to that predicted theoretically for the umklapp FL [22]. Furthermore, at temperatures below T^{**} , the magnetoresistance of Hg1201 was found to obey Kohler’s rule, a property of conventional metals [23].

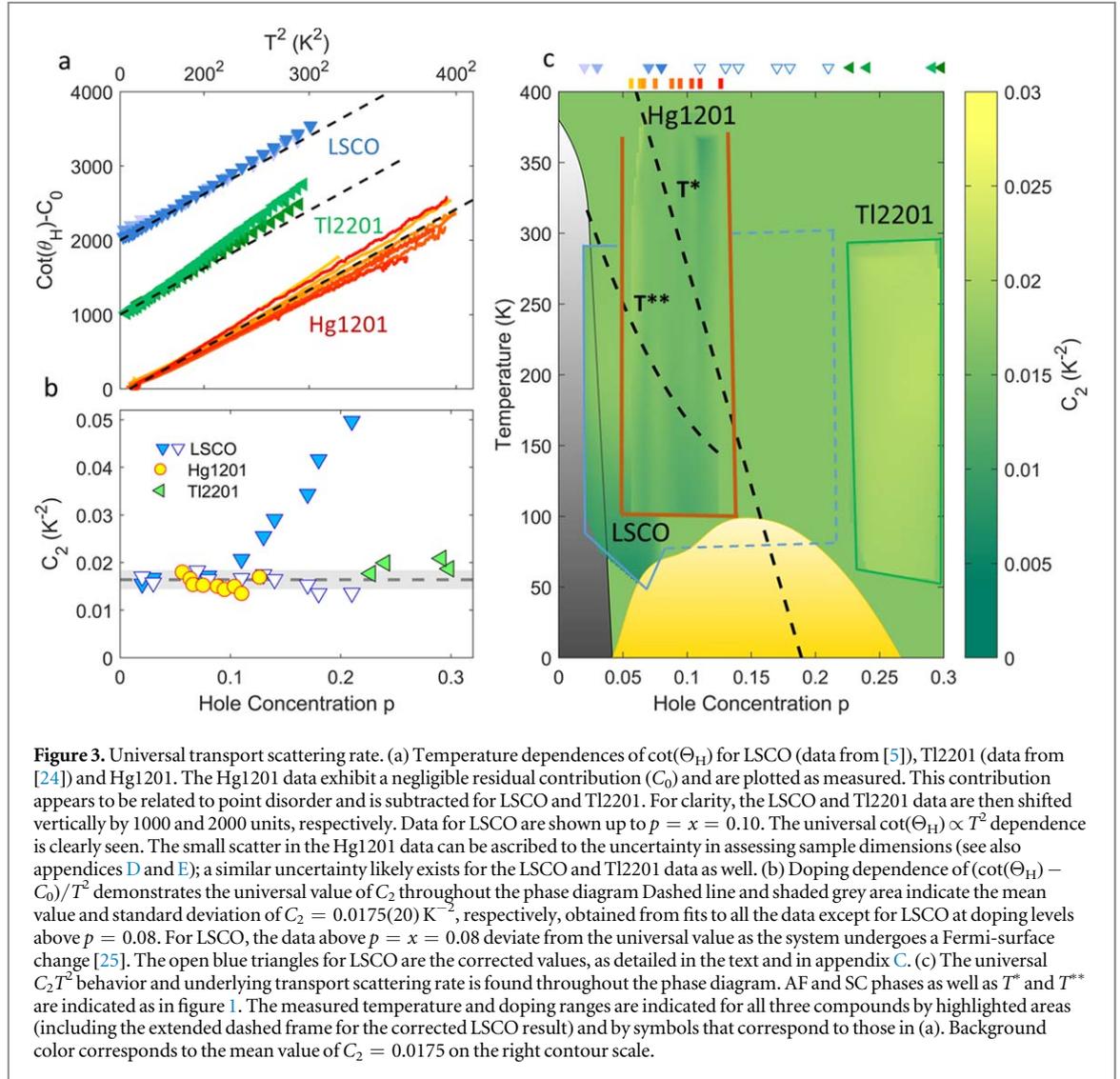
In contrast to previous approaches that extended ideas developed for the SM phase to the PG phase, we start here from the now well-documented PG/FL state of Hg1201 [4, 22, 23] and find that the cotangent of the Hall angle, and hence the quadratic transport scattering rate is unaltered in the SM phase, and that it is independent of doping in the range $0.05 < p < 0.14$. We then demonstrate that the scattering rate is in fact doping and compound independent throughout the entire normal-state phase diagram, and hence universal. Although the magnitude of the quadratic temperature dependence of the cotangent of the Hall angle may exhibit compound-specific deviations from the underlying universal value, we demonstrate for the cuprate La_{2–x}Sr_xCuO₄ (where this effect is the largest due to the presence of a Lifshitz transition) that these deviations can be understood as a breakdown of the effective-mass approximation rather than of the FL concept. Based on these new insights, we propose a fundamentally new understanding of the cuprates: the seemingly disconnected PG/FL [4, 22, 23] and overdoped FL [2, 3] regions are in some sense connected, and the notion that the carrier density in the SM region is independent of temperature has to be abandoned.



2. Transport measurements

As noted, these conclusions follow from the behavior of the cotangent of the Hall angle, $\cot(\Theta_H)$, which is the ratio of planar resistivity, ρ , to Hall resistivity, $\rho_H = HR_H$, where H is the magnetic field and R_H is the Hall coefficient. Within the simple effective-mass approximation that assumes a parabolic band, $\rho = m^*/(ne^2\tau)$ and $R_H = 1/(ne)$, where m^* is the effective mass and n is the carrier density, so that $\cot(\Theta_H) = \rho/\rho_H \propto m^*/\tau$ is independent of the carrier density and essentially a direct measure of the scattering rate $1/\tau$.

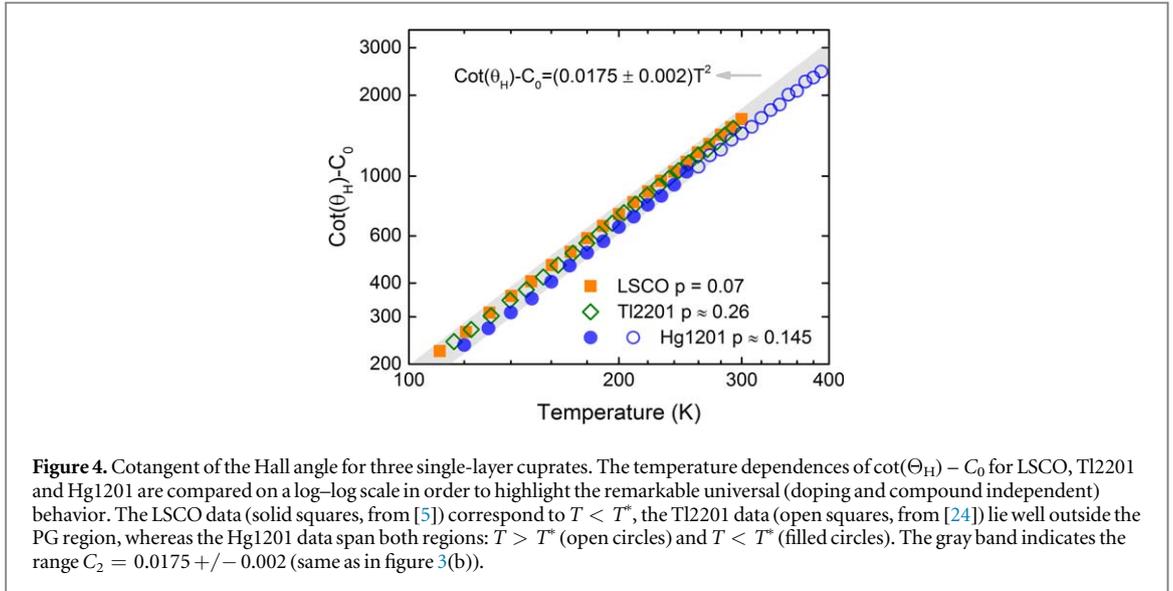
Figure 2 shows the temperature dependences of the resistivity and Hall coefficient for Hg1201 up to 400 K (see appendix B for experimental details). The resistivity exhibits the well-known (approximate) linear behavior at temperatures above T^* and a quadratic dependence in the PG/FL state (for $T_c < T < T^{**}$). One of our key findings for this model cuprate is that $\cot(\Theta_H) \propto T^2$ not only in the PG/FL phase, where $1/\tau \propto T^2$ has been established [4, 23], but that this quadratic temperature dependence remains unaffected upon crossing T^{**} and T^* , and moreover is independent of doping. This is demonstrated in figure 2(d) for three doping levels and summarized in figure 3 along with matching results for five additional doping levels (see also appendix C). Since there exist no noticeable changes in behavior at T^{**} and T^* , the simplest and most natural interpretation is that $\cot(\Theta_H)$ continues to measure the scattering rate at temperatures above T^{**} , which would imply that the effective mass is doping and temperature independent, consistent with other experimental observations [4, 26–30]. A seemingly less likely possibility is a coincidental compensation effect across distinct parts of the phase diagram involving a scattering rate and effective mass that are both temperature- and doping-dependent in a manner that conspires to give rise to the simple and robust $\cot(\Theta_H) = C_2 T^2$ behavior. In principle, both the SM and the PG/FL regime could exhibit this behavior for different reasons, with distinct temperature dependences of the Hall (τ_H) and transport (τ_{tr}) scattering rates for $T > T^{**}$ [31], but then it would be purely accidental to find the same value of C_2 , which we consider highly unlikely.



3. Comparison with other single-layer cuprates

Motivated by these observations for Hg1201, we compare in figure 3 our data for $\cot(\Theta_H)$ to already published results for the thoroughly investigated cuprates $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (LSCO) [5] and $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ (Tl2201) [24]. The three compounds have in common that they all feature a single CuO_2 layer per structural unit. The LSCO data correspond to the PG region of the phase diagram ($T < T^*$) and extend to the non-SC state at low doping, whereas the Tl2201 results correspond to high doping levels, where FL behavior has been firmly established [1–3]. The combined data span nearly the entire phase diagram. All three compounds exhibit quadratic temperature dependence, $\cot(\Theta_H) = C_0 + C_2 T^2$. The compound/sample specific residual term C_0 is related to disorder [32] and effectively absent in Hg1201. Remarkably, within the measurement error, all three cuprates (except LSCO for $p > 0.08$; see below) exhibit the same value of C_2 (see also appendix D). Since there is good evidence that the effective mass is essentially independent of compound and doping [4, 26–30], this indicates that the transport scattering rate is universal across the cuprate phase diagram (figure 1(b)).

This remarkable result is highlighted in figure 4, which shows representative data for the temperature dependences of $\cot(\Theta_H) - C_0$ on a log–log scale for the three single-layer cuprates LSCO, Tl2201 and Hg1201. The respective data correspond to different parts of the phase diagram, and range from highly underdoped (LSCO, $p = 0.07$) to highly overdoped (Tl2201, $p \approx 0.26$). For Hg1201 ($p \approx 0.145$), they span different regions (from $T < T^{**}$ to $T > T^*$), without any noticeable change in behavior. Clearly, the slope (C_2) is the same in all cases. To the best of our knowledge, this newly uncovered universality is not captured by previous theories for the cuprates.



4. Implications for the Fermi surface at low temperatures

The main difficulty in understanding the resistivity, Hall coefficient and other electronic properties of the cuprates is associated with the rather unusual Fermi-surface evolution with temperature [33] and doping [25] (see also appendix D). The simple universal quadratic temperature dependence of the cotangent of the Hall angle established here provides a crucial new constraint. Accordingly, two Fermi-surface changes with temperature/doping should be distinguished and carefully considered.

First, we consider the character of the Fermi surface at temperatures below T^{**} . The most prominent feature in the PG phase is the antinodal gap at the Fermi level. This partial gap does not appear to affect the near-nodal parts of the Fermi surface (arcs), but rather determines their length [33]. The carrier density in the PG phase, as deduced from dc-resistivity [4] and optical conductivity [22] measurements is proportional to the hole concentration p , and the observation of FL charge transport [4, 22, 23] suggests that the arcs must be well-formed below T^{**} [4]. Indeed, the Hall density $n_H = 1/(eR_H)$ is approximately constant for $T_c < T < T^{**}$ [5]. For Hg1201, this is best seen for the $T_c = 71$ K sample (figure 2(c)), whereas for LSCO this observation extends over a wider temperature/doping range [5]. Importantly, for $T_c < T < T^{**}$, n_H yields a carrier density that corresponds quite well to the nominal hole density, $n_H \approx p/V$, where V is the unit cell volume. For LSCO, this is the case up to about $p = x = 0.08$ [5]. For Hg1201, this holds for the entire doping range of the present study, apart from a systematic offset of about 25% that can be ascribed to the uncertainty in determining the absolute value of p in cuprates in which hole carriers are introduced into the CuO_2 planes via excess oxygen atoms in the interstitial layers (appendix C). Deep in the PG/FL region of Hg1201, where the resistivity exhibits simple quadratic temperature dependence, there remains a relatively weak temperature dependence of R_H . In contrast to the resistivity ($\rho = 1/\sigma_{xx}$), the Hall coefficient ($R_H = \sigma_{xy}/(H\sigma_{xx}\sigma_{yy})$, where σ is the conductivity tensor) is sensitive (via σ_{xy}) to the curvature and the details of the termination of the arcs. The weak temperature dependence of R_H between T_c and T^{**} might therefore be related to the subtleties of the arc-tip formation. Alternatively, it might be associated with the appearance of SC traces [34–36] or with charge-density-wave correlations [37].

Second, with increasing hole concentration, the cuprates undergo a change from Fermi arcs to a closed Fermi surface in a non-universal, compound-specific fashion [25]. In the general case of a non-parabolic electronic band, the off-diagonal terms of the conductivity tensor need to be taken into account, as noted in the case of LSCO [38]. For LSCO, the observed deviation from $n_H = p/V$, for $p > 0.08$ and $T_c < T < T^{**}$, and the apparent divergence of n_H at $p \approx 0.22$ are related to changes in the curvature of the Fermi surface [25] (appendix D). The Hall coefficient therefore ceases to be a proper measure of the carrier density in this doping range, and the observed behavior is the result of the failure of the effective-mass approximation rather than of the applicability of the FL concept [38]. Indeed, for LSCO at $p > 0.08$, $\cot(\Theta_H)$ remains quadratic in temperature [5], but C_2 starts to increase (figure 3(b)) with the concomitant change in curvature of the underlying Fermi surface. We therefore expect the Hall effect to systematically overestimate the carrier density in this doping range. We can test this hypothesis by correcting the Hall data based on the assumption that the true doping level for $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ remains $p = x$ at temperatures below T^{**} (appendix D), consistent with the dc resistivity [4] and optical conductivity [22] results. As shown in figure 3(b), the corrected values of C_2 indeed

agree with the universal value. Evidently, as also demonstrated in figure 3(b), no such correction is necessary for Hg1201 and Tl2201 in the studied doping ranges. We note that comparable values of C_2 have also been obtained for several multi-layer cuprates and that, similar to LSCO, there exist systematic deviations from the underlying universal behavior near optimal doping (appendix E).

These observations provide new insight into the charge transport throughout the entire phase diagram. Since the universal magnitude and temperature dependence of the scattering rate directly connect the PG/FL, SM, and overdoped FL regions without any changes at T^* and T^{**} , the archetypal linear temperature dependence of the resistivity may not reflect a linear scattering rate, contrary to common belief [1]. Instead, the $\rho \propto T$ behavior appears to be the result of a temperature-dependent carrier density, consistent with the well-known approximate $1/R_H \propto T$ behavior for $T > T^*$ [5, 18, 39]. In fact, a change in carrier density must always be associated with the formation of a gap, and the PG cannot be an exception. In other words, it is a priori incorrect to interpret any gap formation exclusively through a change in the scattering rate, without taking into account the change in carrier density.

5. Fermi surface and intrinsic inhomogeneity

The canonical Landau FL features well-defined low-energy quasiparticles whose density does not depend on temperature and satisfies Luttinger's theorem at zero temperature, namely that the particle density enclosed by the Fermi surface equals the total electron density [3, 40]. The situation is clearly more complex in the case of the cuprates, which seemingly lack a continuous Fermi surface in the PG phase. Nevertheless, there exist well-defined 'nodal' quasiparticles [55, 91], FL behavior is observed [4, 22, 23] and, as discussed, the Hall coefficient in compounds such as Hg1201 and LSCO is a good measure of the carrier density deep in the PG/FL region of the phase diagram [5]. A simple estimate of the carrier density from the arc length in the PG/FL regime indeed suggests that the density is low and increases with doping ($\approx p$) [4]. More rigorous theoretical modeling yields the same conclusion [18, 38]. The Hall data, including the present result, are overall consistent with a gradual evolution from p carriers that reside on arcs at temperatures below T^{**} toward a full Fermi surface of size $1 + p$ not only at large doping levels [3], but also at high temperatures [5, 39] (see also appendixes F and G).

Our findings also call for a reinterpretation of experimental results for the SM region of the phase diagram. In particular, it is of interest to consider optical conductivity and photoemission results along the lines discussed in appendix G. The gradual delocalization with increasing doping and temperature of one hole per CuO_2 might be the result of the dual covalent and ionic character of the cuprates [15, 17]. In order to better understand how such an unusual behavior might arise, we suggest that it is important to recognize that the cuprates feature considerable inherent structural and hence electronic inhomogeneity [41–44], in addition to disorder associated with doping [45]. Bulk nuclear magnetic resonance measurements reveal significant spatial inhomogeneity even for simple tetragonal Hg1201 [46], yet they also indicate the simultaneous presence of local PG and FL electronic components in the CuO_2 planes [47]. Upon increasing the temperature above T^{**} , the physical properties are affected by the closing of the unconventional PG and by the related increase in carrier density. In real space, the PG manifests itself as inhomogeneous sub-nanoscale electronic gaps, as detected by scanning tunneling microscopy/spectroscopy [41, 48]. Real-space gaps exist even at temperatures well above T^* , and they were found to close at temperatures proportional to the local gap magnitude [49]. It has been proposed [50] that $\sim 100\%$ and $\sim 50\%$ PG coverage of the CuO_2 planes corresponds to two characteristic temperatures that match T^{**} and T^* , respectively. In this picture, T^* signifies a percolation transition. At a qualitative level, this is consistent with the evidence for a phase transition, including from polarized neutron diffraction [7, 8], polar Kerr effect [9], optical [12], ultrasound [10], thermoelectric [11], and magnetic torque [13, 14] experiments, and with the concomitant absence of a significant specific heat anomaly [51]. Such a phase transition would be a secondary, emergent phenomenon [52].

For correlated metals, it was noted that well-defined quasiparticle excitations may survive at temperatures well above the range of validity of FL theory as signified by the breakdown of a quadratic temperature dependence of the resistivity, before the Ioffe-Regel limit is reached [53]. However, the fact that the scattering rate is nearly unchanged across the cuprate phase diagram (at least up to 400 K) suggests that the effective Fermi energy at low doping is essentially the same as in the overdoped region ($E_F \sim 1$ eV) [54]. This is consistent with the observation of a large, doping-independent Fermi velocity in photoemission studies [55] and with the notion that the effective mass is (nearly) doping and compound independent [4, 26–30]. A large effective Fermi energy ($E_F \gg k_B T$) would also explain why FL-like behavior extends to rather high temperatures. Assuming a simple two-dimensional parabolic band, the Ioffe-Regel limit ($k_F l = hc/(\rho e^2) \sim 1$, where c is the interlayer distance) is approached at 400 K in our most underdoped Hg1201 samples [4]. However, this analysis does not take into account the fact that parts of the Fermi surface are removed by the PG and that the mobile carrier density is overestimated [4], and it neglects the role played by electronic correlations in determining the electronic kinetic

energy [20]. In fact, the room-temperature mobility, $\mu = (H \cot(\Theta_H))^{-1} \approx 10 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, is not unusual and comparable to that of ordinary metals such as Aluminum [56]. The situation appears to be more complex in underdoped compounds such as LSCO that exhibit a considerable non-universal resistivity contribution characterized by a logarithmic low-temperature upturn [23, 30], although the underlying FL transport behavior persists to very low hole-dopant concentrations, as seen from the universal temperature dependences of the resistivity [4, 5] and of $\cot(\Theta_H)$. This additional complexity is similar to that in certain inhomogeneous conventional metals [23, 30, 57]. We note that it was recently demonstrated that FL transport behavior (with nearly the same value of C_2) prevails even deep in the AF phase of the electron-doped cuprates, where the non-universal resistivity upturn is particularly prominent [58].

6. Concluding remarks

Our findings point to the need for a paradigm shift regarding the cuprate phase diagram. The observation that $\cot(\Theta_H) \propto T^2$ in the SM region was first made in the early days of cuprate research and, in fact, a FL interpretation was given in the early 1990s [15]. However, this interpretation of the charge transport has not been given much attention since crucial experimental facts were not known. Similarly, it has long been known that, analogous to other complex materials, the cuprates are inherently inhomogeneous as a result of martensitic strain accommodation [42, 43]. In conjunction with the recent demonstration of FL charge transport in the PG region [4, 22, 23], the results for Hg1201 reported here unambiguously demonstrate a profound connection between the PG/FL and SM states, as $\cot(\Theta_H) = C_2 T^2$ remains unaffected upon crossing T^{**} and T^* . Furthermore, we demonstrate in figures 3 and 4 that this behavior is (nearly) doping and compound independent, and thus universal, which establishes a direct connection between the FL/PG region and the well-accepted FL state on the overdoped side of the phase diagram. We note that it is important to keep in mind that the PG/FL state is unusual, as it features arcs rather than a closed Fermi surface. The present results imply that the states on the arcs are remnants of the states of the large Fermi surface at high doping, where the system exhibits standard FL behavior. Notably, our work also implies that the underlying Fermi surface in the PG regime is closed and encompasses $1 + p$ states, which is supported by recent photoemission spectroscopy work [59].

The universal temperature dependence of $\cot(\Theta_H)$ and, in particular, the de facto universal value of C_2 provides an unprecedented constraint on any physical interpretation. To our knowledge, no prior model for the cuprates is consistent with the above experimental facts. Whereas some theoretical models seem to capture the experimental observations made in the overdoped region, where with decreasing doping the planar resistivity gradually evolves from quadratic to linear temperature dependence, we emphasize that, at a fixed doping level, the resistivity in the model compound Hg1201 switches from purely T^2 (PG/FL) to purely T (SM) without any change in C_2 . This experimental fact alone excludes interpretations of the transport properties based on an anisotropic scattering rate (e.g. [24, 32]). Namely, it would seem highly unphysical that in distinct parts of the phase diagram ($T_c < T < T^{**}$ versus $T > T^*$) the scattering rates are qualitatively different (or correspond to different parts of the Fermi surface) without any significant change in $\cot(\Theta_H) = C_2 T^2$. Moreover, the fact that $\cot(\Theta_H)$ is nearly doping and compound independent provides a profound connection among all the regions of the phase diagram (two of which exhibit clear FL quasiparticle behavior) and excludes narrow theoretical interpretations based on the behavior of any particular compound in a specific doping and temperature range.

One pivotal goal of our work is to separate underlying fundamental properties of the cuprates from those that are compound specific. Only once the former are firmly established is it feasible to address the latter. In this regard, it is important to note that compounds such as $\text{Bi}_2(\text{Sr},\text{La})_2\text{CuO}_{6+\delta}$ (Bi2201) and $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ (Bi2212) do not show the underlying quadratic temperature dependence of the planar resistivity in the PG/FL regime [4], and that LSCO and twinned samples of YBCO do not obey Kohler's rule for the magnetoresistance [23]. Nevertheless, the quadratic temperature dependence of the planar resistivity and Kohler's rule clearly are underlying fundamental properties of the doped CuO_2 sheets, with compound-specific deviations that can be understood [4, 23, 58]. In the present work, we demonstrate for LSCO that the large apparent deviation from the underlying universal behavior of the cotangent of the Hall angle for $x > 0.08$ can be understood to result from a combination of a compound-specific Fermi-surface evolution and effects related to the opening of the PG. Upon correcting for this, the underlying universal value of C_2 is recovered. This simple and straightforward result has profound consequences for our understanding of the cuprates. Namely, instead of evoking any exotic interpretations of their physical properties, classic interpretations should first be tried and tested. We thus suspect that the (rather small) deviations from the underlying universal behavior seen in certain compounds, doping and temperature ranges (e.g., Bi2201 [60] in part of the SM region, or Tl2201 at temperatures below 22 K [61]) have a 'benign' origin. Just as in the case of LSCO, where these deviations appear to be the strongest, they most probably are not the result of a failure of the FL concept. In fact, it has been demonstrated for Tl2201 [24]

that a slight difference in Fermi-surface shape may result in a substantially different σ_{xy} . The temperature- and doping-dependent partial gapping of a non-circular Fermi surface will thus surely cause deviations from the underlying universal transport behavior.

The observation of a FL transport scattering rate in an inherently inhomogeneous system remains a challenge to capture theoretically at a microscopic level. It appears necessary to explicitly include the planar oxygen degrees of freedom. We note that calculations indicate that direct oxygen–oxygen propagation may generate arcs with sizeable oxygen spectral weight at the Fermi level [17, 38]. Moreover, umklapp interactions might be essential to obtain the T^2 scattering rate [4, 17, 18]. Regardless of the ultimate microscopic description, the transport results presented here imply that the transformation from a state with a hole density of $(1 + p)/V$ to a state with a density of p/V holes is complete at T^{**} [49, 50]. At temperatures below T^{**} , these $n_H = p/V$ planar holes per CuO_2 unit give rise to the previously observed unmasked PG/FL behavior [4, 22, 23]. This characteristic temperature furthermore appears to be an upper bound to the charge-density-wave order exhibited by a range of cuprates, including Hg1201 [37, 62]. On the very overdoped side of the phase diagram, the observation of pristine FL behavior in both transport and thermodynamic properties [2, 3] indicates that the remnants of the PG are gone. Interestingly, the termination of the SC phase is concomitant with the disappearance of these remnants. The present work demonstrates that these two FL regions are in fact connected. The largely hidden yet ubiquitous FL scattering rate observed throughout the cuprate phase diagram, along with the elucidation of charge transport in the SM region, can be expected to enable a more focused discussion of the remaining challenges presented by these fascinating materials.

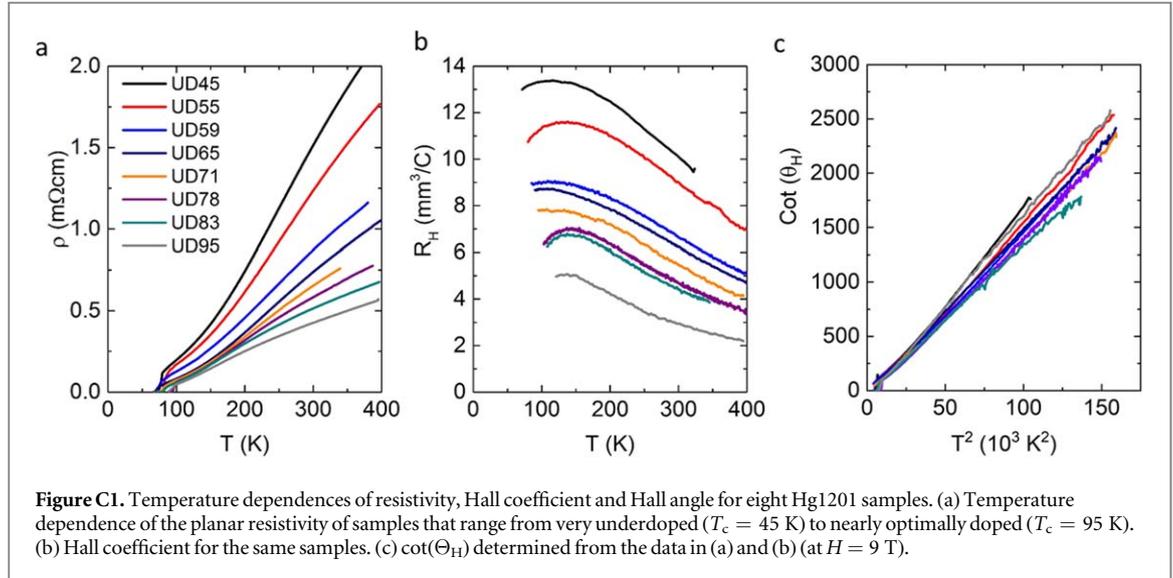
In fact, the observations made in the present work constitute the foundation of significant recent progress in this direction [35, 52, 58, 63, 64]. For example, the universal scattering rate is an essential ingredient in a phenomenological model that captures many of the major mysteries presented by the cuprates [52, 64]. A second crucial ingredient of the model, which also follows from the present work, is the gradual delocalization of one hole per planar CuO_2 unit associated with an inhomogeneous high-energy PG that is a remnant of the charge-transfer gap of the undoped, insulating parent compounds; holes are gradually included in the Fermi sea as the system evolves from p to $1 + p$ itinerant carriers with increasing doping and temperature. With only a few experimentally-constrained parameters, this model quantitatively describes the transport coefficients across the temperature-doping phase diagram, including the PG and SM regimes. The change from a small charge-carrier concentration at low doping/temperature to a large concentration at high doping/temperature appears naturally and gradually, in agreement with the present results. Remarkably, the unusual non-monotonic doping dependence and scaling behavior of the superfluid density, including recent data at very high doping [65], is directly obtained from normal-state properties. The dome-shaped doping dependence of the SC transition temperature T_c also follows naturally. Moreover, the model is consistent with optical conductivity, tunneling and photoemission spectroscopy data, and with the presence of unconventional broken-symmetry phenomena observed below the PG temperature T^* [7–14, 51]. Finally, the model identifies the main characteristics of the SC glue, which must be associated with the same local correlations that localize the one hole per planar CuO_2 unit discerned in the present work.

Acknowledgments

NB is grateful to the late S Barišić for extensive discussions. We thank A V Chubukov, J R Cooper, L Forró, and D van der Marel for comments on the manuscript. NB and WT acknowledge the support of FWF project P27980-N36 and the European Research Council (ERC Consolidator Grant No. 725521). The work at the University of Minnesota was funded by the Department of Energy through the University of Minnesota Center for Quantum Materials, under DE-SC-0006858.

Appendix A. FL behavior in correlated systems

Although the possibility of FL behavior in the PG region of the cuprate phase diagram was initially disputed by many, this interpretation is now increasingly accepted (e.g., [18, 66–68]). In fact, there has been a revival of FL concepts in correlated systems beyond the cuprates [69, 70]. For example, FL behavior has been found in the iron-pnictides [71, 72], and for the Mn-pnictides the evolution from Hund’s insulator to a FL was traced in an optical spectroscopy study [73]. Even the perfectly compensated semimetal WTe_2 , which features electron/hole pockets with a Fermi energy of 20–40 meV, exhibits a T^2 scattering rate up to high temperatures [74]. Another potential example is the recent work on strontium titanate, which was shown to exhibit a T^2 resistivity even at very low carrier densities ($\approx 10^{17} \text{ cm}^{-3}$) [75]. At those carrier densities, only a single pocket is present at the Fermi level, and the Fermi energy is merely 1 meV.



Appendix B. Sample preparation, resistivity, Hall coefficient and Hall angle

The Hg1201 samples were synthesized, annealed at various temperatures and oxygen partial pressures in order to adjust the hole concentration, and subsequently contacted according to previously reported procedures [4, 21, 76]. The SC transition temperature (T_c) was determined with a Quantum Design, Inc., Magnetic Properties Measurement System. The quoted T_c values correspond to the transition mid-point (10%–90% of the diamagnetic signal appears within 1 K). A small ‘diamagnetic tail’ can be found to extend to higher temperatures as a result of filamentary superconductivity. The latter can shorten the sample and cause a resistivity drop already at temperatures above the bulk T_c . The doping levels of the samples were assessed using the measured T_c values and the universal thermoelectric power scale [77, 78]. The transport measurements were carried out with a Quantum Design, Inc., Physical Properties Measurement System (PPMS). That Hall data were assessed at $H = 9$ T. In order to properly contact *ac* surfaces, the samples had to be cleaved, which introduced an uncertainty of 10%–20% in the estimate of the sample contact dimensions [4].

Appendix C. Resistivity, Hall coefficient and Hall angle in Hg1201

Figure C1 shows the temperature dependences of the planar resistivity and Hall effect for eight samples in the doping range $0.05 < p < 0.14$. Representative data for three of these samples are shown in figure 2. As discussed in the main text, the resistivity exhibits linear and quadratic temperature dependences above and below the characteristic temperatures T^* and T^{**} , respectively. Nevertheless, $\cot(\Theta_H)$ for all samples exhibits doping-independent T^2 behavior from just above T_c up to the highest measured temperature of 400 K. We attribute the small differences in the slope $C_2 = \cot(\Theta_H)/T^2$ to the systematic error associated with the estimation of the exact sample geometry. Indeed, as seen from figure C1(c), no systematic tendency is observed as a function of doping. All Hg1201 samples are found to exhibit negligible extrapolated residual resistance, and thus $\cot(\Theta_H)$ is presented as measured, without any offset.

Figure C2 shows the ratio of nominal to measured carrier density as a function of temperature for Hg1201. Below approximately 200 K, all samples exhibit a maximum value that is approximately 20% lower than 1. While there exists an estimated 10%–20% uncertainty in the determination of the sample geometry, and hence in the absolute value of R_H for each of the measured samples, the systematically lower value of $eR_H p/V$ more likely results from a somewhat subtle uncertainty in the estimation of the hole concentration p for those cuprates in which the hole doping level is tuned via changes of interstitial oxygen density [79]. We emphasize that this systematic deviation does not affect any of our conclusions. In particular, we find that $n_H \propto p$, consistent with the result for LSCO ($p = x < 0.08$) and with the observation that the dc-resistivity scales as $1/p$ ([4]). In fact, a systematically larger carrier density of $\sim 25\%$ for Hg1201 would shift the center of the $T(p)$ plateau and the doping level of the strongest charge-order effects from $p \approx 0.09$ to $p = 0.11$ – 0.12 , consistent with analogous results for other cuprates [8, 37].

From figure C2 it can also be seen that the peak exhibited by $eR_H p/V$ is rather broad at lower doping, whereas it is narrower close to optimal doping, consistent with the narrowing of the PG/FL region with increasing hole concentration.

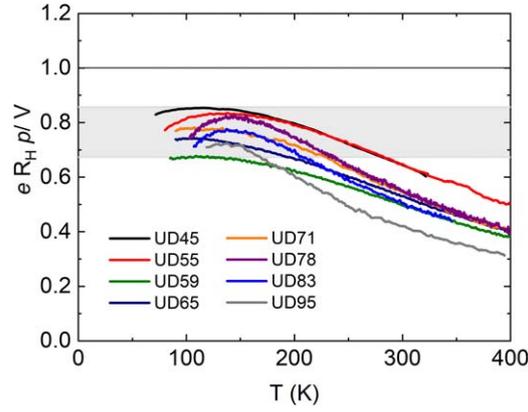


Figure C2. Temperature dependence of the ratio of nominal hole concentration, p/V , and measured carrier density, $n_H = 1/(eR_H)$. The grey horizontal band indicates the range 0.76 ± 0.09 . e is electron charge and V the unit cell volume. This ratio should yield a value of 1 if the carrier density measured by the Hall effect corresponds to p . As discussed in the main text, for LSCO this is indeed the case in the PG/FL region (for $p = x < 0.08$ and $T < T^{**}$) [5].

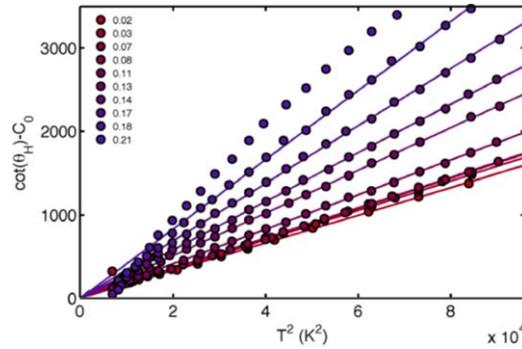
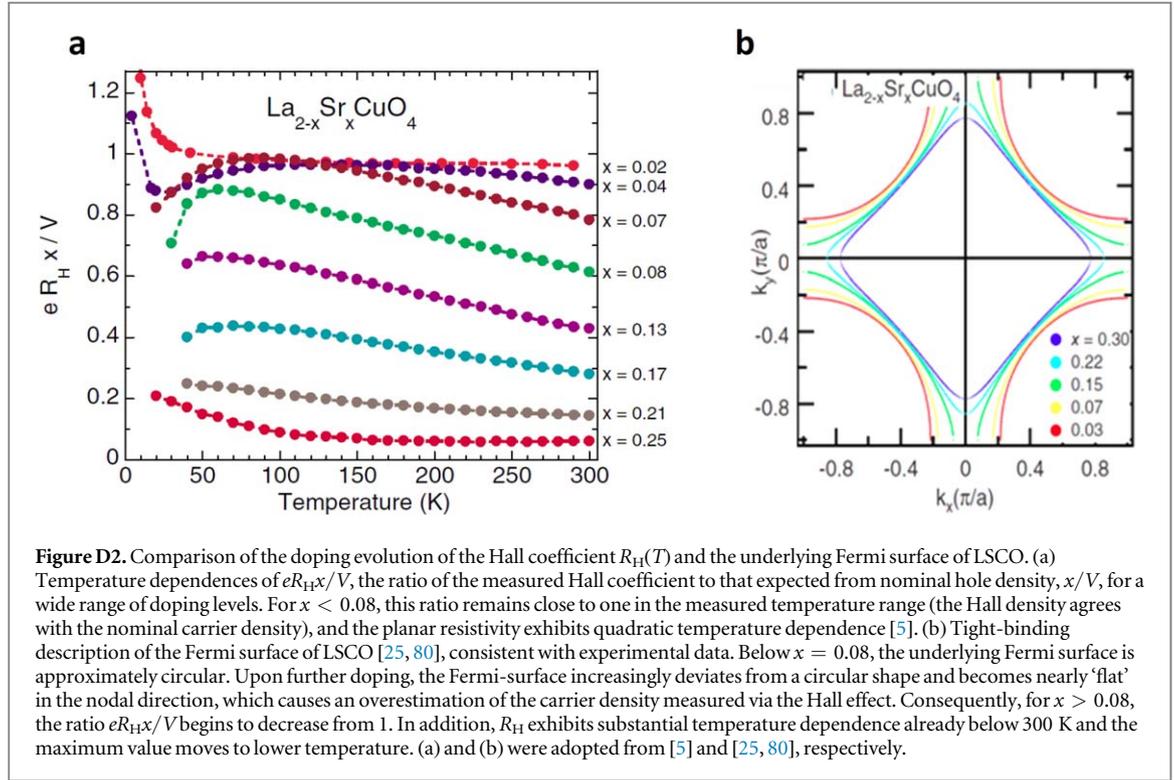


Figure D1. Hall angle in LSCO for $p > 0.08$. Temperature dependence of $\cot(\Theta_H) - C_0$ for LSCO shows quadratic behavior for a very wide range of Sr doping values x (data from [5]). Low-temperature data are not shown for clarity, due to large upturns for the most underdoped samples. Solid lines are fits to $C_2 T^2$. The so-obtained C_2 values are shown in figure 3(b). The data for $x = 0.21$ do not exhibit a quadratic temperature dependence and were not fit.

Appendix D. Analysis of the Hall angle for LSCO ($p > 0.08$)

As discussed in [25, 38, 80] and in the main text, with increasing doping the Fermi-surface topology of LSCO evolves from arcs to a diamond-like shape, and the Hall coefficient ceases to be a good measure of the carrier density. For LSCO, this becomes noticeable already for $p = x > 0.08$. Consequently, C_2 begins to deviate from the established universal value (figures 3(b) and D1). Nevertheless, the simple quadratic temperature dependence $\cot(\Theta_H) - C_0 \propto T^2$ remains omnipresent. This indicates that the temperature dependence of the evolution from arcs toward the full Fermi surface, which is related to gradual closing of the antinodal PG at temperatures above T^{**} , is still captured by the Hall coefficient. However, R_H is related to the curvature of the Fermi surface and ceases to be a reliable measure of the carrier density. Indeed, as shown in figure D2, the nodal Fermi-surface curvature ceases to be nearly circular above about $p \approx 0.07$ and, concomitantly, the Hall effect overestimates the carrier density. The nearly straight Fermi-surface segments near $p = 0.22$ result in the apparent divergence of n_H .

We consider two methods to correct for this effect. In the first method, we use the recently established temperature and doping dependence of the universal sheet resistance. In contrast to the Hall coefficient, $R_H = \sigma_{xy}/(H\sigma_{xx}\sigma_{yy})$, this observable is not particularly sensitive to the Fermi surface curvature. In the PG/FL part of the phase diagram, the sheet resistance is simply proportional to T^2/p ([4]), and the scattering rate follows $1/\tau \propto T^2$ ([4, 22, 23]), whereas R_H is approximately constant below T^{**} . Since there is very good evidence that the effective mass m^* does not change with doping (e.g., from specific heat [81, 82], optical conductivity [26], and dc transport; see main text and [4]), the Drude formula $\rho = m^*/(ne^2\tau)$ implies a carrier density $n = p/V$. This suggests that the Hall data for LSCO (figure D2) ought to be corrected (for $p = x > 0.08$), i.e., we replace $n_H = 1/(eR_H)$ by $n_H(T) = (p/V)R_{H,\max}(p)/R_H(p,T)$, where $R_{H,\max}(p)$ is the maximum in the temperature



dependence of the Hall coefficient. As demonstrated in figure 3(b), this adjustment of $\cot(\Theta_H) = \rho/(H\rho_H)$ indeed yields the universal value of C_2 .

The second method to correct $R_H(x, T)$ for $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ is very similar to the first. Whereas the first method uses the maximum of $R_H(T)$ at each doping level, the second method is based on [83], where the carrier density $n(x, T)$ is described in a heuristic fashion as the sum of a doping dependent contribution, $n_0(x)$, that gives the density of carriers in the PG/FL region as measured by the Hall effect, and of a thermally-activated contribution, $n_1(x) \exp[-\Delta(x)/T]$, that is relevant at higher temperatures:

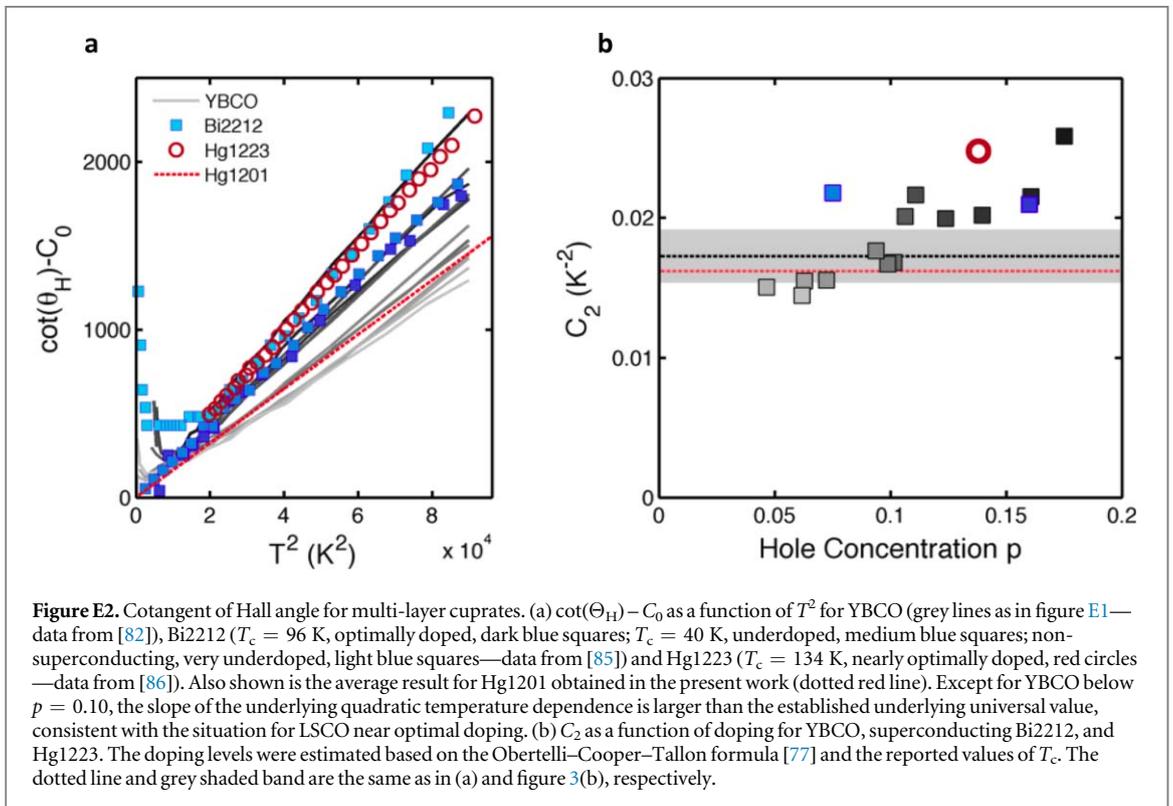
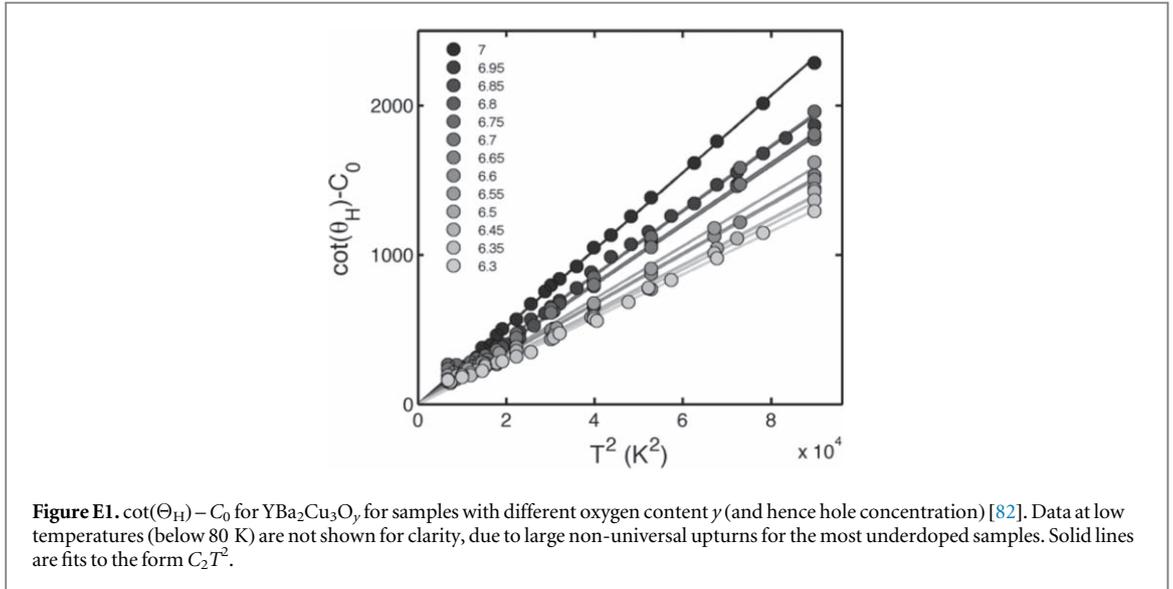
$$n_H(x, T) = n_0(x) + n_1(x) \exp[-\Delta(x)/T].$$

Indeed, for $x < 0.08$, $n_0(x)$ equals the nominal carrier concentration $p = x$, whereas for $x > 0.08$ the absolute value of $n_H = 1/(eR_H)$ should be corrected (but not its temperature dependence, as argued above). Instead of using the estimated value $R_{H,\max}$ we can use the value of n_0 determined from the fit to correct the absolute value of the Hall effect. Due to the rather small difference between in $R_{H,\max}$ and n_0 , the two methods yield very similar results for the corrected value of C_2 .

Appendix E. Hall-angle results for multi-layer cuprates

$\text{YBa}_2\text{Ca}_3\text{O}_{6+\delta}$ (YBCO) features CuO_2 double-layers, Cu–O chains, and is orthorhombic in the SC doping range, and hence structurally more complex than single-layer compounds, especially compared to simple-tetragonal Hg1201. A quadratic temperature dependence of $\cot(\Theta_H)$ was reported early on up to elevated temperatures (500 °C) [32, 84]. Extensive Hall data were obtained in subsequent work, and an attempt was made to separate contributions due to the CuO_2 planes from those of the Cu–O chains [82]. These latter data, which span a rather wide doping range and are reproduced in figures E1 and E2, demonstrate that, for $p < 0.10$, C_2 is consistent with the universal value established for the single-layer compounds. For $p > 0.10$, YBCO behaves similar to LSCO (see appendix D). Figure E2 also shows data for double-layer $\text{Bi}_2\text{SrCa}_{1-x}\text{Y}_x\text{Cu}_2\text{O}_{8+\delta}$ (Bi2212; [85]) and triple-layer $\text{HgBa}_2\text{Ca}_2\text{Cu}_3\text{O}_{8+\delta}$ (Hg1223; [86]).

The Fermi surfaces of these compounds are inherently more complicated due to the multi-layer structure. As noted, in the case of YBCO it is necessary to carefully separate Cu–O chain from CuO_2 plane contributions. In the Bi-based cuprates, the underlying quadratic temperature dependence of the resistivity in the PG/FL region is masked ([4]), yet the quadratic scattering rate is clearly revealed from the temperature dependence of $\cot(\Theta_H)$ (figure E2). In triple-layer Hg1223, the inequivalent inner and outer layers might have different hole concentrations and different levels of intrinsic inhomogeneity. In light of this additional complexity, the data for



the multi-layer cuprates are remarkably consistent with those for the single-layer compounds discussed in the main text.

Appendix F. General observations related to optical conductivity and photoemission spectroscopy results

Recent analysis of the zero-frequency limit of the optical conductivity established for several transition-metal oxides the temperature dependence of the effective plasma frequency and revealed a hidden FL scattering rate, $1/\tau \propto T^2$ ([69]). This result was obtained for V_2O_3 and NdNiO_3 , two correlated materials that exhibit a temperature-driven metal-insulator transition, and for CaRuO_3 , which is a Hund's metal. The observation that the anomalous transport properties of these complex materials arise from a temperature-dependent plasma frequency ($\omega_p^2 \propto n/m^*$) is consistent with our findings, yet the temperature dependence was ascribed to the effective mass rather than the carrier density [69]. We can exclude the former possibility in the case of the

cuprates, since $\cot(\Theta_H) - C_0 = C_2 T^2 \propto m^*/\tau$ is universal, and thus very unlikely the result of a compensation between separate doping/temperature dependences of the scattering rate and effective mass. Our result instead naturally demonstrates the existence of a universal transport scattering rate, $1/\tau \propto T^2$, throughout the entire phase diagram, and it suggests that the effective mass is independent of doping and temperature, in the temperature range relevant to our discussion.

We note that quantum oscillation experiments for underdoped YBCO and Hg1201 indicate a small, pocket-like Fermi-surface with an effective mass of $m^* = 2-3 m_e$ (m_e is the free-electron mass) that is approximately half as large as that for highly doped Tl2201 [87]. Whereas the small Fermi surface measured in underdoped Hg1201 and YBCO is the result of a Fermi-surface reconstruction [37, 62, 87–89] that can be expected to modify the effective mass, the experiments on Tl2201 determine the large unreconstructed Fermi surface [3] and hence are directly relevant to the present discussion.

Photoemission experiments typically are carried out on the bismuth-based cuprates for which neither $\rho \propto T^2$ nor Kohler scaling has been reported in the PG/FL region. This could be the result of a particularly high degree of point disorder [43] or inherent inhomogeneity [41–43] exhibited by these compounds, which might cause a substantial temperature dependence of the carrier density even at temperatures below T^{**} . And indeed, despite the apparent non-FL behavior of the resistivity, $\cot(\Theta_H)$ for double-layer $\text{Bi}_2\text{SrCa}_{1-x}\text{Y}_x\text{Cu}_2\text{O}_{8+\delta}$ exhibits quadratic temperature dependence with a prefactor C_2 that agrees rather well with the universal value (figure E2). Although the single-particle lifetime obtained from photoemission is not identical to the transport lifetime, high-resolution photoemission measurements of the normal state of bismuth-based compounds indicate a quadratic energy dependence of the scattering rate [90]. Moreover, for LSCO ($p = x = 0.23$), photoemission spectroscopy indeed yields quadratic frequency dependence of the self-energy in the nodal region, consistent with our findings, but an approximately linear behavior in the antinodal region [91]. At the same doping level the resistivity can be decomposed into quadratic and linear terms [4] and $R_H(T)$ still exhibits significant temperature dependence below about 200 K [5, 39]. Consequently, in those parts of the phase diagram where $R_H(T)$ exhibits substantial temperature dependence and where, in accord with our finding of a universal scattering rate, the carrier density can not be assumed to be independent of temperature, it seems necessary for photoemission results in the antinodal region to be re-analyzed. These insights are further supported by the success of the recent phenomenological model of [52, 64].

Appendix G. Suggestion of a novel approach to analyze the optical conductivity

In the main text, we briefly discuss optical conductivity data in order to demonstrate that these (as well as photoemission) results are not inconsistent with our proposed interpretation of the dc transport data. Here, we emphasize that the commonly applied extended Drude analysis should be treated with care in the case of systems for which a simple single-band approach is insufficient. This seems to be particularly relevant to the cuprates at temperatures above T^{**} , i.e., outside the PG/FL region.

More generally, in light of our dc transport results, we believe that all optical conductivity data for the cuprates need to be re-analyzed. While this analysis is clearly beyond the scope of the present work, our results give several key constraints. First, instead of the prior approaches, we suggest that the low-frequency data that correspond to the coherence peak are fit throughout the entire phase diagram (i.e., not only in the PG/FL and FL, but also in the SM region) in a FL manner, with $1/\tau \propto (\hbar\omega)^2 + (a \pi k_B T)^2$. We suggest three different approaches to fix the coefficient a : (i) from fits to $1/\tau \propto (\hbar\omega)^2 + (a \pi k_B T)^2$ in the PG/FL or FL regions; (ii) from an extended Drude analysis in the PG/FL or FL regions (e.g., $a = 1.5$ [22]); (iii) a can be fixed to the theoretically predicted value $a = 2$ [92, 93]. Once the value of a has been determined, it should be held fixed in the SM region, and the coherent spectral weight should be matched to the carrier density determined from the Hall effect or dc-resistivity [52, 64]. This procedure implies that there is essentially no free parameter for the coherent spectral weight in the SM region.

The second constraint pertains to the delocalization of one carrier per planar copper atom at temperatures above T^{**} . The redistribution of spectral weight with temperature at a fixed nominal doping level p should bear important similarities to the evolution with doping at a fixed temperature. Indeed, it is remarkable that the spectral weight of the coherent contribution at temperatures below T^{**} corresponds to p , whereas the spectral weight integrated to about 2.5 eV (on the order of the charge-transfer gap) approaches $1 + p$ (where we attribute 1 to the localized charge). With this in mind, one can now take a fresh look at the doping dependence of the optical conductivity in this energy range. We consider the extensive early data for LSCO [94], which are reproduced in figure G1. Without any detailed analysis, it is indeed possible to follow the evolution of a signature of the localized charge from a hump at intermediate energy at low doping ($x = p$ for LSCO) to the quasiparticle peak at high doping. We expect a corresponding evolution with temperature at fixed doping.

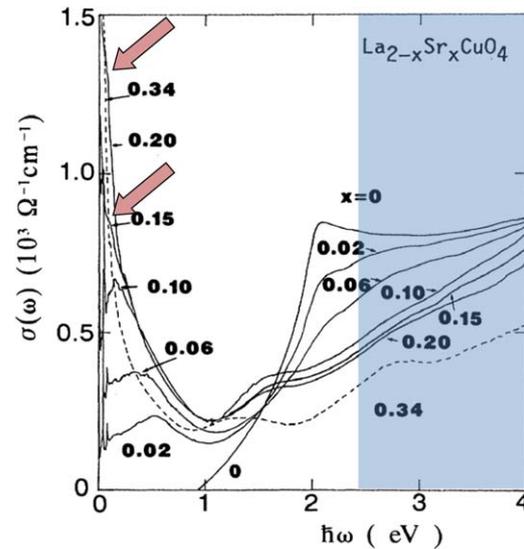


Figure G1. Planar optical conductivity for LSCO, measured at room temperature (adapted from 94). The frequency range of interest (up to about 2.5 eV; white background) approximately corresponds to $1 + p$ holes per CuO_2 unit [22]. We associate the ‘1’ with the doping-dependent ‘hump’ that moves toward low energy with increasing nominal hole concentration p . At low doping, this feature is easily seen as a local maximum. At $x = p = 0.15$ and 0.20 , the hump is indicated by arrows. At $x = 0.15$, it is seen to have nearly merged with the coherent quasiparticle peak, whereas at $x = 0.20$ only a weak ‘shoulder’ can be discerned (arrows). Finally, at $x = 0.34$, the low-frequency response is dominated by a simple quasiparticle peak.

References

- [1] Keimer B, Kivelson S A, Norman M R, Uchida S and Zaanen J 2015 *Nature* **518** 179
- [2] Nakamae S et al 2003 *Phys. Rev. B* **68** 100502
- [3] Vignolle B et al 2008 *Nature* **455** 952
- [4] Barišić N et al 2013 *Proc. Natl Acad. Sci. USA* **110** 12235
- [5] Ando Y, Kurita Y, Komiya S, Ono S and Segawa K 2004 *Phys. Rev. Lett.* **92** 197001
- [6] Gurvitch M and Fiory A T 1987 *Phys. Rev. Lett.* **59** 1337
- [7] Fauqué B et al 2006 *Phys. Rev. Lett.* **96** 197001
- [8] Li Y et al 2008 *Nature* **455** 372
- [9] Xia J et al 2008 *Phys. Rev. Lett.* **100** 127002
- [10] Shekhter A et al 2013 *Nature* **498** 75
- [11] Daou R et al 2010 *Nature* **463** 519
- [12] Zhao L et al 2017 *Nat. Phys.* **13** 250
- [13] Sato Y et al 2017 *Nat. Phys.* **13** 1074
- [14] Murayama H et al 2019 *Nat. Commun.* **10** 3282
- [15] Kubo Y and Manako T 1992 *Physica C* **197** 378
- [16] Laughlin R B 2014 *Phys. Rev. B* **89** 035134
- [17] Barišić S and Barišić O S 2012 *J. Supercond. Nov. Magn.* **25** 669
- [18] Gor’kov L P and Teitel’baum G B 2015 *Sci. Rep.* **5** 8524
- [19] Luo N and Miley G H 2009 *J. Phys. Condens. Matter* **21** 025701
- [20] Gunnarsson O, Calandra M and Han J E 2003 *Rev. Mod. Phys.* **75** 1085
- [21] Barišić N et al 2008 *Phys. Rev. B* **78** 054518
- [22] Mirzaei S I et al 2013 *Proc. Natl Acad. Sci. USA* **110** 5774
- [23] Chan M K et al 2014 *Phys. Rev. Lett.* **113** 177005
- [24] Kokalj J, Hussey N E and McKenzie R H 2012 *Phys. Rev. B* **86** 045132
- [25] Hashimoto M et al 2008 *Phys. Rev. B* **77** 094516
- [26] Padilla W J et al 2001 *Phys. Rev. B* **72** 060511
- [27] Basov D N and Timusk T 2005 *Rev. Mod. Phys.* **77** 721
- [28] Yoshida T et al 2012 *J. Phys. Soc. Japan* **81** 011006
- [29] Dai Y M et al 2012 *Phys. Rev. B* **85** 092504
- [30] Ando Y, Lavrov A N, Komiya S, Segawa K and Sun X F 2001 *Phys. Rev. Lett.* **87** 017001
- [31] Anderson P W 1991 *Phys. Rev. Lett.* **67** 2092
- [32] Chien T R, Wang Z Z and Ong N P 1991 *Phys. Rev. Lett.* **67** 2088
- [33] Lee W S et al 2007 *Nature* **450** 81
- [34] Pelc D et al 2018 *Nat. Commun.* **9** 4327
- [35] Popčević P et al 2018 *Nat. Quant. Matt.* **3** 42
- [36] Yu G et al 2019 *Phys. Rev. B* **99** 214502
- [37] Tabis W et al 2017 *Phys. Rev. B* **96** 134510
- [38] Nikšić G, Kupčić I, Barišić O S, Sunko D K and Barišić S 2014 *J. Supercond. Nov. Magn.* **27** 969
- [39] Hwang H Y et al 1994 *Phys. Rev. Lett.* **72** 2636
- [40] Luttinger J M 1960 *Phys. Rev.* **119** 1153
- [41] Alldredge J W, Fujita K, Eisaki H, Uchida S and McElroy K 2013 *Phys. Rev. B* **87** 104520

- [42] Krumhansl J A 1992 *Proceedings of the Conference* (New Mexico: Santa Fe)
- [43] Phillips J C, Saxena A and Bishop A P 2003 *Rep. Prog. Phys.* **66** 2111
- [44] Pelc D, Anderson Z, Yu B, Leighton C and Greven M 2019 *Nat. Commun.* **10** 2729
- [45] Eisaki H et al 2004 *Phys. Rev. B* **69** 064512
- [46] Rybicki D et al 2009 *J. Supercond. Nov. Magn.* **22** 179
- [47] Haase J et al 2012 *Phys. Rev. B* **85** 104517
- [48] Pan S H et al 2001 *Nature* **413** 282
- [49] Gomes K K et al 2007 *Nature* **447** 569
- [50] Honma T and Hor P H 2015 *Physica C* **509** 11
- [51] Cooper J R, Loram J W, Kokanović I, Storey J G and Tallon J L 2014 *Phys. Rev. B* **89** 201104
- [52] Pelc D, Popčević P, Požek M, Greven M and Barišić N 2019 *Sci. Adv.* **5** eaau4538
- [53] Deng X et al 2013 *Phys. Rev. Lett.* **110** 086401
- [54] Graf J et al 2007 *Phys. Rev. Lett.* **98** 067004
- [55] Zhou X J et al 2003 *Nature* **423** 398
- [56] Kasap S O 2006 *Principles of Electronic Materials and Devices* vol 3 (New York: McGraw-Hill)
- [57] Arnason S B, Herschfield S P and Hebard A F 1998 *Phys. Rev. Lett.* **81** 3936
- [58] Li Y, Tabis W, Yu G, Barišić N and Greven M 2016 *Phys. Rev. Lett.* **117** 197001
- [59] Drozdov I K et al 2018 *Nat. Commun.* **9** 5210
- [60] Konstantinović Z, Li Z Z and Raffy H 2000 *Phys. Rev. B* **62** R11989
- [61] Mackenzie A P, Julian S R, Sinclair D C and Lin C T 1996 *Phys. Rev. B* **53** 5848
- [62] Tabis W et al 2014 *Nat. Commun.* **5** 5875
- [63] Li Y et al 2019 *Sci. Adv.* **5** eaap7349
- [64] Pelc D et al 2019 arXiv:1902.00529
- [65] Božović I, He X, Wu J and Bollinger A T 2016 *Nature* **536** 309
- [66] Varma C M 2014 *J. Phys. Condens. Matter* **26** 505701
- [67] Punk M, Allais A and Sachdev S 2015 *Proc. Natl. Acad. Sci. USA* **112** 9552
- [68] Buhmann J M, Ossadnik M, Rice T M and Sigrist M 2013 *Phys. Rev. B* **87** 035129
- [69] Deng X, Sternbach S, Haule K, Basov D N and Kotliar G 2014 *Phys. Rev. Lett.* **113** 246404
- [70] Dang H T, Mravlje J, Georges A and Millis A J 2015 *Phys. Rev. Lett.* **115** 107003
- [71] Wu D et al 2010 *Phys. Rev. B* **81** 100512
- [72] Barišić N et al 2010 *Phys. Rev. B* **82** 054518
- [73] McNally D E et al 2015 *Phys. Rev. B* **92** 115142
- [74] Homes C C et al 2015 *Phys. Rev. B* **92** 161104
- [75] Lin X, Fauqué B and Behnia B 2015 *Science* **349** 945
- [76] Zhao X et al 2006 *Adv. Mater.* **18** 3243
- [77] Obertelli S D, Cooper J R and Tallon J L 1992 *Phys. Rev. B* **46** 14928
- [78] Yamamoto A, Hu W Z and Tajima S 2000 *Phys. Rev. B* **63** 024504
- [79] Loram J W, Mirza K A, Liang W Y and Osborne J A 1989 *Physica C* **162** 498
- [80] Yoshida T et al 2007 *J. Phys. Condens. Matter* **19** 125209
- [81] Kumagai K et al 1993 *Phys. Rev. B* **48** 7636
- [82] Segawa K et al 2004 *Phys. Rev. B* **69** 104521
- [83] Gor'kov L P and Teitel'baum G B 2006 *Phys. Rev. Lett.* **97** 247003
- [84] Harris J M, Yan Y F and Ong N P 1992 *Phys. Rev. B* **46** 14293
- [85] Kendziora C, Mandrus D, Mihály D and Forró L 1992 *Phys. Rev. B* **46** 14297
- [86] Carrington A et al 1994 *Physica C* **234** 11
- [87] Barišić N et al 2013 *Nat. Phys.* **9** 761
- [88] Harrison N and Sebastian S E 2011 *Phys. Rev. Lett.* **106** 226402
- [89] Chan M K et al 2016 *Nat. Commun.* **7** 12244
- [90] Yamasaki T et al 2007 *Phys. Rev. B* **75** 140513
- [91] Chang J et al 2013 *Nat. Commun.* **4** 2559
- [92] Gurzhi R N 1959 *Sov. Phys. JETP* **35** 673
- [93] Maslov D L and Chubukov A V 2012 *Phys. Rev. B* **86** 155137
- [94] Uchida S et al 1991 *Phys. Rev. B* **43** 7942